

Employing RHIC and LHC data to determine TMD gluon density in a proton

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Abstract

Transverse momentum dependent (TMD) parton distributions in a proton are important in high energy physics from both theoretical and phenomenological points of view. Using the latest RHIC and LHC data on the inclusive soft hadron production in pp and AA collisions at small transverse momenta, we determine the parameters of the initial TMD gluon density, derived in the framework of quark-gluon string model at the low scale $\mu_0 \sim 1 - 2$ GeV and refine its large- x behaviour using the LHC data on the $t\bar{t}$ production at $\sqrt{s} = 13$ TeV. Then, we apply the Catani-Ciafaloni-Fiorani-Marchesini (CCFM) evolution equation to extend the obtained TMD gluon density to the whole kinematical region. In addition, the complementary TMD valence and sea quark distributions are generated. The latter are evaluated in the approximation where the gluon-to-quark splitting occurs at the last evolution step using the TMD gluon-to-quark splitting function. Several phenomenological applications of the proposed TMD quark and gluon densities to the LHC processes are discussed.

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1 Introduction

In the recent years an understanding has been obtained that a theoretical description of a number of processes at high energies and large momentum transfer containing multiple hard scales requires unintegrated, or transverse momentum dependent (TMD) parton density functions [1], which encode non-perturbative information on proton structure, including transverse momentum and polarization degrees of freedom. The TMD parton densities are related to the physical cross sections and other observables, measured in the collider experiments, via TMD factorization theorems in Quantum Chromodynamics (QCD). At present, the Collins-Soper-Sterman factorization approach, designed for semi-inclusive processes with a finite and non-zero ratio between the hard scale and total energy [2], and high-energy factorization [3] (or k_T -factorization [4]) approach, valid in the limit of a fixed hard scale and high energy, are developed. The factorization theorems provide the necessary framework to separate hard partonic physics, described with a perturbative QCD expansion, from soft hadronic physics and allow one to determine the TMD parton distributions from collider data.

In the high-energy factorization, the production cross sections at low transverse momenta are governed by the non-perturbative input to the TMD parton density functions. The latter, being used as an initial condition for the subsequent QCD evolution, could play an important role for phenomenological applications [5–8]. As it was shown [9–11], its influence on the description of the experimental data can be significant. At present, several approaches to determine the TMD gluon density in a proton (or rather its initial parameters) are known in the literature. In the Kimber-Martin-Ryskin (KMR) scheme, developed at leading (LO) [12] and next-to-leading (NLO) [13] orders, the TMD quark and gluon densities are derived from the conventional parton distribution functions. At low $k_T \leq \mu_0 \sim 1$ GeV they are defined from a simple normalization condition. Recently, the TMD quark and gluon densities in a proton were determined [14] from fits to precision measurements of deep inelastic scattering cross sections at HERA and evolved by Dokshitzer-Gribov-Lipatov-Altarelli-Parisi (DGLAP) evolution [15] with NLO splitting functions using the parton branching method [16, 17]. In a more complicated approach [18], based on the Catani-Ciafaloni-Fiorani-Marchesini (CCFM) gluon evolution equation [19], the parameters of initial TMD gluon distribution were fitted from the precision HERA data on proton structure function $F_2(x, Q^2)$ in the range $x < 5 \cdot 10^{-3}$, $Q^2 > 5$ GeV² and $F_2^c(x, Q^2)$ at $Q^2 > 2.5$ GeV², assuming the Gaussian-like dependence on the intrinsic gluon transverse momentum k_T at $k_T \leq \mu_0 \sim 2$ GeV. In our previous papers [9–11] the initial TMD gluon density was derived in the framework of the soft quark-gluon string model [20–22] by taking into account gluon saturation effects at low Q^2 . The essential parameters were obtained from the best description of the inclusive spectra of hadrons produced in pp collisions at LHC energies in the midrapidity region at low transverse momenta $p_T \leq 4.5$ GeV. Being used with the CCFM evolution, the predictions based on the proposed TMD gluon density describe well the HERA measurements of the proton structure functions $F_2^c(x, Q^2)$, $F_2^b(x, Q^2)$ and $F_L(x, Q^2)$. Thereby, the connection between soft LHC processes and small- x physics at HERA in a wide kinematical region was established. An important advantage of the approaches [10, 11, 18] is that one can rather easily take into account a large piece of higher-order corrections, namely, part of NLO + NNLO + ... terms containing leading $\log 1/x$ enhancement of cross sections due to real initial state parton emissions, absorbed into the CCFM evolution¹ (see [24]

¹At present, most of the proposed TMD parton distributions in a proton is collected in the TMDLIB package [23], which is a C++ library providing a framework and an interface to the different parametrizations.

for more information).

In the present paper we continue our previous studies [9–11] and test the parameters of the initial TMD gluon density [9–11] using the recent NA61 [25], LHC [26–31] and RHIC [32, 33] data for soft hadron production in pp and AA collisions obtained in a wide energy range. Moreover, we refine its large- x behaviour using the latest LHC data on the inclusive top quark pair production at $\sqrt{s} = 13$ TeV [34]. Following Refs. [10, 11], we extend the updated TMD gluon distribution to the whole range of the longitudinal momentum fraction x , transverse momentum \mathbf{k}_T^2 and hard scale μ^2 numerically using the UPDFEVOLV package [35], which is the CCFM evolution code for TMD parton densities. In our opinion, the CCFM equation is the most suitable tool for our study since it smoothly interpolates between the small- x Balitsky-Fadin-Kuraev-Lipatov [36] (BFKL) gluon dynamics and the conventional DGLAP one. We supply the obtained TMD gluon density with the corresponding TMD valence and sea quark distributions, calculated in the approximation, where the sea quarks occur in the last gluon splitting. Finally, we discuss several phenomenological applications of the proposed TMD parton densities to hard LHC processes, sensitive to the quark and gluon content of the proton.

The paper is organized as follows. In Section 2 we describe how we determine the initial gluon density from the LHC data and discuss its subsequent QCD evolution. In Section 3 we illustrate the use of the obtained TMD gluon density at the LHC. We give conclusions in Section 4.

2 Non-perturbative TMD gluon input and evolution

In fact, the determination of the parameters of the initial TMD gluon density in a proton can be splitted into the two almost independent pieces referring to the regions of small and large x . We consider first the small- x region and start from the simple analytical expression for the starting TMD gluon distribution function at some fixed scale $\mu_0 \sim 1 - 2$ GeV. It can be presented in a form [11]

$$f_g^{(0)}(x, \mathbf{k}_T^2, \mu_0^2) = \tilde{f}_g^{(0)}(x, \mathbf{k}_T^2, \mu_0^2) + \lambda(x, \mathbf{k}_T^2, \mu_0^2) f_g(x, \mathbf{k}_T^2), \quad (1)$$

where x and \mathbf{k}_T are the proton longitudinal momentum fraction and two-dimensional gluon transverse momentum, respectively. The first term, $\tilde{f}_g^{(0)}(x, \mathbf{k}_T^2, \mu_0^2)$, was calculated [9] within the soft QCD model and reads:

$$\tilde{f}_g^{(0)}(x, \mathbf{k}_T^2, \mu_0^2) = c_0 c_1 (1-x)^b \times \left[R_0^2(x) \mathbf{k}_T^2 + c_2 (R_0^2(x) \mathbf{k}_T^2)^{a/2} \right] \exp \left(-R_0(x) |\mathbf{k}_T| - d [R_0^2(x) \mathbf{k}_T^2]^{3/2} \right), \quad (2)$$

where $R_0^2(x) = (x/x_0)^\lambda / \mu_0^2$ and $c_0 = 3\sigma_0 / 4\pi^2 \alpha_s$. The parameters $\sigma_0 = 29.12$ mb, $\lambda = 0.22$, $x_0 = 4.21 \cdot 10^{-5}$ and $\alpha_s = 0.2$ come from the Golec-Biernat-Wüsthoff (GBW) saturation model [37], while other parameters a , b , c_1 , c_2 and d were fitted from LHC data on inclusive spectra of charged hadrons. The numerical values of these parameters, details of the calculations and the relation between the TMD gluon density and the inclusive hadron spectra are given in our previous papers [9–11]. The gluon density $\tilde{f}_g^{(0)}(x, \mathbf{k}_T^2, \mu_0^2)$ differs from the one obtained in the GBW model at $|\mathbf{k}_T| < 1$ GeV and coincides with the GBW gluon at larger $|\mathbf{k}_T| > 1.5$ GeV [9]. The second term, $f_g(x, \mathbf{k}_T^2)$, represents the analytical solution [38] of the linear BFKL equation at low x weighted with a matching function $\lambda(x, \mathbf{k}_T^2, \mu_0^2)$:

$$f_g(x, \mathbf{k}_T^2) = \alpha_s^2 x^{-\Delta} t^{-1/2} \frac{1}{v} \exp \left[-\frac{\pi \ln^2 v}{t} \right], \quad (3)$$

$$\lambda(x, \mathbf{k}_T^2, \mu_0^2) = c_0 \left(\frac{x}{x_0} \right)^{0.81} \exp \left[-k_0^2 \frac{R_0(x)}{|\mathbf{k}_T|} \right], \quad (4)$$

where $t = 14\alpha_s N_c \zeta(3) \ln(1/x)$, $\Delta = 4\alpha_s N_c \ln 2/\pi$, $v = |\mathbf{k}_T|/\Lambda_{\text{QCD}}$ and $k_0 = 1$ GeV. This term allows one to describe LHC measurements of inclusive charged hadrons up to $p_T \leq 4.5$ GeV [11]. It is important that the contribution from $f_g(x, \mathbf{k}_T^2)$ is only non-zero at $|\mathbf{k}_T| \ll \Lambda_{\text{QCD}} (1/x)^\delta$ with $\delta = \alpha_s N_c$, resulting in an average generated gluon transverse momentum of $\langle |\mathbf{k}_T| \rangle \sim 1.9$ GeV. The latter value is close to the non-perturbative QCD regime, that allows one to treat the TMD gluon density above as a starting one for the CCFM evolution.

Previously, the phenomenological parameters a , b , c_1 , c_2 and d in (1) — (4) were determined in the small- x region only, where $x \sim 1 \cdot 10^{-4} - 1 \cdot 10^{-5}$ (see [9–11]). The fit was based on NA61 data on inclusive cross sections of π^- meson production in pp collisions at initial momenta 31 and 158 GeV [25] and on CMS [26] and ATLAS [27] data on inclusive hadron production in pp collisions at the LHC. In the present note we tested all these parameters using the experimental data on the pion transverse mass distribution in Au + Au and Pb + Pb collisions taken by the STAR Collaboration at the RHIC [32,33] and ALICE Collaboration at the LHC [28–31]. The details of the calculations of hadron production cross sections in AA collisions are given in [39]. Let us stress that the possible higher-order corrections (see, for example, [40–42]) to the leading-order BFKL motivated k_T -dependence of the proposed gluon input at low- x (as well as saturation dynamics) are effectively included.

Next, we note that determination of the parameters of the TMD gluon density in the small- x region only could result in significant theoretical uncertainties of the predictions and/or poor description of the data at moderate and large x values. Therefore, in the present paper we refine some of these parameters, essential in the large x region, using recent experimental data on inclusive $t\bar{t}$ production taken by the CMS Collaboration at $\sqrt{s} = 13$ TeV [34]. These data refer to $x \sim 2m_t/\sqrt{s} \sim 3 \cdot 10^{-2}$ (with a top mass $m_t \sim 170$ GeV) and are reported at the parton level in the full phase space, allowing us to avoid the numerical simulation of top quark decays. To calculate the $t\bar{t}$ production cross sections in the k_T -factorization approach we follow our previous consideration [43]. We find that $b = 10$ and $d = 0.4$ are more preferable to describe the distributions on the rapidity and transverse momentum of top quark pairs. The latter leads, in addition, to a different value of overall normalization $n = 0.27$ in (1), which was determined using the CMS data on inclusive b -jet production.

The illustration of the satisfactory description of the RHIC [32,33] and LHC data [28–31] on soft hadron production in pp and AA collisions at mid-rapidities is presented in Fig. 1. The soft QCD predictions include both gluon and quark contributions. The perturbative QCD corrections, calculated [44,45] at LO, are divergent at low transverse momenta² (not shown for AA collisions). The hadron production at $p_T < 2$ GeV are fitted with $\chi^2/n.d.f = 0.9$. We would like to note here that the approach [39] with the above determined parameters of the TMD gluon density is able to describe the experimental data in a wide energy range. Concerning the large- x region, the achieved description of the CMS data [34] on the top pair production is illustrated in Fig. 2, where the transverse momentum and rapidity distributions of the top quarks are shown as an example. For the reader's convenience, we collected all the parameters of (1) — (4) in Table 1.

Next, we extend the obtained TMD gluon density (1) — (4) to a higher scale μ^2 using the CCFM evolution equation. This equation resums large logarithms $\alpha_s^n \ln^n 1/x$ and $\alpha_s^n \ln^n 1/(1-x)$ and, therefore, is valid at both small and large x (see, for example, [24]

²The kinematical region $p_T \sim 1.8 - 2.2$ GeV can be treated as the matching region of the soft QCD and pQCD calculations.

Parameter	a	b	c_1	c_2	d	μ_0/GeV
Fitted value	0.3	10.0	0.3295	2.3	0.4	2.2

Table 1: Numerical values of the parameters of the TMD gluon density (1) — (4). All other parameters, namely, x_0 , σ_0 , λ and α_s are unchanged.

for more information). In the leading logarithmic approximation³, the CCFM equation with respect to the evolution scale μ^2 can be written as

$$f_g(x, \mathbf{k}_T^2, \mu^2) = f_g^{(0)}(x, \mathbf{k}_T^2, \mu_0^2) \Delta_s(\mu^2, \mu_0^2) + \int \frac{dz}{z} \int \frac{dq^2}{q^2} \theta(\mu - zq) \Delta_s(\mu^2, z^2 q^2) P_{gg}(z, q^2, \mathbf{k}_T^2) f_g(x/z, \mathbf{k}'_T^2, q^2), \quad (5)$$

where $\mathbf{k}'_T = \mathbf{q}(1 - z) + \mathbf{k}_T$. The exact analytical expressions for the Sudakov form factor $\Delta_s(p^2, q^2)$ and gluon splitting functions $P_{gg}(z, q^2, \mathbf{k}_T^2)$ can be found, for example, in [35]. The CCFM equation with the starting TMD gluon density $f_g^{(0)}(x, \mathbf{k}_T^2, \mu_0^2)$ given by (1) — (4) was solved numerically using the UPDFEVOLV package [35]. As it was done earlier [11], to produce the TMD valence and sea quark distributions we apply the approach [49]. So, the TMD sea quark density was calculated in the approximation where the sea quarks occur in the last gluon splitting:

$$f_q^{(s)}(x, \mathbf{k}_T^2, \mu^2) = \int_x^1 \frac{dz}{z} \int d\mathbf{q}_T^2 \frac{1}{\Delta^2} \frac{\alpha_s}{2\pi} P_{qg}(z, \mathbf{q}_T^2, \Delta^2) f_g(x/z, \mathbf{q}_T^2, \bar{\mu}^2), \quad (6)$$

where z is the fraction of the gluon light-cone momentum carried by the quark and $\Delta = \mathbf{k}_T - z\mathbf{q}_T$. The hard scale $\bar{\mu}^2$ was defined [50] from the angular ordering condition which is natural from the CCFM point of view: $\bar{\mu}^2 = \Delta^2/(1 - z)^2 + \mathbf{q}_T^2/(1 - z)$. The off-shell gluon-to-quark splitting function $P_{qg}(z, \mathbf{q}_T^2, \Delta^2)$ was calculated in [51].

The gluon density $f_g(x, \mathbf{k}_T^2, \mu^2)$ obtained according to (1) — (5), labeled below as *Moscow-Dubna 2018*, or *MD'2018*, is shown in Fig. 3 versus the longitudinal momentum fraction x and transverse momentum \mathbf{k}_T at different evolution scales. Additionally, we plot the TMD gluon distribution [18] (namely, the *JH'2013 set 2*) which is widely discussed in the literature and commonly used in applications. One can observe some difference in the absolute normalization and shape between both TMD gluon distributions. In particular, the \mathbf{k}_T -tail of the *MD'2018* density function is the contribution due to the solution of the linear BFKL equation, as was described above. Actually, it was needed to improve the description of the LHC data on charge hadron production in pp collisions at $\sqrt{s} = 7$ TeV and $2.5 < p_T < 4$ GeV (see [9] for more details). Below we will consider the phenomenological consequences for several LHC processes⁴.

³The next-to-leading logarithmic corrections for the CCFM equation are still unknown. However, as it was argued [46], amending the leading logarithmic evolution with kinematical constraint [47, 48] leads to reasonable QCD predictions, although still formally only to leading logarithmic accuracy (see also [24]).

⁴The *MD'2018* gluon density will be implemented in forthcoming release of the TMDLIB package.

3 Phenomenological applications

We are now in a position to apply the *MD'2018* gluon density to several hard processes studied at hadron colliders. We use the k_T -factorization approach, where the production cross section of any process under consideration (say, in pp collisions) can be written as

$$\sigma = \int dx_1 dx_2 \int d\mathbf{k}_{1T}^2 d\mathbf{k}_{2T}^2 f_{q/g}(x_1, \mathbf{k}_{1T}^2, \mu^2) f_{q/g}(x_2, \mathbf{k}_{2T}^2, \mu^2) \times \times d\hat{\sigma}(x_1, x_2, \mathbf{k}_{1T}^2, \mathbf{k}_{2T}^2, \mu^2), \quad (7)$$

where $\hat{\sigma}(x_1, x_2, \mathbf{k}_{1T}^2, \mathbf{k}_{2T}^2, \mu^2)$ is the corresponding off-shell (depending on the transverse momenta of incoming particles) partonic cross section. Everywhere below, the multidimensional integration was performed by the Monte Carlo technique, using the routine VEGAS [52].

3.1 Proton structure functions F_2^c and F_2^b

It is well-known that the basic information on the proton structure can be extracted from deep inelastic ep scattering. Its differential cross-section can be presented in the simple form:

$$\frac{d^2\sigma}{dx dy} = \frac{2\pi\alpha^2}{xQ^4} \left[\left(1 - y + \frac{y^2}{2}\right) F_2(x, Q^2) - \frac{y^2}{2} F_L(x, Q^2) \right], \quad (8)$$

where $F_2(x, Q^2)$ and $F_L(x, Q^2)$ are the proton transverse and longitudinal structure functions, x and y are the usual Bjorken scaling variables. In the present note we concentrate on the charm and beauty contributions to $F_2(x, Q^2)$. The latter are described through perturbative generation of charm and beauty quarks and, therefore, directly related with the gluon content of the proton. Our evaluation below is based on the formulas [53]. Numerically, we apply the pole mass $m_c = 1.7$ GeV and $m_b = 4.8$ GeV and strictly follow our previous consideration [53] in all other aspects.

Our results are shown in Figs. 3 and 4 in comparison with the latest ZEUS [54] and H1 data [55, 56]. The green and grey curves correspond to the predictions obtained with the *MD'2018* and *JH'2013 set 2* gluon densities, whereas the shaded bands represent the estimations of the scale uncertainties of these calculations. We find that the *MD'2018* predictions for $F_2^c(x, Q^2)$ and $F_2^b(x, Q^2)$ are in reasonable agreement with the HERA data in a wide region of x and Q^2 , both in overall normalization and shape. It slightly overshoots the *JH'2013 set 2* predictions at small Q^2 and low $x \leq 10^{-4}$. At larger Q^2 and moderate and/or large $x \geq 10^{-2}$, the *JH'2013 set 2* gluon density function tends to overestimate the HERA data on the structure function $F_2^b(x, Q^2)$, that is due to the determination of input parameters of this gluon density at small x only [18]. Therefore, the influence of the shape and other parameters of the initial non-perturbative gluon distribution on the description of the collider data is significant for a wide region of x and Q^2 [9–11]. The *MD'2018* gluon density, where all these parameters are verified by the description of LHC data, leads to a better agreement with the HERA data, that confirms the link between soft processes at the LHC and low- x physics at HERA, pointed out earlier [9–11]. Note that to estimate the scale uncertainties of the *JH'2013 set 2* calculations the method proposed in [18] was used. So, to evaluate the latter we used the *JH'2013 set 2+* and *JH'2013 set 2-* sets instead of default one *JH'2013 set 2*. These two sets represent a variation of the renormalization scale used in the off-shell production amplitude: the *JH'2013 set 2+* stands for a variation of $2\mu_R$, while *JH'2013 set 2-* reflects $\mu_R/2$. This method leads to somewhat reduced uncertainty bands in comparison with the *MD'2018* predictions.

3.2 Single top production at the LHC

Recently the CMS and ATLAS Collaborations have measured the differential cross sections of single top production (in the t -channel) at the LHC as a function of the transverse momenta and rapidity of the top quark and top-antiquark at $\sqrt{s} = 8$ TeV [57, 58]. Such measurements are known to be very useful for constraining parton densities in a proton [59, 60]. To calculate the total and differential production cross sections we employ the four-flavor scheme (4FS), so that the leading contribution comes from the $2 \rightarrow 3$ off-shell (reggeized) quark-gluon interaction subprocess:

$$q^*(k_1) + g^*(k_2) \rightarrow q'(p_1) + \bar{b}(p_2) + t(p), \quad (9)$$

where the four-momenta of all particles are indicated in parentheses. The main contribution to the amplitude (8) comes from the diagram, which corresponds to initial gluon splitting to $b\bar{b}$ pair with subsequent exchange of W -boson between the b and the light quark. The latter reads

$$\begin{aligned} \mathcal{A} = & -g \frac{e^2}{8 \sin^2 \theta_W} V_{qq'} V_{tb} \bar{u}_{s_1}(p_1) \Gamma_{(+)}^\mu(k_1, -p_1) (1 - \gamma^5) u_{s_2}(x_1 l_1) \times \\ & \bar{u}_{s_3}(p) \gamma_\mu (1 - \gamma^5) \frac{\hat{k}_2 - \hat{p}_2 + m_b}{(k_2 - p_2)^2 - m_b^2} \hat{e}(k_2) v_{s_4}(p_2) t^a \frac{1}{(p_1 - k_1)^2 - m_W^2 + im_W \Gamma_W}, \end{aligned} \quad (10)$$

where g and e are the strong and electric charges respectively, θ_W is the weak Weinberg mixing angle, $V_{q_a q_b}$ are the Cabibbo-Kobayashi-Maskawa (CKM) matrix elements, m_b and m_W are the b -quark and W -boson masses, a is the eight-fold color index and Γ_W is the W -boson full decay width. The effective vertex $\Gamma_{(+)}^\mu(k, q)$, that ensures gauge invariance of the amplitude (9) despite the off-shell initial partons, can be written as [61, 62]:

$$\Gamma_{(+)}^\mu(k, q) = \gamma^\mu - \hat{k} \frac{l_1^\mu}{l_1 \cdot q}, \quad (11)$$

where l_1 is the proton four-momentum ($k_1 = x_1 l_1 + k_{1T}$ and $k_2 = x_2 l_2 + k_{2T}$). The polarization sum for the off-shell gluon is taken in the BFKL form [3, 4]:

$$\sum \epsilon^\mu(k) \epsilon^\nu(k) = \frac{k_T^\mu k_T^\nu}{\mathbf{k}_T^2}. \quad (12)$$

In all other aspects the calculation is straightforward and follows standard Feynman rules. The evaluation of traces was performed using the algebraic manipulation system FORM.

Having calculated the squared amplitude (9), one can evaluate the total and differential cross sections of single top production according to the TMD factorization formula (7). Numerically, we took $m_W = 80.4$ GeV and $\Gamma_W = 2.1$ GeV. The light quarks were kept massless, while for heavy quarks we took $m_b = 4.75$ GeV and $m_t = 175$ GeV. The weak mixing angle was chosen to correspond to $\sin^2 \theta_W = 0.23$ [63]. As the renormalization μ_R and factorization μ_F scales, we choose the largest mass parameter in our calculation, the top transverse mass⁵.

The results of our calculations for single top quark production in t -channel are presented in Fig. 5 — 7 in comparison with the CMS and ATLAS data [57, 58]. These data correspond to the absolute and normalized cross-sections on parton level, differential on top quark transverse momentum and rapidity. Studying the latter could lead to a more stringent comparison between data and theory due to reduced experimental (mainly

⁵The different choices of hard scales in the single top production are discussed in [60, 64].

systematic) and theoretical (scale) uncertainties. We find that both the *MD'2018* and *JH'2013 set 2* gluon densities predict almost identical normalized cross sections, which agree with the CMS and ATLAS measurement quite well. However, the *MD'2018* density results in a little smaller total cross section than the *JH'2013 set 2* one, that leads to somewhat better description of the data. Thus the calculations endorse the usage of the *MD'2018* gluon density for evaluation of cross sections of processes with quite large x values involved. Note that the size of scale uncertainties of *MD'2018* and *JH'2013 set 2* calculations are rather close to each other in the kinematical region probed.

3.3 Inclusive Higgs boson production at the LHC

Very recently the CMS and ATLAS Collaborations have reported measurements [65–68] of the total and differential cross sections of inclusive Higgs boson production at $\sqrt{s} = 13$ TeV obtained in different Higgs decay channels. These measurements can be used to investigate the gluon dynamics in a proton since the dominant mechanism of inclusive Higgs production at the LHC is gluon-gluon fusion [69–72]. Here, to calculate the total and differential cross sections of Higgs boson production we strictly follow our previous consideration [73]. The latter is based on the off-shell amplitude of the gluon-gluon fusion subprocess $g^*g^* \rightarrow H$ calculated using the effective Lagrangian [74, 75] for the Higgs coupling to gluons and extended recently to the subsequent $H \rightarrow \gamma\gamma$, $H \rightarrow W^+W^- \rightarrow e^\pm\mu^\mp\nu\bar{\nu}$ [76] and $H \rightarrow ZZ^* \rightarrow 4l$ decays [76, 77]. The details of the calculations are explained in [76]. Below we present the numerical results obtained with the *MD'2018* and *JH'2013 set 2* gluon densities for $H \rightarrow \gamma\gamma$ and $H \rightarrow ZZ^* \rightarrow 4l$ decay modes.

The CMS and ATLAS measurements refer to a restricted part of the phase space (fiducial phase space) defined to match the experimental acceptance in terms of the photon kinematics and event selection. In the CMS analysis [65] two isolated photons originating from the Higgs boson decays are required to have pseudorapidities $|\eta^\gamma| < 2.5$. Photons with largest and next-to-largest transverse momentum p_T^γ (so-called leading and subleading photons) must satisfy the conditions of $p_T^\gamma/m^{\gamma\gamma} > 1/3$ and $p_T^\gamma/m^{\gamma\gamma} > 1/4$ respectively, where the diphoton mass $m^{\gamma\gamma}$ is required to be $100 < m^{\gamma\gamma} < 180$ GeV. In the ATLAS measurement [67] both decay photons must have pseudorapidities $|\eta^\gamma| < 2.37$ with the leading (subleading) photon satisfying $p_T^\gamma/m^{\gamma\gamma} > 0.35$ (0.25), while invariant mass $m^{\gamma\gamma}$ is required to be $105 < m^{\gamma\gamma} < 160$ GeV. In the $H \rightarrow ZZ^* \rightarrow 4l$ decay channel, only events with a four-lepton invariant mass $118 < m_{4l} < 129$ GeV are kept by ATLAS Collaboration [68] and each lepton (electron or muon) must satisfy transverse momentum cut $p_T > 6$ GeV and be in the pseudorapidity range $|\eta| < 2.47$. The highest- p_T lepton in the quadruplet must have $p_T > 20$ GeV and the second (third) lepton in p_T order must satisfy $p_T > 15(10)$ GeV. These leptons are required to be separated from each other by $\Delta R = \sqrt{(\Delta\eta)^2 + (\Delta\phi)^2} > 0.1(0.2)$ when having the same (different) lepton flavors. The invariant mass m_{12} of the lepton pair closest to the Z boson mass (leading pair) is required to be $50 < m_{12} < 106$ GeV. The subleading pair is chosen as the remaining lepton pair with invariant mass m_{34} closest to the Z boson mass and satisfying the requirement $12 < m_{34} < 115$ GeV. The CMS measurement [66] requires at least four leptons in the event with at least one lepton having $p_T > 20$ GeV, another lepton having $p_T > 10$ GeV and the remaining ones having $p_T > 7$ and 5 GeV respectively. All leptons must have the pseudorapidity $|\eta| < 2.4$, the leading pair invariant mass m_{12} must be $40 < m_{12} < 120$ GeV and subleading one should be $12 < m_{34} < 120$ GeV. Finally, the four-lepton invariant mass m_{4l} must satisfy $105 < m_{4l} < 140$ GeV cut.

The results of our calculations are shown in Figs. 8 and 9 in comparison with latest LHC data [65–68]. In the $H \rightarrow \gamma\gamma$ decay channel, we calculated the distributions on

the diphoton pair transverse momentum $p_T^{\gamma\gamma}$, absolute value of the rapidity $|y^{\gamma\gamma}|$, photon helicity angle $|\cos\theta^*|$ (in the Collins-Soper frame) and azimuthal angle difference $\Delta\phi^{\gamma\gamma}$ between the produced photons. In the $H \rightarrow ZZ^* \rightarrow 4l$ decay channel, we calculated distributions on the Higgs transverse momentum p_T^H , rapidity $|y^H|$, invariant mass of the subleading lepton pair m_{34} and cosine of the leading lepton pair decay angle $|\cos\theta^*|$ in the four-lepton rest frame with respect to the beam axis. We find that both the *MD'2018* and *JH'2013 set 2* predictions reasonably agree with the data within the uncertainties for all considered kinematical observables, although the *MD'2018* results lie a bit below *JH'2013 set 2* ones. Some tendency to underestimate the LHC data at large transverse momenta could be explained by the missing contributions from the weak boson fusion ($W^+W^- \rightarrow H$ and $ZZ \rightarrow H$) and/or associated HZ or HW^\pm production [78], which become important at high p_T and are not taken into account in our present consideration. The measured rapidity, $|\cos\theta^*|$ and m_{34} distributions are well reproduced by our calculations. As one can see, despite the fact that both the *MD'2018* and *JH'2013 set 2* gluon distributions agree with the available data, the inclusive Higgs boson production at the LHC is very sensitive to the TMD gluon density in a proton, in particular, to the parameters of the initial TMD gluon distribution. It could be important to further constrain the latter.

4 Conclusion

We have refined a fit of the experimental data on the inclusive spectra of the charged particles produced in the central pp and AA collisions at RHIC and the LHC to determine the TMD gluon density in a proton at the starting scale. The parameters of this fit do not depend on the initial energy in a wide energy interval. Using a numerical solution of the CCFM gluon evolution equation, we extended the derived TMD gluon density (denoted as *Moscow-Dubna 2018*, or *MD'2018 set*) to a whole kinematical region and supplied it with the relevant TMD valence and sea quark distributions. The latter was calculated in the approximation where the gluon-to-quark splitting occurred at the last evolution step using the TMD gluon-to-quark splitting function. Some phenomenological applications of the proposed *MD'2018* quark and gluon densities to the hard LHC processes were discussed. We demonstrated a significant influence of the initial non-perturbative gluon distribution on the description of the LHC data, that is important to further precise determination of the TMD quark and gluon densities in a proton.

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References

- [1] R. Angeles-Martinez, A. Bacchetta, I.I. Balitsky, D. Boer, M. Boglione, R. Boussarie, F.A. Ceccopieri, I.O. Cherednikov, P. Connor, M.G. Echevarria, G. Ferrera,

- J. Grados Luyando, F. Hautmann, H. Jung, T. Kasemets, K. Kutak, J.P. Lansberg, A. Lelek, G.I. Lykasov, J.D. Madrigal Martinez, P.J. Mulders, E.R. Nocera, E. Petreska, C. Pisano, R. Placakyte, V. Radescu, M. Radici, G. Schnell, I. Scimemi, A. Signori, L. Szymanowski, S. Taheri Monfared, F.F. Van der Veken, H.J. Van Haevermaet, P. Van Mechelen, A.A. Vladimirov, S. Wallon, *Acta Phys. Polon. B* **46**, 2501 (2015).
- [2] J.C. Collins, D.E. Soper, G.F. Sterman, *Nucl. Phys. B* **223**, 381 (1983),
J.C. Collins, D.E. Soper, G.F. Sterman, *Nucl. Phys. B* **250**, 199 (1985).
- [3] S. Catani, M. Ciafaloni, F. Hautmann, *Nucl. Phys. B* **366**, 135 (1991);
J.C. Collins, R.K. Ellis, *Nucl. Phys. B* **360**, 3 (1991).
- [4] L.V. Gribov, E.M. Levin, M.G. Ryskin, *Phys. Rep.* **100**, 1 (1983);
E.M. Levin, M.G. Ryskin, Yu.M. Shabelsky, A.G. Shuvaev, *Sov. J. Nucl. Phys.* **53**, 657 (1991).
- [5] E. Avsar, arXiv:1108.1181 [hep-ph]; arXiv:1203.1916 [hep-ph].
- [6] S.M. Aybat, T.C. Rogers, *Phys. Rev. D* **83**, 114042 (2011).
- [7] B.I. Ermolaev, M. Greco, S.I. Troyan, *Eur. Phys. J. C* **71**, 1750 (2011);
B.I. Ermolaev, M. Greco, S.I. Troyan, *Eur. Phys. J. C* **72**, 1953 (2012).
- [8] P. Kotko, K. Kutak, C. Marquet, E. Petreska, S. Sapeta, A. Van Hameren, *JHEP* **1509**, 106 (2015).
- [9] A.A. Grinyuk, A.V. Lipatov, G.I. Lykasov, N.P. Zotov, *Phys. Rev. D* **93**, 014035 (2016).
- [10] A.V. Lipatov, G.I. Lykasov, N.P. Zotov, *Phys. Rev. D* **89**, 014001 (2014).
- [11] A.A. Grinyuk, A.V. Lipatov, G.I. Lykasov, N.P. Zotov, *Phys. Rev. D* **87**, 074017 (2013).
- [12] M.A. Kimber, A.D. Martin, M.G. Ryskin, *Phys. Rev. D* **63**, 114027 (2001);
G. Watt, A.D. Martin, M.G. Ryskin, *Eur. Phys. J. C* **31**, 73 (2003).
- [13] A.D. Martin, M.G. Ryskin, G. Watt, *Eur. Phys. J. C* **66**, 163 (2010).
- [14] A. Bermudez Martinez, P. Connor, F. Hautmann, H. Jung, A. Lelek, V. Radescu, R. Zlebcik, arXiv:1804.11152 [hep-ph].
- [15] V.N. Gribov and L.N. Lipatov, *Sov. J. Nucl. Phys.* **15**, 438 (1972);
L.N. Lipatov, *Sov. J. Nucl. Phys.* **20**, 94 (1975);
G. Altarelli, G. Parisi, *Nucl. Phys. B* **126**, 298 (1977);
Yu.L. Dokshitzer, *Sov. Phys. JETP* **46**, 641 (1977).
- [16] F. Hautmann, H. Jung, A. Lelek, V. Radescu, R. Zlebcik, *Phys. Lett. B* **772**, 446 (2017).
- [17] F. Hautmann, H. Jung, A. Lelek, V. Radescu, *JHEP* **01**, 070 (2018).
- [18] F. Hautmann, H. Jung, *Nucl. Phys. B* **883**, 1 (2014).

- [19] M. Ciafaloni, Nucl. Phys. B **296**, 49 (1988);
S. Catani, F. Fiorani, G. Marchesini, Phys. Lett. B **234**, 339 (1990);
S. Catani, F. Fiorani, G. Marchesini, Nucl. Phys. B **336**, 18 (1990);
G. Marchesini, Nucl. Phys. B **445**, 49 (1995).
- [20] A.B. Kaidalov, Z. Phys. C **12**, 63 (1982); Surveys High Energy Phys. **13**, 265 (1999);
A.B. Kaidalov, O.I. Piskunova, Z. Phys. C **30**, 145 (1986); Yad. Fiz. **43**, 1545 (1986).
- [21] G.I. Lykasov, M.N. Sergeenko, Z. Phys. C **56**, 697 (1992); Z. Phys. C **52**, 635 (1991);
Z. Phys. C **70**, 455 (1996).
- [22] V.A. Bednyakov, G.I. Lykasov, V.V. Lyubushkin, Europhys. Lett. **92**, 31001 (2010).
- [23] <http://tmd.hepforge.org>
- [24] B. Andersson *et al.* (Small- x Collaboration), Eur. Phys. J. C **25**, 77 (2002);
J. Andersen *et al.* (Small- x Collaboration), Eur. Phys. J. C **35**, 67 (2004);
J. Andersen *et al.* (Small- x Collaboration), Eur. Phys. J. C **48**, 53 (2006).
- [25] NA61 Collaboration, Eur. Phys. J. C **74**, 2794 (2014).
- [26] CMS Collaboration, Phys. Rev. Lett. **105**, 022002 (2010).
- [27] ATLAS Collaboration, New J. Phys. **13**, 053033 (2011).
- [28] ALICE Collaboration, Eur. Phys. J. C **71**, 1655 (2011).
- [29] ALICE Collaboration, Phys. Lett. B **693**, 53 (2010).
- [30] ALICE Collaboration, Phys. Rev. D **82**, 052001 (2010).
- [31] ALICE Collaboration, Phys. Rev. D **88**, 044910 (2013).
- [32] STAR Collaboration, Phys. Rev. D **75**, 064901 (2007).
- [33] STAR Collaboration, Phys. Rev. Lett. **97**, 152301 (2006).
- [34] CMS Collaboration, arXiv:1803.08856 [hep-ex].
- [35] F. Hautmann, H. Jung, S. Taheri Monfared, Eur. Phys. J. C **74**, 3082 (2014).
- [36] E.A. Kuraev, L.N. Lipatov, V.S. Fadin, Sov. Phys. JETP **44**, 443 (1976);
E.A. Kuraev, L.N. Lipatov, V.S. Fadin, Sov. Phys. JETP **45**, 199 (1977);
I.I. Balitsky, L.N. Lipatov, Sov. J. Nucl. Phys. **28**, 822 (1978).
- [37] K. Golec-Biernat, M. Wüsthoff, Phys. Rev. D **59**, 014017 (1998); Phys. Rev. D **60**,
114023 (1999).
- [38] Yu.V. Kovchegov, Phys. Rev. D **61**, 074018 (2000).
- [39] G.I. Lykasov, A.I. Malakhov, arXiv:1801.07250 [hep-ph].
- [40] V.S. Fadin, L.N. Lipatov, Phys. Lett. B **429**, 127 (1998).
- [41] M. Ciafaloni, G. Camici, Phys. Lett. B **430**, 349 (1998).
- [42] D.N. Triantafyllopoulos, Nucl. Phys. B **648**, 293 (2003).

- [43] A.V. Lipatov, N.P. Zotov, Phys. Lett. B **704**, 189 (2011).
- [44] D.A. Artemenkov, G.I. Lykasov, A.I. Malakhov, Int. J. Mod. Phys. A **30**, 1550127 (2015).
- [45] V.A. Bednyakov, A.A. Grinyuk, G.I. Lykasov, M. Poghosyan, Int. J. Mod. Phys. A **27**, 1250042 (2012).
- [46] H. Jung, S.P. Baranov, M. Deak, A. Grebenyuk, F. Hautmann, M. Hentschinski, A. Knutsson, M. Krämer, K. Kutak, A.V. Lipatov, N.P. Zotov, Eur. Phys. J. C **70**, 1237 (2010).
- [47] J. Kwiecinski, A.D. Martin, P. Sutton, Z. Phys. C **71**, 585 (1996).
- [48] B. Andersson, G. Gustafson, J. Samuelsson, Nucl. Phys. B **467**, 443 (1996).
- [49] F. Hautmann, M. Hentschinski, H. Jung, Nucl. Phys. B **865**, 54 (2012).
- [50] F. Hautmann, M. Hentschinski, H. Jung, arXiv:1207.6420 [hep-ph].
- [51] S. Catani, F. Hautmann, Nucl. Phys. B **427**, 475 (1994); Phys. Lett. B **315**, 157 (1993).
- [52] G.P. Lepage, J. Comput. Phys. **27**, 192 (1978).
- [53] A.V. Kotikov, A.V. Lipatov, G. Parente, N.P. Zotov, Eur. Phys. J. C **26**, 51 (2002); A.V. Kotikov, A.V. Lipatov, N.P. Zotov, Eur. Phys. J. C **27**, 219 (2003).
- [54] ZEUS Collaboration, JHEP **1409**, 127 (2014).
- [55] H1 Collaboration, Eur. Phys. J. C **71**, 1769 (2011); Eur. Phys. J. C **72**, 2252 (2012).
- [56] H1 Collaboration, Eur. Phys. J. C **65**, 89 (2010).
- [57] CMS Collaboration, CMS-PAS-TOP-16-004.
- [58] ATLAS Collaboration, Eur. Phys. J. C **77**, 531 (2017).
- [59] S. Alekhin, J. Blümlein, S. Moch, R. Placakyte, Phys. Rev. D **94**, 114038 (2016).
- [60] Z. Sullivan, EPJ Web of Conferences **172**, 03008 (2018).
- [61] L.N. Lipatov, M.I. Vyazovsky, Nucl. Phys. B **597**, 399 (2001).
- [62] A.V. Bogdan, V.S. Fadin, Nucl. Phys. B **740**, 36 (2006).
- [63] PDG Collaboration, Chin. Phys. C **38**, 090001 (2014).
- [64] T. Stelzer, Z. Sullivan, S. Willenbrock, Phys. Rev. D **56**, 5919 (1997).
- [65] CMS Collaboration, CMS-PAS-HIG-17-015.
- [66] CMS Collaboration, CMS-PAS-HIG-16-041.
- [67] ATLAS Collaboration, arXiv:1802.04146 [hep-ex].
- [68] ATLAS Collaboration, arXiv:1708.02810 [hep-ex]; ATLAS-CONF-2017-032.
- [69] LHC Higgs Cross Section Working Group, arXiv:1101.0593 [hep-ph].

- [70] LHC Higgs Cross Section Working Group, arXiv:1201.3084 [hep-ph].
- [71] LHC Higgs Cross Section Working Group, arXiv:1307.1347 [hep-ph].
- [72] LHC Higgs Cross Section Working Group, arXiv:1610.07922 [hep-ph].
- [73] N.A. Abdulov, A.V. Lipatov, M.A. Malyshev, Phys. Rev. D **97**, 054017 (2018).
- [74] J.R. Ellis, M.K. Gaillard, D.V. Nanopoulos, Nucl. Phys. B **106**, 292 (1976).
- [75] M.A. Shifman, A.I. Vainstein, M.B. Voloshin, V.I. Zakharov, Sov. J. Nucl. Phys. **30**, 711 (1979).
- [76] A.V. Lipatov, M.A. Malyshev, N.P. Zotov, Phys. Lett. B **735**, 79 (2014);
- [77] R. Islam, M. Kumar, V.S. Rawoot, arXiv:1706.01402 [hep-ph].
- [78] A. Szczurek, M. Luszczak, R. Maciula, Phys. Rev. D **90**, 094023 (2014).

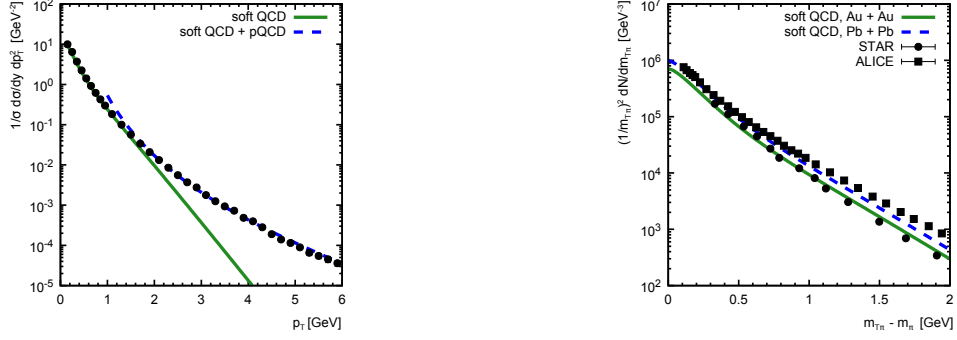


Figure 1: Left panel: the inclusive cross section of charge hadrons produced in pp collisions as a function of their transverse momentum at $\sqrt{s} = 7$ TeV. The experimental data are from CMS and ATLAS [26,27]. Right panel: pion transverse mass spectra in Au + Au and Pb + Pb collisions. The experimental data are from STAR [32,33] and ALICE [28–31].

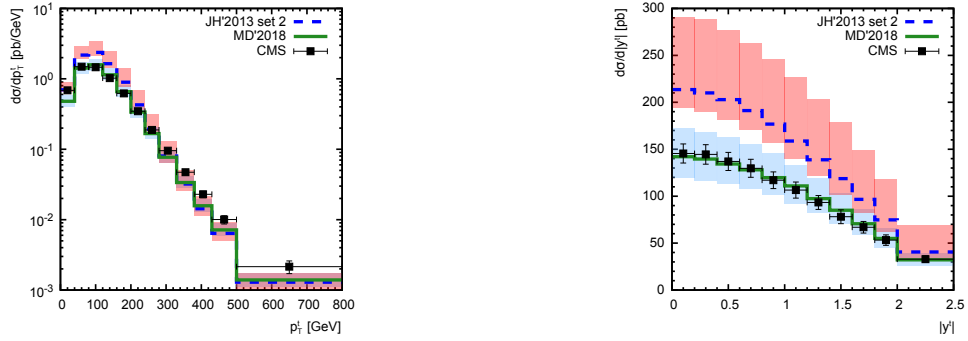


Figure 2: The transverse momentum and rapidity distributions of inclusive $t\bar{t}$ production in pp collisions at $\sqrt{s} = 13$ TeV. The green (solid) and blue (dashed) curves correspond to the predictions obtained using the $MD'2018$ and $JH'2013$ set 2 gluons, respectively. The shaded bands represent their scale uncertainties. The experimental data are from CMS [34].

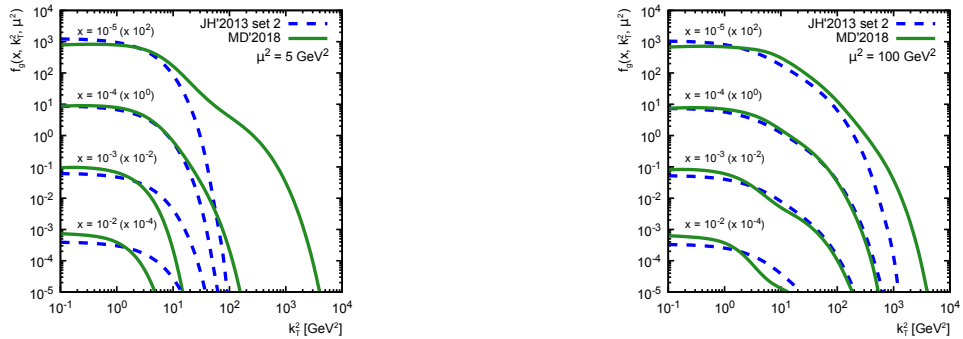


Figure 3: The TMD gluon densities in the proton calculated as a function of the gluon transverse momentum \mathbf{k}_T^2 at different longitudinal momentum fraction x and μ^2 values. The green (solid) and blue (dashed) curves correspond to the $MD'2018$ and $JH'2013$ set 2 gluon density functions, respectively.

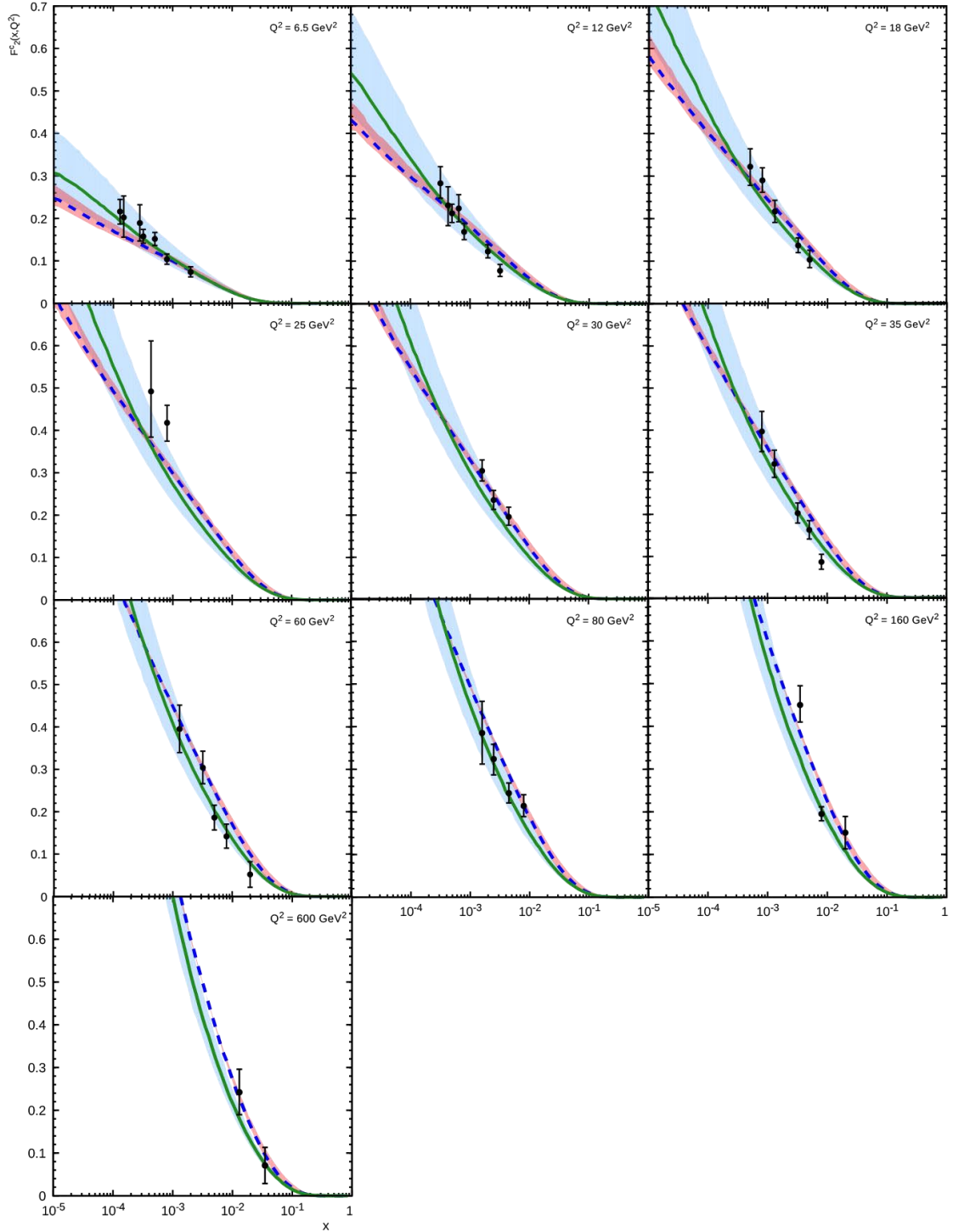


Figure 4: The charm contribution to the proton structure function $F_2(x, Q^2)$ as a function of x calculated at different Q^2 . Notation of histograms is the same as in Fig. 2. The experimental data are from ZEUS [54] and H1 [55].

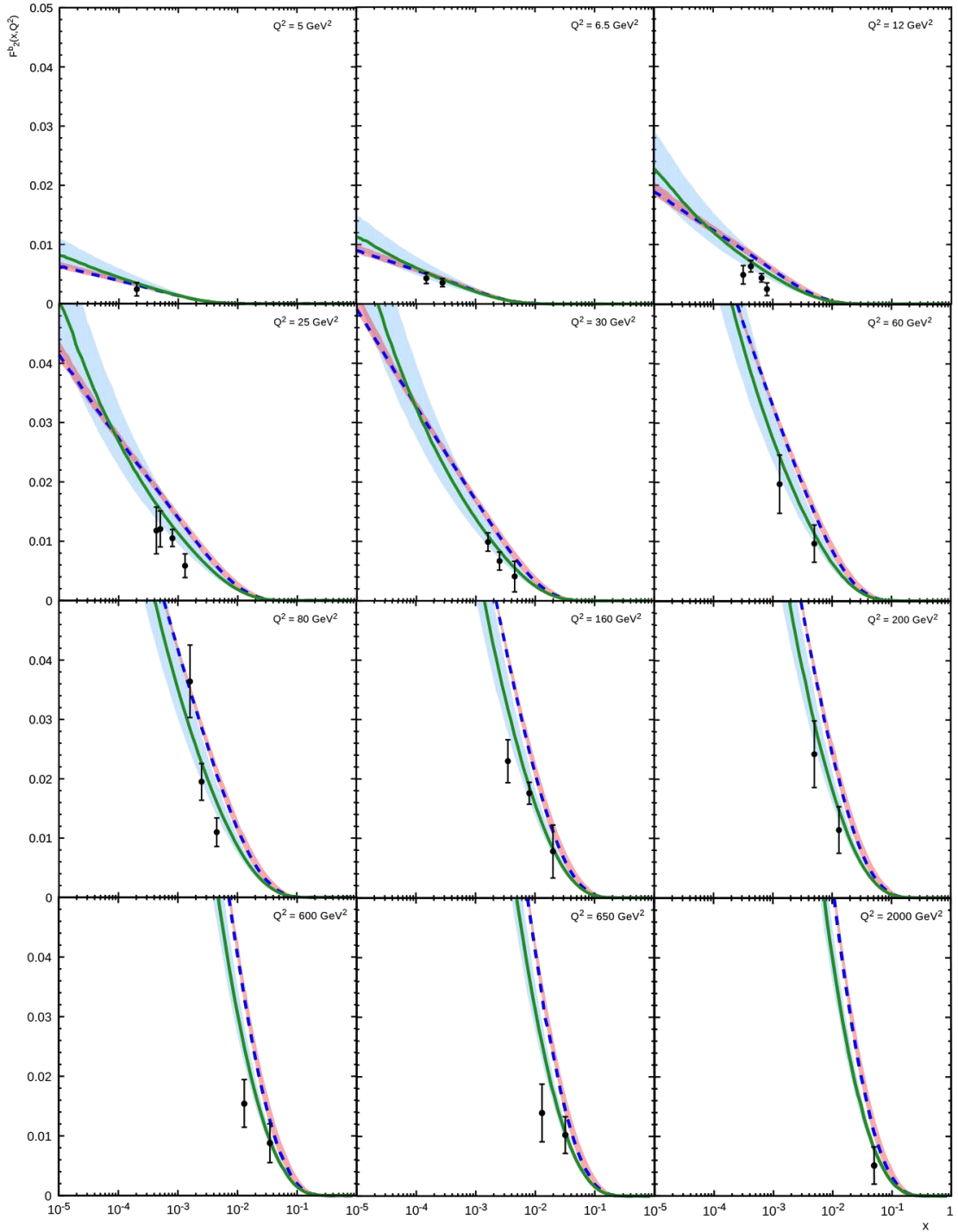


Figure 5: The beauty contribution to the proton structure function $F_2(x, Q^2)$ as a function of x calculated at different Q^2 . Notation of histograms is the same as in Fig. 2. The experimental data are from ZEUS [54] and H1 [56].

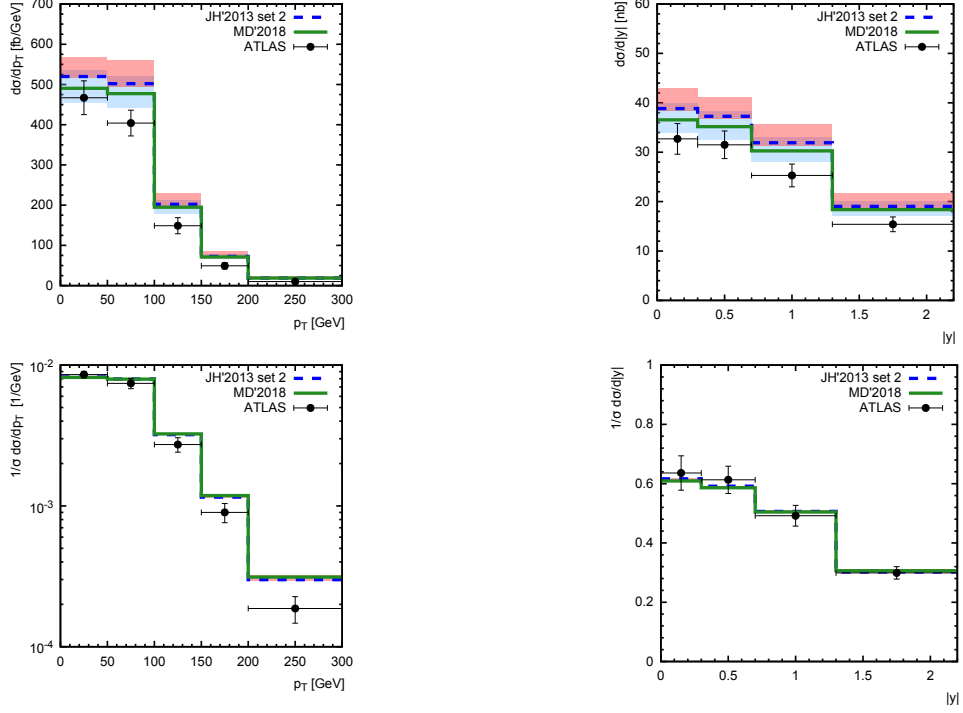


Figure 6: The differential cross sections of inclusive t -channel single top production at $\sqrt{s} = 8$ TeV as a functions of top quark transverse momentum and rapidity. Notation of histograms is the same as in Fig. 2. The experimental data are from ATLAS [58].

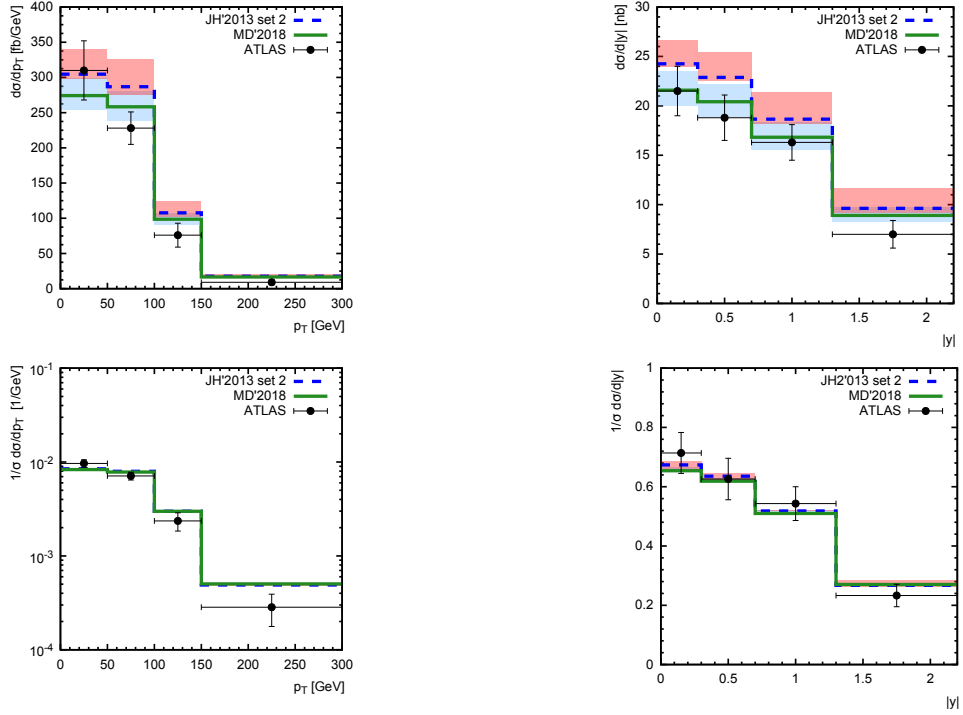


Figure 7: The differential cross sections of inclusive t -channel single anti-top production at $\sqrt{s} = 8$ TeV as a functions of \bar{t} quark transverse momentum and rapidity. Notation of histograms is the same as in Fig. 2. The experimental data are from ATLAS [58].

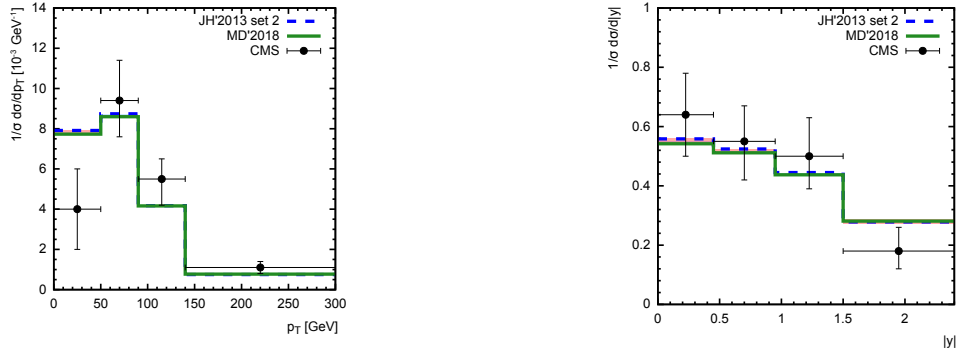


Figure 8: The normalized differential cross sections of inclusive t -channel single top production at $\sqrt{s} = 8$ TeV as a functions of top quark transverse momentum and rapidity. Notation of histograms is the same as in Fig. 2. The experimental data are from CMS [57].

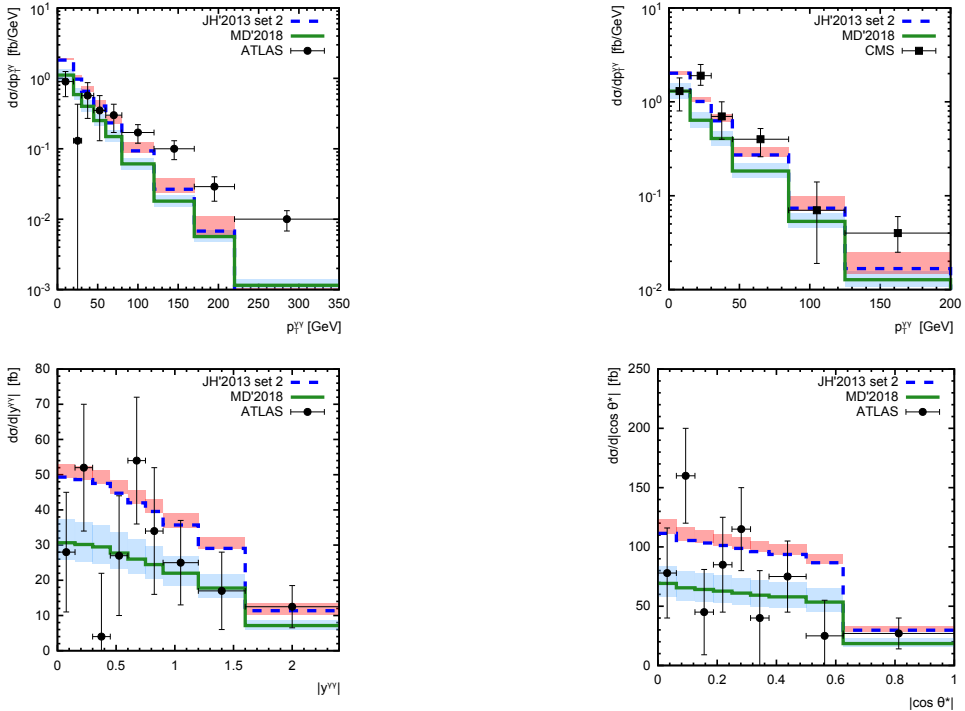


Figure 9: The differential cross sections of inclusive Higgs boson production (in the diphoton decay mode) at $\sqrt{s} = 13$ TeV as functions of diphoton pair transverse momentum $p_T^{\gamma\gamma}$, rapidity $|y^{\gamma\gamma}|$ and photon helicity angle $\cos \theta^*$ in the Collins-Soper frame. Notation of histograms is the same as in Fig. 2. The experimental data are from CMS [65] and ATLAS [67].

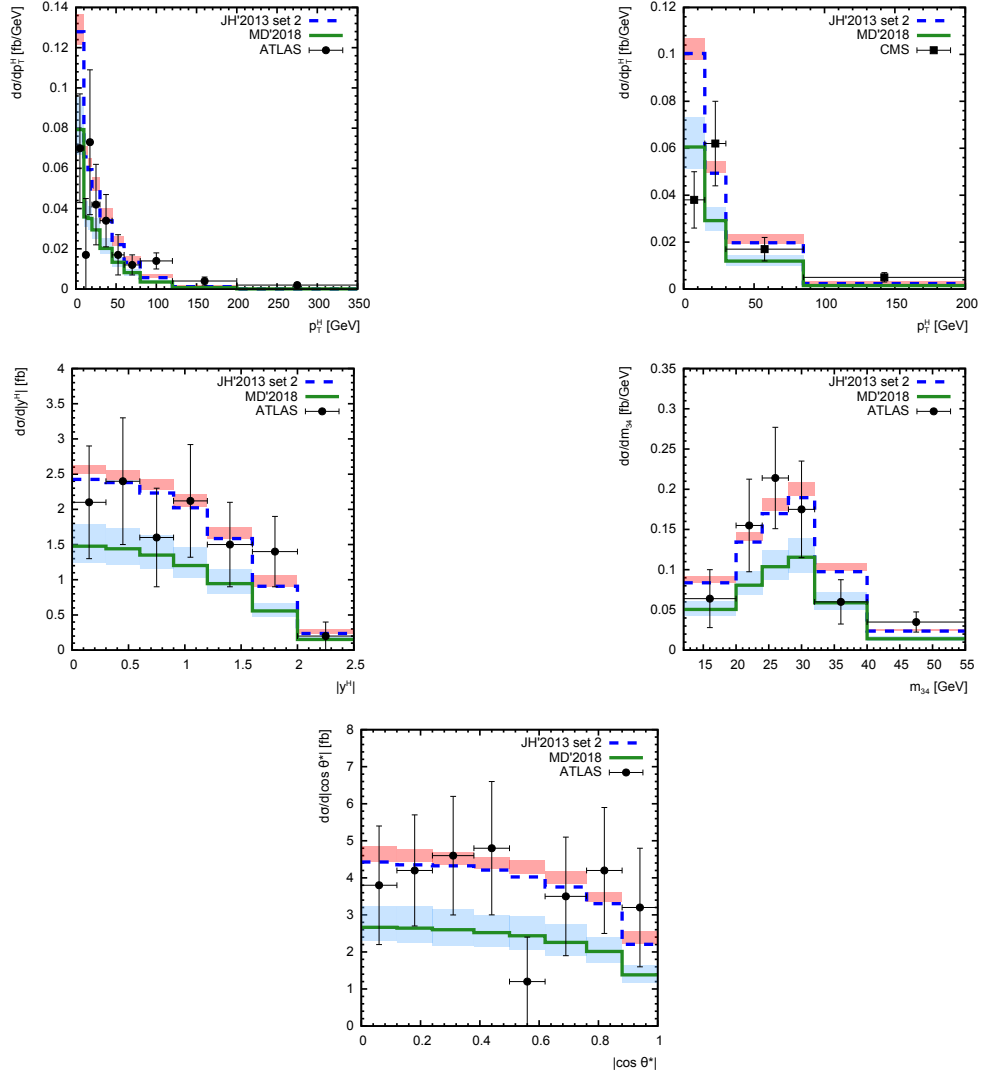


Figure 10: The differential cross sections of inclusive Higgs production (in the $H \rightarrow ZZ^* \rightarrow 4l$ decay mode) at $\sqrt{s} = 13$ TeV as functions of Higgs boson transverse momentum p_T^H , rapidity $|y^H|$, leading lepton pair decay angle $|\cos \theta^*|$ (in the Collins-Soper frame) and invariant mass m_{34} of the subleading lepton pair. Notation of histograms is the same as in Fig. 2. The experimental data are from CMS [66] and ATLAS [68].