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THE FINAL STATES & K TK TX IN JETS AS SIGNATURES OF BE-BE MIXINGS

by

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The Final States $\ell^{\widetilde{T}}K^{\overset{L}{T}}K^{\overset{L}{T}}X$ in Jets as Signatures of $B_S^{\bullet}-\widetilde{B}_S^{\bullet}$ Mixings

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Abstract

Significant mixing is expected between the neutral bottom mesons $B_S^0 - \overline{B}_S^0$ in the standard model of weak interactions. We propose measurements of the processes $\left\{e^+e^-\right\} \longrightarrow b\bar{b} \longrightarrow \mbox{k^+K^-K^-X} + \mbox{c.c.}$ as a measure of such mixing. Rates are presented for energetic bottom quark jets, produced in e^+e^- annihilation.

Introduction

A non-trivial test of the standard model of electroweeak interactions lies in measuring the strength of the flavour changing $|\Delta F| = 2$, $\Delta Q = 0$ transitions among the neutral meson systems $K^0 - \bar{K}^0$, $D^0 - \bar{D}^0$, $8^0 - \bar{B}^0$ and $8^0 - \bar{8}^0_s$. Experimentally, such transitions have so far been observed in the $K^0 - \bar{K}^0$ sector only, though there exists some preliminary evidence from the CERN $\bar{p}p$ data that such mixings may also be present among the neutral bottom mesons. 1)

The presence of the $|\Delta B|=2$, $|\Delta Q|=0$ transition involving the neutral bottom mesons have a number of interesting phenomenological consequences, two of which have received experimental attention. The first concerns the production of energetic same-sign dileptons in the processes $e^+e^- \rightarrow b\bar{b} \rightarrow e^+ e^+ \chi^2$, and $\bar{p}p \rightarrow b\bar{b} \rightarrow e^+ e^+ \chi^2$. The second method involves the measurement of the electroweak charge asymmetry in the process $e^+e^- \rightarrow b\bar{b} \rightarrow e^+ \chi^4$, since the $|\Delta B|=2$ interactions lead to the "wrong-sign" lepton and hence tend to decrease the electroweak asymmetry. However, none of these measurements by themselves would distinguish between the mixings in the $B_d^0 - \bar{B}_d^0$ and $B_s^0 - \bar{B}_s^0$ mesons, since either of the two transitions would lead to the $e^+ e^+ \chi^2 - \chi^2 + \chi^2$

In the standard model one expects significant $B_s^0 - \bar{B}_s^0$ mixing and negligible $B_d^0 - \bar{B}_d^0$ mixing. 5) In a number of non-standard scenarios, however, there

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exist additional effective interactions which may enhance the $\mathbf{B_d} \cdot \overline{\mathbf{B_d}}$ mixing amplitude. For example, in the supersymmetric extension of the standard model additional mechanisms which enhance the $\mathbf{B}_d - \overline{\mathbf{B}}_d$ mixings have been recently emphasized. 6) It is therefore imperative to be able to distinguish experimentally between the $\rm B_d^{-\overline B}_d$ and $\rm B_s^{-\overline B}_s$ mixings. In principle, some of these tests have already been proposed 7) which consist of measuring the final states ltt. and ltt. in the fragmentation products of bottom quark jets initiated by the hard collisions $(e^+e^-, p\bar{p}) \rightarrow b\bar{b}X$. Another test, which suggests itself naturally lies in scanning the region at and above the 4S resonance in the final state $e^+e^- \rightarrow l^{\pm}l^{\pm}X$. In gractice, the former tests would require a very high bottom hadron statistics, which may or may not be available in the near future. Theoretical interpretation of the signal in $e^+e^- \rightarrow \frac{1}{2} \frac{1}{2} \times X$ in the region $\Upsilon(n5), n>4$, is a potential-model dependent enterprise, since the branching ratios for $\Im(NS) \rightarrow B_S \overline{B}_S$, $B_S \overline{B}_S$, $B_S \overline{B}_S$ etc. are needed, which can at best be modelled. In any case there is no signal yet from the CESR/DORIS data of either $\mathbf{B_d}^-\overline{\mathbf{B_d}}$ or $\mathbf{B_s}^-\overline{\mathbf{B_s}}$ mixings. Model dependent calculations $^{8)}$ estimate that a signal is expected at * (5S) but would require an integrated luminosity of 1000 pb^{-1} . There is no evidence of B-B mixing from the PETRA/PEP data either 3),4), nor it is expected with the present luminosity 9).

The aim of this paper is to devise a new test of B-B mixing which i) is experimentally measurable, ii) is less dependent on the production cross-section $\mathbf{G}(B_s^0 X)$ and the semileptonic branching ratio $\mathrm{BR}(B_s^0 \to \ell^{\frac{1}{\lambda}} X)$ of the B_s^0 meson and iii) could distinguish between mixings in the $B_d^0 - \overline{B}_d^0$ and $B_s^0 - \overline{B}_s^0$ mesons.

2. Proposal

We propose measurements of the final states $t^{\frac{1}{2}} K^{\frac{1}{4}} K^{\frac{1}{4}} X$ in the bottom quark jets produced, for example, in the processes

$$\begin{cases}
e^{+e^{-}} \\
\bar{p}p
\end{cases} \longrightarrow b\bar{b} \qquad l^{+} K^{-} K^{-} X + c.c.$$
(1)

as a measure of weak mass mixing in the 8_s - \overline{B}_s^{\bullet} mesons. The test implicitly assumes that the decay products of b and \overline{b} do not contaminate each other, in other words that the b and \overline{b} hadrons are well separated spatially; a criterion well satisfied by jets at PEP and PETRA and in $p\overline{p}$ collisions.

The main idea behind the "decay" of an excited b-quark, b— ℓ^+ K K X, as a measure of $B_s^- \overline{B}_s$ mixing is rather simple. The decay of a b-quark produced in a hard collision follows a certain fragmentation weak decay chain, the general features of which are now well known experimentally 10). Thus, concentrating on the semileptonic decays of the bottom hadrons and the final states containing charged kaons, K^{\dagger} , one schematically has

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where only the Cabibbo-allowed decays of the D^o, D⁺ and F⁺ mesons are shown. Since D^o, D⁺ $\xrightarrow{}$ K⁺X decays are Cabibbo forbidden but F⁺ $\xrightarrow{}$ K⁺X are Cabibbo allowed, a good two-particle inclusive final state to enhance the B^o_S(\overline{B}_S^o)

signal should be in the decays $B \to \overline{L} \ K^{\dagger} X$, $\overline{B} \to \overline{L} \ K^{\dagger} X$. Next, we remark that all experimental measurements of particle production in jets give a suppression in the production of $s\overline{s}$ pair from the vacuum $\overline{}^{11}$. In fact the world data is in agreement with the probability, $f(s\overline{s}) = 0.1$ - 0.15 in quark jets. Hence it makes sense to use $f(s\overline{s})$ as an order parameter. To leading order in $f(s\overline{s})$ one would have the fragmentation $b \to (B_d^0, B_u^0)K^{\dagger}X$ and $\overline{b} \to \overline{B}_s^0K^TX$. Thus, in the approximation of keeping $\sin^2 \mathfrak{D}_c = 0$ and leading K^{\dagger} mesons from the associated jet accompanying the bottom hadron, the "decay" of the bottom quark jets

$$(b \text{ or } \overline{b}) \longrightarrow \underline{V}^{\overline{Y}} K^{\pm} K^{\pm} X \tag{4}$$

is forbidden! The situation is quite different in the presence of $B_s - \overline{B}_s$ mixing. In that case, to leading order in $f(s\overline{s})$ one would have $b \rightarrow B_s K^T X$, $\overline{B}_s^0 K^T X$ in the ratio $(1 - \gamma_s)$ and γ_s where γ_s is the probability of the transition $B_s \rightarrow \overline{B}_s^0$. This would lead to the decays

$$(\overline{b}s) \longrightarrow f \ell^{\dagger} \partial_{\ell}, \cdots \qquad (5)$$

giving rise to the final states $b \longrightarrow K K X$ and $b \longrightarrow K K X$ which are both Cabibbo allowed and favoured by the fragmentation process $s \longrightarrow K X$. It is easy to see that in the same approximation $B_a^{\bullet} - \overline{B}_d^{\bullet}$ mixing would lead to the final states (b or \overline{b}) $\longrightarrow K K X$. Thus, in the limit stated above observation of (b or \overline{b}) $\longrightarrow K K X$ in a bottom quark jet would signal $B_s^{\bullet} - \overline{B}_s^{\bullet}$ mixings.

To quantify our proposal, we define the following ratio

$$R(l^{\dagger}\bar{K}\bar{K}) = \frac{b \rightarrow l^{\dagger}\bar{K}\bar{K}X}{b \rightarrow l^{\dagger}\bar{K}\bar{K}X}$$
(6)

Then, quite generally for collisions leading to $b\bar{b}$ production one can express the ratio R as

$$R(\frac{1}{1}\overline{\kappa}\overline{\kappa}\overline{\kappa}\overline{\kappa}) = \frac{\sum_{q} 6(\frac{1}{2})\left\{8R(\frac{1}{2}+\frac{1}{1}\overline{\kappa}x)f(q+\overline{\kappa}x)+8R(\frac{1}{2}+\frac{1}{1}\overline{\kappa}x)f(q+\overline{\kappa}\overline{\kappa}x)\right\}}{\sum_{q} 6(\frac{1}{2})\left\{8R(\frac{1}{2}+\frac{1}{1}\overline{\kappa}x)f(q+\overline{\kappa}x)+8R(\frac{1}{2}+\frac{1}{1}\overline{\kappa}x)f(q+\overline{\kappa}\overline{\kappa}x)\right\}}$$
(7)

where the sum \sum_{q} is over all species of the bottom hadrons Bq and $f(q \rightarrow K^+ X)$ etc. represents the probability of a quark giving a K^+ . In principle, one could additionally have the decays Bq $\rightarrow k^+ K^- K^- X$, due to, for example, $B_S \rightarrow k^+ F_S K^- K^- K^-$, but being suppressed by phase space and $\sin^2 \theta_S$, they must have negligible branching ratios ($\leq 10^{-3}$).

Now, in the limit $\sin^2\theta_{\epsilon}^2=0$ and leading order in f(ss) (keeping only the valence K hadron from the fragmentation process $q \to K^{\pm}X$), we have

$$\mathcal{R}(\mathbf{i}^{\dagger}\mathbf{k}\cdot\mathbf{k}^{\prime}/\mathbf{i}\cdot\mathbf{k}\cdot\mathbf{k}) \approx \frac{\mathcal{C}(\mathcal{B}_{s}^{s})\mathcal{B}\mathcal{R}(\mathcal{B}_{s}^{s}\rightarrow\mathbf{i}^{\dagger}\mathbf{k}\cdot\mathbf{x})\mathcal{L}(\mathbf{s}\rightarrow\mathbf{k}\cdot\mathbf{x})}{\mathcal{C}(\mathcal{B}_{s}^{s})\mathcal{B}\mathcal{R}(\mathcal{B}_{s}^{s}\rightarrow\mathbf{i}^{\dagger}\mathbf{k}\cdot\mathbf{x})\mathcal{L}(\mathbf{s}\rightarrow\mathbf{k}\cdot\mathbf{x})}$$
(8)

$$= \frac{BR(B_s^0 + 1 \overline{k} X)}{BR(B_s^0 + 1 \overline{k} X)} = \frac{\chi_s}{1 \cdot \chi_s} \frac{BR(\overline{r} + \overline{k} X)}{BR(\overline{r}^0 + \overline{k} X)}$$
(9)

where $\chi_s \equiv I'(B_s' + I^* \mathfrak{d}_{L} X) / I'(B_s' + I^* \mathfrak{d}_{L} X)$ is the measure of $B_s'' - B_s''$ mixing. Thus, in the limit that Eq. (8) holds, the quantity R(I'' + K' / I' + K'') is independent of the B_s'' -production cross-section $G(B_s'' X)$, the probability $f(s \to K'' X)$ and the semileptonic branching ratio for the B_s'' meson. It depends, however, on the inclusive branching ratio of the F'' mesons, namely $F' \to K'' X$. The quantity $BR(F' \to K'' X)/BR(F' \to K'' X)$ in eq. (9) is expected to be around 1 in the quark-parton model description

of the $F^{\frac{1}{2}}$ decays, and hopefully should be available soon experimentally.

In the rest of this paper, we present a calculation to estimate the signal and background for the final state $b \rightarrow \ell^+ K^- K^- X$ for realistic experimental conditions in $e^+ e^-$ annihilatoion at PETRA/PEP and LEP/SLC energies.

3. Rate Estimates

$$f(z_0) = \frac{z_0 (1 - z_0)^2}{\left[z_0 (1 - z_0) - (1 - z_0) - \varepsilon_0 z_0\right]^2}$$
(9)

where $\Xi_{\mathcal{B}} = \frac{\Xi_{\mathcal{B}}}{\Xi_{\mathcal{b}}} = \frac{2\Xi_{\mathcal{B}}}{\sqrt{3}}$ and $\Xi_{\mathcal{B}} = 0.02$, compatible with the measurements in e^+e^- experiments. The momentum distribution of the K mesons in the process

$$z^{\dagger}z^{-} \longrightarrow b\overline{b}$$
 $(b\overline{q}) + q \qquad k^{\pm}X$ (10)

is then considerably soft, as can be seen in figs. (1), where we have plotted the fragmentation functions $D(Z=2E_K/\sqrt{s})$ for $q \to K^{\dagger}X$, q=u,d,s with the normalization $\int_0^1 D(Z) dz = f(q \to K^{\dagger}X)$. Fig. (1a) shows the D(Z) distributions for a typical PETRA energy $\sqrt{s}=43$ GeV and should be representative of the high energy data from PETRA and PEP collected at $\sqrt{s}=29-46$ GeV. Fig. (1b) shows the same distributions at $\sqrt{s}=m_Z \approx 93$ GeV, relevant for the LEP and SLC experiments. Since the general features of the quark jets observed at PETRA and PEP are remarkably well described by the fragmentation models $\frac{14}{s}$ of the type we are discussing, we expect that the distribution functions D(Z) shown in figs. (1) should be rather close to the experimental distributions, though we are aware that an analysis of the bottom quark jets as depicted in figs. (1) has not yet been undertaken.

The flavour distributions D(Z) shown in figs. (1) are quite instructive. They give a concrete meaning to the concept of allowed (valence) and suppressed (sea) $q \rightarrow K^{\pm}X$ fragmentation transitions. For example, for an s-quark accompanying a Bs meson in a jet, the ratio $\sum_{k=1}^{\infty} \frac{\sum_{k=1}^{\infty} x_{k}}{\sum_{k=1}^{\infty} x_{k}}$ has the value: $\sum_{k=1}^{\infty} \frac{x_{k}}{x_{k}} > 0.1$ and this ratio becomes >20 for Z>0.3. Thus, the ability to detect energetic K^{\pm} mesons

is at a premium! This is all that one needs to show that $\mathbf{5}(B_S^{\bullet}K^{\dagger}X)/\mathbf{5}(B_S^{\bullet}K^{\top}X) <<1 \text{ for realistic fragmentation functions in the absence of } B_S^{\bullet}-\overline{B}_S^{\bullet} \text{ mixing.}$

Our next task is to calculate the inclusive bottom hadron cross-section ${\bf 6}(B_qX)$ in continuum e^+e^- and $\overline{p}p$ collisions. We argue that it is very plausible to assume that given the inclusive bottom quark cross-section, ${\bf 6}(bX)$, the inclusive cross-section for producing a bottom hadron ${\bf 6}(BqX)$ is determined essentially by the probability of producing a quark-antiquark or diquark pair from the vacuum $f(q\overline{q})$, f(qq). These probabilities have been well measured in the light-quark fragmentation processes ${\bf 11}$). We argue that the functions $f(q\overline{q})$, f(qq) are approximately independent of the flavour of the decaying quark. This assumption is implicit in most fragmentation models in vogue ${\bf 14}$ 0 and appears rather plausible. However, it has not yet been directly tested. We remark that measurements of the cross-section ratio ${\bf 6}(F^+X)/{\bf 6}(D^{0,+X}X)$ would be very welcome to determine $f(s\overline{s})$ for the charm quark jets. With this assumption we have

$$\mathcal{E}(\mathcal{B}_{q} \times) = \mathcal{E}(\mathcal{b}^{X}) \mathcal{F}(q\bar{q})$$

$$\mathcal{E}(\Lambda_{g} \times) = \mathcal{E}(\mathcal{b}^{X}) \mathcal{F}(qq)$$
(11)

where 5(bX) is obtained from perturbative QCD. For example,

$$\frac{G(e^{\dagger}e^{-} \rightarrow b \times)}{G(e^{\dagger}e^{-} \rightarrow \mu^{\dagger}\mu^{-})} = \frac{1}{3}\left(1 + \frac{\varphi_{S}(\varphi^{2})}{\pi}\right)$$

It is well known that exact $\mathcal{D}(\alpha_s^2)$ contributions $^{15)}$, as well as all order contributions in leading log $^{16)}$ to \mathbf{G} (e⁺e⁻ \rightarrow bx) are entirely negligible upto and including LEP energies. This means that the multiplicity of the bottom hadron in a jet is at most 1. $^{16)}$

In fig. (2a) we show the differential cross-section $\frac{A}{G(bb)} = \frac{A}{dz} (e^+e^-bk^-x)$ for the final states $e^+e^- \to B_U^{-K}X$, $B_d^+K^-X$ and $B_s^+K^-X$ for $\sqrt{s} = 43$ GeV, assuming $f(s\bar{s}) = 0.15$. Similar cross-sections are shown for $\sqrt{s} = m_Z = 93$ GeV in fig. (2b). The hierarchy in the cross-sections is very striking, with $G(B_s^0K^-X) \simeq G(B_U^0K^+X)$ being the largest and $G(B_s^0K^+X)$ the smallest cross-section. For the particular choice of $f(s\bar{s})$, we note that $G(B_s^0K^-X)/G(B_s^0K^+X) \simeq 5$ for $Z = 2E_K/\sqrt{s} \geqslant 0.1$ and this ratio becomes $\geqslant 10$ for $Z \geqslant 0.2$. In the presence of $B_s^0 - B_s^0$ mixing, no change is really expected in the cross-sections for $e^+e^- \to B_U^0K^-X$, $B_d^0K^-X$ but the cross-sections $G(B_s^0K^-X)$ and $G(B_s^0K^+X)$ are expected to change. They would tend to each other and become identical for complete $B_s^0 - B_s^0$ mixing, in which case

$$\frac{d6}{dz} \left(e^{+}e^{-} \rightarrow B_{s}^{o} K^{X} \right) = \frac{d6}{dz} \left(e^{+}e^{-} \rightarrow B_{s}^{o} K^{X} \right)$$

for all values of Z. This is an effect hard to miss for detectors having a good B_S^{\bullet} and K^- identification!

How does one tag on the B $_{\rm S}$ meson in a bottom quark jet produced for example at PETRA/PEP and LEP/SLC energies? There might be more favourable decay modes discovered in the course of time, but as of now we recall from the discussion above that the decays $B \rightarrow l^- K^+ X$ are expected to provide a $B_{\rm S}^{\bullet}$ -

enriched sample. To that end we need the branching ratios for the decays $B_{U}^{-} \to \ell^{-}K^{-}X$, $B_{d}^{\sigma} \to \ell^{-}K^{-}X$ and $B_{s}^{\sigma} \to \ell^{-}K^{-}X$, none of which are presently available. We make the assumption based on the quark-parton model that the semileptonic branching ratios for all three bottom mesons are close to each other, $BR(B_{U}^{-} \to \ell^{-}X) \simeq BR(B_{d}^{\sigma} \to \ell^{-}X) \simeq BR(B_{s}^{\sigma} \to \ell^{-}X) \qquad (12)$ Then, since the transition $b \to c$ completely dominates over the transition $b \to c$, and the two-body leptonic decays of the bottom mesons are also negligible, the X in Eq. (12) essentially consists of $(D^{0}, D^{+}) + \ldots$ and $F^{+}+\ldots$ for the B_{U}^{-}, B_{d}^{-} and B_{s}^{σ} semileptonic decays B^{0} . We, therefore need to know the inclusive branching ratios for $D^{0} \to K^{-}X$, $D^{+}+K^{-}X$ and $F^{+}+K^{-}X$.

The experimental situation about D^0 and D^+ decays is quite satisfactory D^0 , with about 80 % of the exclusive D^0 decays and 85 % of the D^+ decays now well measured. Only one of the measured exclusive D^0 decays namely $D^0 \rightarrow K^-K^+$ involves a K^+ with a branching ratio $BR(D^0 \rightarrow K^-K^+) = \{0.6^+ 0.09\}\%$. There are several exclusive modes known for the D^+ decays involving D^+ . Summing over all of them, one gets $D^0 \rightarrow D^+$ decays involving $D^0 \rightarrow D^+$ decays. The experimental situation about $D^0 \rightarrow D^+$ decays is rather unsatisfactory. However, since the dominant decays of the D^+ would involve the decays $D^+ \rightarrow D^+$ (ss) $D^+ \rightarrow D^+$ (ss) (ud), and ss would give $D^0 \rightarrow D^+$ (KK, we expect substantial branching ratios for the decays $D^+ \rightarrow D^+$ (ref. X.). Certainly in this case, no Cabibbo suppression is operative for $D^0 \rightarrow D^+$ and $D^0 \rightarrow D^+$ decays that we have used in our calculations. The two set of values for the $D^0 \rightarrow D^+$ and $D^0 \rightarrow D^+$ decays bracket the expectations in a number of models $D^0 \rightarrow D^+$ and $D^0 \rightarrow D^+$

4. Results

In Table (2) we present our results for the final states $e^+e^- \rightarrow \cline{L} \cline{L} \cline{X}, \cline{L} \ckkxx$

for \sqrt{s} = 43 GeV with all possible charge combinations for \sqrt{t} and \sqrt{t} . The corresponding results for \sqrt{s} = 93 GeV + cuts (ii) are presented in Table (3). The choice of 10^5 bb events in e⁺e⁻ continuum represents a reasonable sample for the kind of effects we are discussing, though for maximum mixing $\chi_s = 0.5$, one may already be able to see a definite trend with 10^4 bb events also.

Concentrating on the results of Table (2), which are representative for the PETRA/PEP energy, we note that the dilepton ratio $l^2 l^2 X / l^4 l^7 X$ rises from 0.21 to 0.38 for $\chi_{\rm s}=0$ to $\chi_{\rm s}=0.5$. The ratio $\Delta(\ell kk)=6(\ell k'k')-6(\ell k'k')$ decreases from 0.37 to 0.14 in the same interval. 8(1xx) +6(1x+x+ With the cut-offs (i), the rates for $\mu^{\pm} k^{\mp} k^{\mp} X$ are higher as compared to $\mu^{\pm}\mu^{\pm}X$ events. At \sqrt{s} = 93 GeV, relevant for LEP/SLC energies and the cut-off (ii) the dilepton ratio $\sqrt[3]{\ell}^{\frac{\pi}{2}} \times \sqrt{\ell^{\frac{\pi}{2}}}$ rises from 0.045($\chi_{\rm s}$ = 0) to 0.175($\chi_{\rm s}$ = 1). In contrast the ratio Δ (\$KK) decreases from 0.41 to 0.23. The rates for the $\mu^{-}K^{+}K^{+}X$ states are now substantially higher than those for the $\mu^{\pm}\mu^{\pm}X$ states. The decrease in the ratio Δ (ξ KK) as a function of χ_{ξ} is a special case of the results shown in figs. (2), where it was shown that the cross-section $8^{\circ}_{c}K^{+}X$ and $8^{\circ}_{c}K^{-}X$ tend to each other with increasing $\chi_{\mathfrak{s}}$. As is obvious, for equal number of bb events, the change in Δ (LKK) due to 8-8 mixing is more marked at lower energies than at higher energies, since the K multiplicity in the bottom quark jet is lower at lower \sqrt{s} , resulting in smaller background.

The actual contribution to Δ ($\rm \&$ KK) from the $\rm B_S^{\bullet} - \overline B_S^{\bullet}$ mixing, namely

$$\frac{\Delta(lkk, \chi_s) - \Delta(lkk, \chi_{s*0})}{\Delta(lkk, \chi_{s*0})}$$

, is independent of $f(s\overline{s})$. In contrast, the dilepton ratio

In fig. (4), we show how to determine $f(s\overline{s})$ in bottom quark jets, where we plot the branching ratio for the inclusive final states \mathfrak{S} (e⁺e⁻ \rightarrow ($\ell^{+}K^{+}K^{-} + \ell^{+}K^{+}K^{-} + \ell^{-}K^{+}K^{-} + \ell^{-}K^{+}K^{-} + \ell^{-}K^{-}K^{-} + \ell^{-}K^{-}K^{-$

Finally, in fig. (5) we show the dependence of Δ (LKK) on the assumed branching ratios for the inclusive decays $F^+ \rightarrow K^{\pm} X$. This serves as a fair indication of the attendant uncertainty. However, this uncertainty is not due to some artifact of our model but due to lack of experimental data on F^{\pm} decays and we hope would be soon removed.

5. Conclusions

In conclusion, we have discussed a new measure, $\Delta(\ell\text{KK})$, of B_s^{\bullet} - $\overline{B_s^{\bullet}}$ mixing, which we hope is useful for experiments studying bottom hadron production in the continuum e^+e^- and $\overline{p}p$ collisions. The measure is meaningful only for those

experiments having good $L^{\frac{1}{2}}$ and $K^{\frac{1}{2}}$ detection ability. It goes beyond the standard technique of measuring mixings namely the ratio $L^{\frac{1}{2}}L^{\frac{1}{2}}/\ell^{\frac{1}{2}}\ell^{\frac{1}{2}}$ in $(e^+e^-, \vec{p}p) \to b\vec{b} \to l\vec{l} X$ and the reduction in the electroweak charge asymmetry in the process $e^+e^- \to b\vec{b} \to l^{\frac{1}{2}} X$, in so far as it is sensitive only to the $B_S^0 - \vec{b}_S^0$ mixing. It depends on the semileptonic branching ratio $BR(B_S^0 \to l^- X)$ and the production cross-section $G(B_S^0 X)$ like its other two aforementioned counterparts. We propose a method to determine $f(s\vec{s})$ in the bottom quark jets; very probably this will determine $G(B_S^0 X)$. However, we do expect the dependence of $\Delta(l KK)$ on both $G(B_S^0 X)$ and $BR(B_S^0 \to l^- X)$ to be mild, since in the limiting case of $\sin^2 t \vec{l}_S = 0$ and leading $K^0 \to l^- X$ mesons this dependence drops out.

In addition, we hope that the lepton-kaon correlations, suggested in this paper will bring us closer to an understanding of the heavy quark jet flavour profile.

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Branching Ratios (%)			
55.0			
9.5			
30.0			
6.5			
case (i) case (ii)			
20.0 30.0			
30.0 45.0			

Table 1: Inclusive branching ratios for the charmed meson decays used in the calculations.

Table 3: Estimates rates based on 10^5 $b\overline{b}$ eventsfor the production of final states $e^+e^- \rightarrow b\overline{b} \rightarrow \ell \overline{\ell}$ %, ℓ KKX (ℓ = e + μ) at \sqrt{s} = m_Z = 93 GeV with cuts (ii) described in the text.

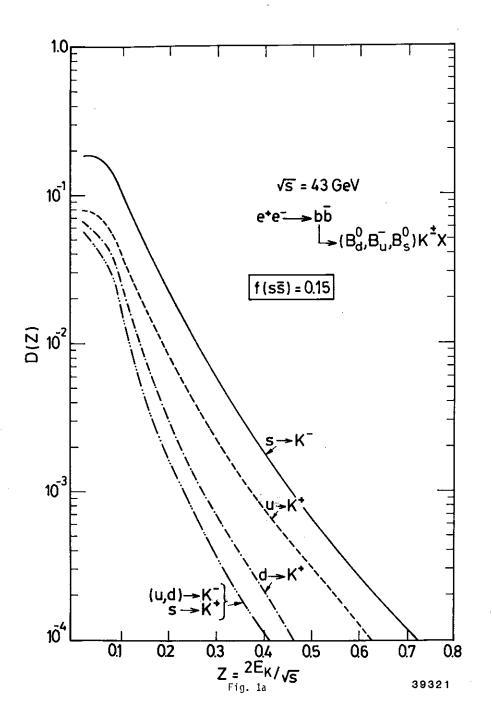
	χ_{s}	8 _± 8 _± ×	1*1°×	i [‡] l [‡] x/iīx	Į [∓] K [±] k [±] X	$i^{\overline{+}}k^{\overline{+}}k^{\overline{+}}X$	l ⁺ k ⁺ k ⁻ X	∆(lkk)
	0.0	845	4065	0.21	590	1275	6010	0.37
	0.20	1100	3800	0.29	685	1220	5970	0.28
į	0.30	1200	3710	0.32	750	1180	5945	0.22
	0.40	1270	3640	0.35	800	1140	5935	0.17
	0.5	1370	3540	0.38	845	1110	5920	0.14
L					<u> </u>	<u> </u>		

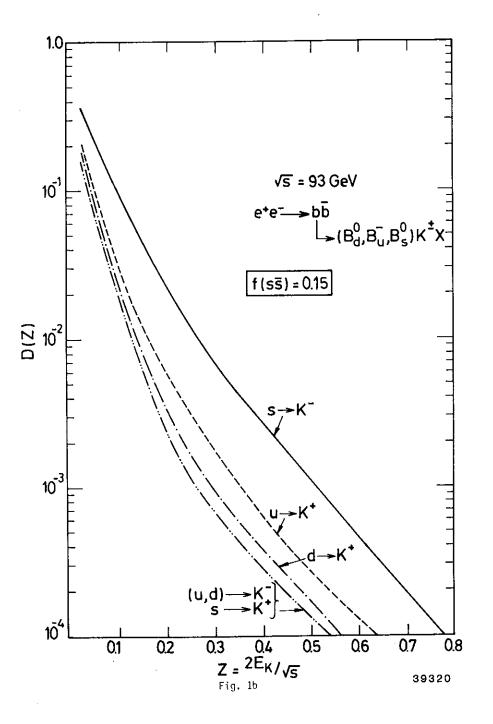
Table 2: Estimated rates based on 10^5 bb events for the production of final states $e^+e^- \rightarrow b\bar{b} \rightarrow \ell\bar{\ell}$ X, ℓ KKX (ℓ = e + μ) at \sqrt{s} = 43 GeV with cuts (i) described in the text.

Figure Captions

- Fig. 1(a): Fragmentation functions O(Z) for $q + K^T X$ produced in association with a bottom meson in the process $e^+e^- + b\bar{b}$ at $\sqrt{s} = 43$ GeV, with $f(s\bar{s}) = 0.15$
 - 1(b): Same as (1a) but at $\sqrt{s} = m_7 \pm 93$ GeV.
- Fig. 2(a): The differential cross-section $\frac{4}{5(b\bar{b})} \frac{d5}{d\bar{z}} \left(e^{+}e^{-} + B k^{\pm} X \right)$ for the various bottom mesons at $\sqrt{s} = 43$ GeV, with $f(s\bar{s}) = 0.15$. The B and K mesons belong to the same jet (hemisphere).
 - 2(b): Same as (2a) but at $\sqrt{s} = m_7 \approx 93$ GeV.
- Fig. 3(a): The quantity $\Delta(lkk) = \left[6\left(e^{t}e^{-}+l^{\mp}k^{\pm}x^{\mp}x\right)-6\left(e^{t}e^{-}+l^{\mp}k^{\pm}k^{\pm}x\right)\right]/$ $\left[6\left(e^{t}e^{-}+l^{\mp}k^{\mp}x^{\mp}x\right)+6\left(e^{t}e^{-}+l^{\mp}k^{\pm}k^{\pm}x\right)\right]$ as a function of the mixing measure N_{ϵ} at N_{ϵ} = 43 GeV with the indicated values of $f(s\bar{s})$ and cuts. Note that l_{ϵ} KK belong to the same jet (hemisphere).
 - 3(b): Same as (3a) but at $\sqrt{s} = m_Z 93$ GeV.
- Fig. 4(a): The branching ratio $6(a^{\dagger}a^{} + b \overset{\bullet}{k} \overset{\bullet}{k})$ summed over all charged combinations of $(a^{\dagger}a^{} + b \overset{\bullet}{k})$ summed over all charged $b^{\dagger}a$ and $b^{\dagger}a$ as a function of b of b with the indicated cuts at b = 43 GeV. Note that b belong to the same jet (hemisphere).
 - 4(b): Same as (4a) but at $\sqrt{s} = m_Z = 93 \text{ GeV}$.

Fig. 5: The dependence of the quantity Δ ($\mbox{$\ell$}$ KKK) on the assumed branching ratios for the inclusive decays $\mbox{$F^+$} \rightarrow \mbox{$K^-$} X$ (sets (i) and (ii) from table (1)) at $\mbox{$\sqrt{s}$} = 43$ GeV, $\mbox{$f(s\bar{s})$} = 0.15$ and indicated cuts.





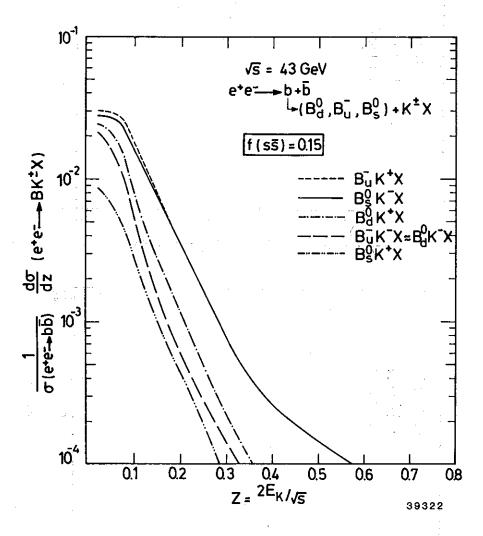


Fig. 2a

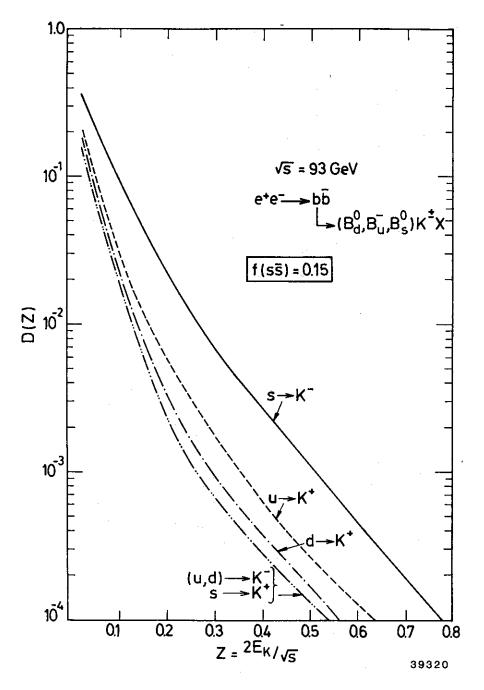


Fig. 2b

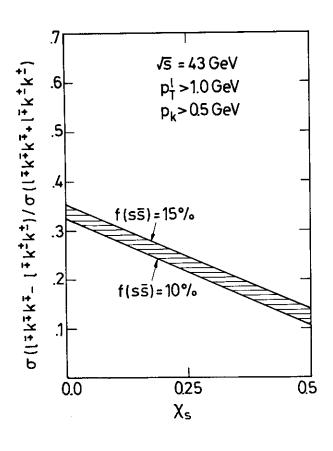


Fig. 3a

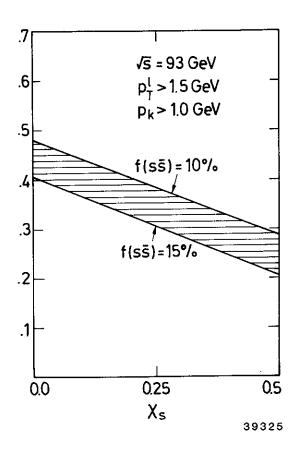


Fig. 3b

