## <span id="page-0-0"></span>**INCLUSIVE DIRECT CP-ASYMMETRIES IN CHARMLESS B±-DECAYS<sup>a</sup>**

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Direct CP-asymmetries in inclusive decay modes can be cleanly calculated by exploiting quark-hadron duality. This is in sharp contrast to CP-asymmetries in exclusive channels, where unknown strong phases prevent a clean extraction of CKM parameters from measured CP-asymmetries. We have calculated the inclusive CP-asymmetries in  $B^{\pm}$ -decays into charmless final states with strangeness one or strangeness zero. In our results large logarithms are properly summed to all orders. We find

> $\sim$  0)  $\sim$   $2.0^{+1.0}_{-1.0}$  $a_{CP} (\Delta S = 1) = (-1.0 \pm 0.5) \%$ .

The constraints on the apex  $(\bar{\rho}, \bar{\eta})$  of the unitarity triangle obtained from these two CP-asymmetries define circles in the  $(\overline{\rho}, \overline{\eta})$ -plane.  $a_{CP} (\Delta S = 0)$  measures  $\sin \gamma \cdot |V_{cb}/V_{ub}|$ . The presented work has been done in collaboration with Gaby Ostermaier and Alexander Lenz.

First we define the average branching fraction in terms of the decay rate  $\Gamma$ :

 $\sim$ 

 $\overline{\phantom{a}}$ 

$$
\overline{Br} = \frac{\Gamma(B^+ \to X) + \Gamma(B^- \to \overline{X})}{2\Gamma_{tot}}.
$$
 (1)

 $\sim$ 

In the following we are interested in inclusive final states  $X$  containing no charmed particle. Further the total strangeness S of X must be known, we will consider the cases  $X = X(S = 0)$  and  $X =$  $X(|S| = 1)$ . Similarly we define the direct CP-asymmetries as

$$
A_{CP} = \frac{1}{2} \left[ Br \left( B^+ \to X \right) - Br \left( B^- \to \overline{X} \right) \right], \qquad a_{CP} = \frac{A_{CP}}{\overline{Br}}. \tag{2}
$$

The measurement of  $\overline{Br}$  in (1) and of the CP-asymmetries in (2) requires a sum over semi-inclusive final states in which the Kaons and strange baryons must be identified. Direct CP-asymmetries in exclusive decay modes are hard to access theoretically. Non-perturbative rescattering effects induce strong phases, which are difficult to estimate. On the contrary for the case of inclusive final states local quark-hadron duality allows to calculate the quantities in (1) and (2) reliably [wi](#page-1-0)thin perturbation theory. Theorist have been considering inclusive direct CP-asymmetries since 1979<sup>1</sup>. Up to now the inclusive  $a_{CP}$ 's were



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Figure 1: The lightly (darkly) shaded area shows the constraint on  $(\bar{\rho}, \bar{\eta})$  stemming from  $a_{CP}$  ( $\Delta S = 0$ ) ( $a_{CP}$  ( $\Delta S = 1$ )), if the  $a_{CP}$ 's are measured as in (3).

believed to be small, of the order of a few permille. Yet in the predictions of  $1$  either large logarithms have not been summed to all orders or  $m_t$  was taken too small. This has been corrected for in our new paper<sup>2</sup>, in which also the predictions for charmless branching ratios calculated before <sup>3</sup> have been improved by incorporating new QCD corrections. We find

$$
a_{CP} (\Delta S = 0) = \left( 2.0^{+1.2}_{-1.0} \right) \% , \qquad a_{CP} (\Delta S = 1) = (-1.0 \pm 0.5) \% .
$$

Here the error bars stem from the uncertainty in  $m_c/m_b$  and  $\bar{\rho}, \bar{\eta}$  and from the residual dependence on the renormalization scale  $\mu$ . The  $\mu$ -dependence can be reduced by calculating certain two-loop diagrams. This is possible with reasonable effort and will be done, once the inclusive direct CP-asymmetries receive experimental interest.

The dependence of the  $a_{CP}$ 's on  $\overline{\rho}$  and  $\overline{\eta}$  is welcome in order to constrain the apex of the unitarity triangle. For a model scenario with

$$
a_{CP} (\Delta S = 0) = 2.0\%, \qquad a_{CP} (\Delta S = 1) = -1.0\% \tag{3}
$$

and an assumed total error of 20 % the constraints on  $\bar{p}$ ,  $\bar{\eta}$  are shown in figure 1. They are nice circles in the  $\overline{\rho}$ ,  $\overline{\eta}$ -plane, whose information is complementary to the familiar circle from  $B$ - $\overline{B}$ -mixing and the hyperbola from  $\varepsilon_K^4$ . The  $A_{CP}$ 's defined in [\(2](#page-0-0)) are simply proportional to  $\overline{\eta}$ .

## **References**

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