DEUTSCHES ELEKTRONEN-SYNCHROTRON DESY



LONGITUDINAL-TRANSVERSE MODE COUPLING IN LOCALIZED STRUCTURES WITH ORBIT DEPENDENT HIGHER ORDER MODE LOSSES

bу

R.D. Kohaupt

Deutsches Elektronen-Synchrotron DESY, Hamburg

ISSN 0418-9833

NOTKESTRASSE 85 · 2 HAMBURG 52

DESY behält sich alle Rechte für den Fall der Schutzrechtserteilung und für die wirtschaftliche Verwertung der in diesem Bericht enthaltenen Informationen vor.

 A state of the sta ترية أوجلها ترية أوجله

ing dia ka Mangalari Mangalari

्रिक्ट के दिने हैं। जुने के कि कि कि कि कि

1.11

(1, 1)

t Angeleine Stategiet og

an start and a eriste Alexandre

 $\sigma = \beta$

DESY reserves all rights for commercial use of information included in this report, especially in case of filing application for or grant of patents.

> To be sure that your preprints are promptly included in the HIGH ENERGY PHYSICS INDEX , send them to the following address (if possible by air mail) :

> > DESY Bibliothek Notkestrasse 85 2 Hamburg 52 Germany

ISSN 0418-9833

Longitudinal-Transverse Mode Coupling in Localized Structures with Orbit Dependent Higher Order Mode Losses

R.O. Kohaupt Deutsches Elektronen-Synchrotron DESY, Hamburg

Introduction

The vertical "PETRA instability" was theoretically described in terms of transverse mode coupling 1,2,3. In the meantime, transverse mode coupling has been extensively treated by several authors 4,5,6,7,8. Since current limitations still present in PETRA are connected with satellite resonances⁹, the question arises whether localized structures can couple the transverse head-tail modes to the longitudinal shape-modes near satellite resonances and can this lead to an unstable collective motion.

The mathematical properties of transverse mode functions leading to transverse mode coupling hold also in the case of longitudinal-transverse mode coupling. The interaction between transverse and longitudinal collective motion is governed by the <u>transverse impedances</u> and that part of the <u>longitudinal impe-dance</u> which depends on the orbit position, both related by Maxwell's equations. The expected effect will therefore strongly depend on closed orbit deviations, a characteristic property of the observed current limitations in PETRA. The effect essentially differs from those effects which have recently been studied for localized structures^{10,11}).

In this article the effect is studied theoretically in the framework of the Vlasow equation 12 .

Vlasow equation

longitudinal

If ϑ denotes the longitudinal angular coordinate of a particle with respect to the equilibrium particle, the perturbation of the longitudinal distribution F obeys a Vlasow equation

$$\left\{\frac{\partial}{\partial t} + \omega_{\rm S} \frac{\partial}{\partial \Psi}\right\} F = \frac{\partial}{\partial r} W_0(r) \omega_{\rm S} \frac{F_{\rm H}[G, \vartheta, t]}{h U_{\rm C}} \sin \Psi$$
(1)

- - - . . .

 $W_0(r) \stackrel{c}{=} stationary distribution$

 $\omega_{c} \stackrel{c}{=} circular sychrotron frequency$

h 🖹 harmonic number

 $\overline{U}_{c} \stackrel{\text{\tiny f}}{=}$ peak voltage multiplied with cosine of phase angle

 F_{μ} describes the longitudinal "force" as a linear functional of the transverse distribution that will be defined later.

The longitudinal coordinate has been parameterized according to

$$\vartheta = r \cos \Psi$$
 (2)

transverse

In the the transverse case we introduce the "quasi-time"²⁾ defined by

$$\tau = \frac{\varphi(\mathbf{s}(\mathbf{t}))}{\omega_{\beta}} \tag{3}$$

s 🖆 longitudinal coordinate along the ring

φ(s) ≘ phase advance

ω_β ≙ ω_ο Q_β

 $\omega_0 \stackrel{\circ}{=} circular revolution frequency$

 $Q_{\beta} \stackrel{\circ}{=} \text{transverse } Q - value$

Instead of the transverse coordinate x we introduce the Courant-Snyder coordinate z with help of the amplitude function $\beta(s)$

 $z = x/\sqrt{\beta}$ (4)

The coordinate z will be parameterized according to

$$z = \rho \cdot \cos \varphi \tag{5}$$

The Vlasow equation for the transverse perturbation $G(\rho, \phi; r, \Psi)$ then reads

$$\left\{\frac{\partial}{\partial\tau} + \omega_{\beta}\frac{\partial}{\partial\varphi} + \omega_{s}\frac{\partial}{\partial\Psi}\right\}G = \frac{F_{L}[F,\vartheta,\tau]}{E} \omega_{\beta}\beta^{3/2} W_{O}(r)\frac{\partial}{\partial\rho} U_{O}(\rho) \sin\varphi \quad (6)$$

 $U_{0}(\rho) \cong$ stationary transverse distribution

E ≜ energy.

Since the forces F_u and $F_{\underline{i}}$ are generated within localized objects, they have an explicit time dependence as expressed in Eqs. (1) and (6). Therefore the time dependence of F and G is not trivial.

We make the following "ansatz"

time dependence of	longitudinal	distribution:	e ^{-1ωτ}	(A)
time dependence of	transverse	distribution:	e^{-1MT}	(B)
with the relation	$\Omega = \omega +$	ω _o Q _{βr}		(C)

where Q_{Br} is the integer part of the transverse Q-value.

The function $e^{i\Omega t - i\omega t}$ is periodic in t and τ with period $2\pi/\omega_0$ because of the periodicity property of $\tau(t)$.

We consider the longitudinal force $F_{\mu}[G,\vartheta,t]$ which can be formally written as

$$F_{\mu}[G,\vartheta,t] = \Sigma \quad \tilde{F}_{\mu}(t,p) \ e^{ip\vartheta} \tilde{g}(p) \ e^{-i\Omega\tau}$$
(7a)

Correspondingly for the transverse case we have

$$F_{\underline{I}}[F,\vartheta,\tau] = \sum_{p} \widetilde{F}_{\underline{I}}(\tau,p) e^{ip\vartheta} \widetilde{f}(p) e^{-i\omega t}$$
(7b)

Here $\tilde{g}(p)$, $\tilde{f}(p)$ are Fourier transforms of transverse and longitudinal density functions to be defined later. The "ansatz" (A), (B), (C) "solves" (1) and (6) if we keep only the "dominant" component in the Fourier expansion of $\tilde{F}_{n}(t,p)$, $\tilde{F}(\tau,p)$, namely the component of $e^{\pm i(\Omega\tau - \omega t)}$.

longitudinal and transverse mode functions

For the definition of longitudinal and transverse mode functions we introduce

longitudinal

$$F(\vartheta,t) = f(\vartheta) e^{-i\omega t}$$
 (8a)

$$f(\vartheta) = \int_{-\pi}^{+\pi} d\Psi \int_{0}^{\infty} drr f(r, \Psi) \delta(\vartheta - r \cos \Psi)$$
(8b)

$$\tilde{f}(q) = \int_{-\infty}^{+\infty} d\vartheta \ f(\vartheta) \ e^{-i\vartheta q}$$
(8c)

$$f(r,\Psi) = \sum_{n=-\infty}^{+\infty} f_n(r) e^{in\Psi}$$
(8d)

and similarly

transverse

$$G(\rho,\varphi; r,\Psi;\tau) = G_{\beta}(\rho,\varphi; r,\Psi) e^{-i\Omega\tau}$$
(8e

$$G_{\beta}(\rho,\varphi; r, \Psi) = \sum G_{\beta m}(\rho,\varphi; r) e^{im\Psi}$$
(8f

$$G_{\beta m} = A(\rho) g_m(r) (\cos \varphi + i \frac{\Omega - m\omega_s}{\omega_\beta} \sin \varphi)$$
 (8g

$$g(\vartheta) = \int_{-\infty}^{+\infty} d\Psi \int drr \left(\sum_{m=-\infty}^{+\infty} g_m(r) e^{im\Psi} \right) \delta(\vartheta - \vartheta \cos\varphi) \qquad (8h)$$

$$\widetilde{g}(q) = \int_{-\infty}^{+\infty} d\vartheta \ g(\vartheta) \ e^{-iq\vartheta}$$
(8i

- 4 -

In addition we define the transverse dipole moment according to

$$\overline{z} g_{m}(r) = \int_{-\pi}^{+\pi} d\varphi \int_{0}^{\infty} d\rho \rho G_{\beta m}(\rho, \varphi; r) \rho \cos \varphi \qquad (9)$$

longitudinal and transverse forces

The longitudinal forces are determined by the longitudinal impedance z_w . This impedance can be written as¹³)

$$Z_{\mu} = Z_{0\mu} + Z_{1\mu} \frac{\chi^2}{b^2}$$
(10)

where b is the aperture radius of the object.

The impedance $Z_{1:i}$ effects a longitudinal force which depends on the transverse position x.

If there is a closed orbit deviation x_{CO} at the location of the object, then betatron oscillations of particles lead to a <u>longitudinal force</u> that depends linearly on the betatron displacement x_{β} according to ¹⁴)

$$F_{\mu} \sim 2 Z_{\mu} \frac{x_{CO} \cdot x_{\beta}}{b^2}$$
 (11a)

Since the longitudinal impedance Z_{11} leads to a transverse impedance

$$Z_{\perp} = \frac{C Z_{\perp u}}{b^2 \omega}$$
(11b)

 $\omega \cong$ spectral frequency $C \cong$ velocity of light

a longitudinal collective oscillation can excite betatron oscillations.

The fundamental integral equations

With help of the relations (1) to (11) we can write down the fundamental integral equations for f and g:

$$(\omega - n\omega_{\rm S})f_{\rm n}(\mathbf{r}) = \frac{2I\omega_{\rm S}\sqrt{\beta_0}\overline{Z}\,\overline{x}_{\rm CO}}{h\,\overline{U}_{\rm C}\,b^2} [i]^{n-1} \frac{n}{r} \frac{\partial W_0}{\partial r} \sum_{p=\infty}^{+\infty} \frac{\overline{Z}_{1\,\rm u}(p)}{p} I_{\rm n}(pr)\tilde{g}(p) \quad (12)$$

$$I\sqrt{\beta_0}C\,x_{\rm CO} \quad m \quad i \quad \dots \quad +\infty \quad \overline{Z}_{1\rm u}^+(p)$$

$$[\Omega - (\omega_{\beta} + m\omega_{s})]\overline{Z}g_{m}(r) = \frac{1 + U_{0} - \kappa_{C0}}{4\pi E/e b^{2}}[i]^{m-1} W_{0}(r) \sum_{p=-\infty} \frac{1 + W_{p}}{p} I_{m}(pr)\tilde{f}(p) (13)$$

Here \overline{B}_0 , \overline{x}_{CO} are the maximum values of the amplitude function and the closed orbit deviation in the rf-region.

The impedances \overline{Z}_{111}^{\pm} are defined by

$$\overline{Z}_{1"}^{\pm} = \sum_{\substack{g=1 \\ g=1}}^{N} Z_{1"g} e^{\pm \Delta(S_g)} \sqrt{\frac{\beta_g}{\beta_o}} \frac{x_{cog}}{\overline{x}_{co}}$$
(14)

The index l runs over the positions of localized objects (rf-section) with impedance $Z_{1||l_{\ell}}$, amplitude function β_{ℓ} and closed orbit deviation x_{col}

The function $\Delta(s)$ is given by

$$\Delta(s) = \Omega \tau(s) - \omega t(s) \tag{15}$$

In the sense of the approximations applied this should be replaced by

$$\Delta(s) = \varphi_{r}(s) \tag{16}$$

where $\phi_{\mathbf{r}}(s)$ is the phase advance corresponding to the integer part of the Q-value.

For the derivation of (12), (13), (14) compare for instance ref. 2 or ref. 3. Writing

$$\lambda_{n} = \omega - n\omega_{s}$$
(17)
$$\lambda_{m} = \Omega - (\omega_{\beta} + m\omega_{s})$$
(18)

and making use of

$$\tilde{f}(p) = 2\pi \sum_{n=-\infty}^{+\infty} [-i]^n \int dr'r' f_n(r') I_n(pr')$$
(19)

$$\widetilde{g}(p) = 2\pi \sum_{n=-\infty}^{+\infty} [-i]^m \int dr'r' g_n(r') I_n(pr')$$
(20)

we obtain from equs. (12) and (13)

$$\lambda_{n}f_{n} = 4\pi n I \frac{\overline{Z} \overline{x}_{CO} \sqrt{\beta_{O}} \omega_{S}}{b^{2} h \overline{U}_{C}} \frac{1}{r} \frac{\partial}{\partial r} W_{O}(r) \sum_{p} \frac{\overline{Z}_{1}}{p} I_{n}(pr) \sum_{n} [i]^{n-m-1} \int_{O}^{\infty} dr'r' I_{m}(pr')g_{m}(r')$$
(21a)

$$\lambda_{m}f_{m} = \frac{I\sqrt{\beta_{0}}}{2E/e z b^{2}} W_{0}(r) \sum_{p} \frac{\overline{Z}_{1n}^{+}}{p} I_{m}(pr) \sum_{m} [i]^{m-n-1} \int_{0}^{\infty} dr'r' I_{n}(pr')f_{n}(r')$$
(21b)

Besides the functions $f_n(r)$, $g_n(r)$ we introduce the adjoint ones

$$f_{n}(r) = -f_{n}^{+} \frac{1}{r} \frac{\partial}{\partial r} W_{0}(r) \qquad (22a)$$

$$g_{n}(r) = g_{m}^{+}(r) W_{0}(r) \qquad (22b)$$
with $2\pi \int_{0}^{\infty} dr r W_{0}(r) = 1 \qquad (22c)$

The scalar product of a pair f, f' resp. g, g' is then defined as

$$(f,f') = \int_{0}^{\infty} drr f^{+*} f$$
 (23a)
 $(g,g') = \int_{0}^{\infty} drr g^{+*} g$ (23b)

According to (22), (23) we put

$$f_{n}(r) = A_{n} \ell_{n}(r)$$
(24a)

$$g_{m}(r) = B_{m} L_{m}(r)$$
.
with $(\ell_{m}, \ell_{m}) = (L_{m}, L_{m}) = 1$ (24b)

for all m.

Finally we introduce

$$k_{n}(p) = \sqrt{2\pi} \int_{0}^{\infty} dr r \ell_{n}(r) I_{n}(pr) \quad (25a)$$

$$k_{m}(p) = \sqrt{2\pi} \int_{0}^{\infty} dr r L_{m}(r) I_{m}(pr) \quad (25b)$$

Multiplying equ. (21a) with f_n^+ , equ. (21b) with L_m^+ and using (25) we find

$$\lambda_{n} A_{n} = \frac{2n \, I \, \overline{z} \sqrt{\overline{B}_{0}} \, \overline{x}_{C0} \, \omega_{S}}{b^{2} \, h \, \overline{U}_{C}} \sum_{m} [i]^{n-m-1} \sum_{p} \frac{\overline{Z}_{1u}^{+}(p)}{p} \, k_{n}^{*}(p) \, k_{m}(p) \, B_{m} \quad (26a)$$

$$\lambda_{m}B_{m} = \frac{I\sqrt{\overline{B}_{0}}\,\overline{x}_{co}\,c}{4\pi\,E/e\,\overline{z}\,b^{2}} \sum_{n} [i]^{m-n-1} \sum_{p} \frac{\overline{Z}^{+}(p)}{p} k_{m}^{\star}(p) k_{n}(p) A_{n} \qquad (26b)$$

Since the functions h(p), k(p), as a function of p, have the same parity properties, the system (26) has similar properties as in the case of transverse mode coupling. Concentrating on the coupling of longitudinal and transverse modes only, one obtains from (26)

`

with
$$\Delta = \delta \omega_{\beta} + (m - n) \omega_{s}$$
, (28)

 $\delta\omega_\beta$ is the circular betatron frequency corresponding to the fractional part of the Q-value.

We introduce the abbreviation

$$|M|^{2} = \frac{n I^{2} \overline{x}_{C0}^{2} \overline{B}_{0} \omega_{S} c}{2\pi E/e b^{4} h \overline{U}_{c}} |D^{-}|^{2}$$
(29)

An instability occurs if

$$n < 0$$

$$|m| - |n| \quad odd \qquad (30)$$

$$|M| > [\frac{\Delta}{2}]$$

From (14) follows

$$O_{nm}^{\pm} = \sum_{\ell=1}^{N} D_{\ell nm} e^{\pm i \Delta(s_{\ell})} \frac{x_{co\ell}}{\overline{x}_{co}} \sqrt{\frac{\beta_{\ell}}{\overline{\beta}_{o}}}$$
(31a)

with
$$D_{\ell nm} = \sum_{p} \frac{Z_{1u\ell}}{p} h_n^{\star}(p) k_m(p)$$
 (31b)

From the parity properties of h, k as functions of p follows

$$D_{lnm} = 2 \sum_{p=0}^{\infty} R_{l} Z_{1n}(p) \frac{h_{n}^{*}(p) k_{m}(p)}{p}$$
 (32)

المتعادين والمستعد ومراري المراسي المنا

At this point we must introduce the normalized functions $\ell(r)$, L(r) solving (12), (13). As an "approximate" solution we put

$$L_{m}(\mathbf{r}) = \left(\frac{m}{|\mathbf{m}|}\right)^{|\mathbf{m}|} \frac{\sqrt{2}}{\sqrt{\pi}\sqrt{|\mathbf{m}|!}} \frac{1}{\sigma^{2}} \left(\frac{\mathbf{r}}{\sigma}\right)^{|\mathbf{m}|} e^{-\mathbf{r}/\sigma^{2}}$$
(33)
with
$$\sigma = \frac{\sigma_{s}}{R}/\sqrt{2}$$
(34)

σ_s ≜ r.m.s. bunch length

R ≘ machine radius

Similarly we put

$$\ell_{\rm m}(r) = \sqrt{2}' \, \frac{L_{\rm m}(r)}{\sigma} \tag{35}$$

and obtain

$$\kappa_{m}(p) = \frac{1}{\sqrt{2^{m}}\sqrt{|m|!}} \left(p \frac{\sigma_{s}}{R}\right)^{|m|} e^{-p^{2} \left(\frac{\sigma_{s}}{R}\right)^{2}}$$
 (36a)

and

$$h_n(p) = \sqrt{2^n} \frac{k_n(p)}{\sigma}$$
(36b)

with

$$\operatorname{Re} Z_{1 \parallel \ell} = R_{1 \parallel \ell}$$
(37)

and $R_{eff \ell} = 2 \Sigma R_{1 \mu \ell} e^{-p^2 (\frac{\sigma_s}{R})^2}$

We can express D by differentiating R_{effl} $(\frac{\sigma_s}{R})$ with respect to $(\frac{\sigma_s}{R})^2$.

Going back to (27) we find lower thresholds if \triangle is small. Putting n = -|n| according to (30) and specializing m = -|m| one obtains from (28)

(38)

$$\Delta = \delta \omega_{\beta} - (|m| - |n|) \omega_{s}$$
(39)

which becomes small for |m|>|n| if $\,\delta\,\omega_{\beta}$ is near a satellite frequency

$$\delta \omega_{\beta SAt} = (|m| - |n|) \omega_{s} \qquad (40)$$

Since an instability occurs only if |m| - |n| is odd (see 30) a blow-up occurs only near odd satellite frequencies. Table I shows the relation between modes and satellite frequencies

- 9 -

transverse m	longitudinal n	satellite frequency	
- 2	- 1	ω _s	
- 4	- 1	3 ω _s	
- 3	- 2	ως	
- 5	- 2	3 ω _ς	



In order to make use of the differentiating process mentioned above we put

$$v = ([m] + |n| - 1)/2$$
(41)

We find from (32) and (36)

$$D_{lnm} = \frac{1}{\frac{\sigma_s}{R}} \frac{\sqrt{2}}{\sqrt{2} |m| \sqrt{2} |n| \sqrt{|m|!} \sqrt{|m|!}} \left(\frac{\sigma_s}{R}\right)^{|n| + |m|} (-1)^{v} \frac{d^{v}}{d \left[\left(\frac{\sigma_s}{R}\right)^2 \right]^{v}} R_{effl}$$
(42)

If in a limited range we assume a "power law" for $R_{\text{eff}~\text{L}}$ as a function of σ_{S}

$$R_{effl} = R_{effl} \left(\frac{\sigma_{S}}{\sigma_{S0}} \right)^{-2\mu} , \quad \mu > 0$$
(43)

we obtain

$$(-1)^{V} \frac{d^{V}}{d\left[\left(\frac{s}{R}\right)^{2}\right]^{V}} = \mu(\mu+1) \dots (\mu+\nu-1) \frac{\sigma_{s}}{R}^{-2V} R_{effl}$$
(44)

and therefore

$$D_{gnm} = \frac{\sqrt{2^{2}} \mu(\mu+1) \dots (\mu+\nu-1)}{\sqrt{2^{2}} (|m|+|n|)} R_{effg}$$
(45)

- 8 -

Relation (29) can then be rewritten as

$$M| = \kappa \frac{I \overline{R}_{eff}}{\sqrt{E/eh \overline{U}_{c}}} \frac{|\overline{x}_{co}|}{b} \sqrt{\frac{\overline{\beta}_{o}}{b}} \sqrt{\omega_{s} \cdot \omega_{b}} \cdot \Sigma$$
(46a)

with

$$\omega_{\rm b} = \frac{\rm c}{\rm b} \cdot 2\pi \tag{46b}$$

$$\kappa = \frac{1}{2\pi} \frac{\sqrt{2 |n|^{\prime} |\mu(\mu+1)...(\mu+\nu-1)}}{\sqrt{2^{\prime} (|m|+|n|) \sqrt{|m|!} \sqrt{|n|!}}}$$
(46c)

 \overline{R}_{eff} is the impedance of the whole structure. The quantity Σ is given by

$$\Sigma = \left\{ \sum_{\substack{g=1}}^{N} \left(\frac{\text{Reff}\,g}{\text{Reff}} \frac{x_{\text{co}}}{\overline{x}_{\text{co}}} \sqrt{\frac{\beta_g}{\beta_0}} \cos \Delta(s_g) \right)^2 + \left(\frac{\text{Reff}\,g}{\overline{R}_{\text{eff}}} \frac{x_{\text{co}}}{\overline{x}_{\text{co}}} \sqrt{\frac{\beta_g}{\beta_0}} \sin \Delta(s_g) \right)^2 \right\}^{1/2}$$
(46c)

Numerical estimates

We apply the maximum value of Σ , i.e. $\Sigma = 1$ for PETRA and choose the following machine parameters:

E = 7 GeV	h = 3840
I ≃ 5 mA	U _c = 25 MV
\overline{x}_{CO} = 2.5 mm	n = -1
$\overline{\beta}_0 = 20 \text{ m}$	m = -2
b = 4 cm	$2\mu = 1.5$
$\omega_{s} = 50 \text{ kHz}$	$\frac{R_{eff}}{b^2} = 1.3 \cdot 10^8 \Omega/cm^2 \text{for 56} 5\text{-cell and} \\ 56 7\text{-cell cavities}^{15})$

This yields

near the first order satellite resonance.

For HERA the effect only appears above the operational bunch intensities if one assumes a distance Δ = 2 kHz.

Experimental results

A "coherent" satellite resonance can be distinguished easily from an incoherent ("normal") satellite resonance if the transverse motion is dominated by a dipole oscillation. An identification of a higher head-tail mode is rather hard.

For the instabilities treated in this article the higher head-tail modes are accompanied by collective longitudinal oscillations. Especially in the case considered numerically the instability leads to longitudinal dipole oscillations which can be easily detected.

In PETRA longitudinal dipole oscillations or longitudinal shape oscillations in coincidence with a transverse blow-up near odd satellite resonances have not been observed.

The reason for this may be that Σ is much smaller than 1 due to the symmetry of the machine and the symmetric locations of the rf cavities.

References

- R.D. Kohaupt, Proc. 11th Internat. Conf., CERN (1980), p. 562
 R.D. Kohaupt, DESY M-80-22, Hamburg (1980)
 R.D. Kohaupt, Habilitationsschrift, Univ. Hamburg, Hamburg (1982)
 T. Susuki, Particle ACC. 1982, Vol. 12, pp. 237-246
 A. Chao, SLAC-PUB-2946, SLAC (1982)
 PEP Group, Proc. 12th Internat. Conf., FERMILAB (1983), p. 209
 K. Saloh, Y. Chin, Nucl. Instr. Methods 207 (1983), p. 309
 D. Brandt, B. Zotter, CERN-LEP-TH/84-2 (1984)
 A. Piwinski, Proc. Internat. Conf., CERN (1980), p. 638
 F. Ruggiero, CERN-LEP-TH/84-21 (1984)
 Y.H. Chin, SPS/85-33 (DI-MST) (1985)
- 12) F. Sacherer, CERN/SI-BR/72-5
- 13) T. Weiland, Nucl. Instr. Methods 216 (1983), pp. 31-34
- 14) R.D. Kohaupt, DESY 85-059 (1985)
- T. Weiland, private communication