

One-loop effects on MSSM parameter determination via chargino production at the LC

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Abstract

At a future linear collider, very precise measurements, typically with errors of $< 1\%$, are expected to be achievable. Such an accuracy yields sensitivity to quantum corrections, which therefore must be incorporated into theoretical calculations in order to determine the underlying new physics parameters from linear collider measurements. In the context of the chargino–neutralino sector of the minimal supersymmetric standard model, this involves fitting one-loop predictions to prospective measurements of cross sections, forward-backward asymmetries and the accessible chargino and neutralino masses. Taking recent results from LHC SUSY and Higgs searches into account, we consider three phenomenological scenarios, each displaying characteristic features. Our analysis demonstrates how an accurate determination of the desired parameters is possible, and could additionally provide access to the stop masses and mixing angle.

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1 Introduction

A linear collider (LC) [1–5] will be an ideal environment for high precision studies of physics beyond the standard model (BSM). A particularly well-motivated description of BSM physics is provided by the minimal supersymmetric standard model (MSSM), offering the lightest supersymmetric particle, often the lightest neutralino, as a candidate to explain the evidence for dark matter in the universe [6, 7]. Naturalness arguments (see e.g. ref. [8]) support the possibility that higgsino-like charginos and neutralinos are light, as also predicted by GUT motivated SUSY models [9]. Further, due to the challenges involved in detecting electroweakinos at the LHC, current bounds from ATLAS and CMS only exclude small regions of parameter space, see e.g. refs. [10, 11]. Charginos and neutralinos could therefore be within reach of a first stage linear collider.

One approach to determine the fundamental MSSM parameters is to consider constrained models such as the constrained minimal supersymmetric standard model (CMSSM), and perform a global fit of this reduced set of parameters to all relevant experimental results available, see e.g. ref. [12]. On the other hand, in order to precisely determine the nature of the underlying SUSY model, we wish to determine the fundamental parameters in the most model-independent way possible. The determination of the $U(1)$ parameter M_1 , the $SU(2)$ parameter M_2 , the higgsino parameter μ and $\tan\beta$, the ratio of the vacuum expectation values of the two neutral Higgs doublet fields, at the percent level via chargino and neutralino pair-production has been shown to be possible at LO (see ref. [13] and references therein). However, due to the expected high precision of mass and coupling measurements at the LC, as well as the fact that one-loop effects in the MSSM may be sizeable, higher order effects have to be considered. Taking these corrections into account additional MSSM parameters become relevant, such as the masses of the stops and sleptons, which, like the electroweakinos, are also weakly constrained by the LHC.

In this paper we demonstrate that the determination of the fundamental parameters of the chargino and neutralino sector at the LC would be possible, even on including the complications arising due to higher order effects. This requires the calculation of the next-to-leading order (NLO) corrections to the cross-section (σ) and forward-backward asymmetry (A_{FB}) for chargino production, as well as to the chargino and neutralino masses. A number of next-to-leading order (NLO) calculations of chargino and neutralino pair production at the LC can be found in the literature [14–18]. We perform our calculations in the on-shell (OS) scheme such that, as far as possible, the mass parameters can be interpreted as the physical masses. Recent work

on the OS renormalization of the chargino-neutralino sector can be found in refs. [18–24].

By fitting these loop corrected predictions to the projected experimental results, we show that it would be possible to extract the fundamental parameters of the MSSM Lagrangian. However due to the greater number of parameters, performing the fit is more involved than for the LO analysis. Choosing three potential MSSM scenarios, we assess the impact of the loop corrections and the feasibility of such an extraction in each. We further investigate the impact of obtaining masses of the charginos and neutralinos from threshold scans rather than the continuum (see ref. [1]) on the resulting accuracy of the parameters obtained from the fit.

The paper is organised as follows. In sec. 2 we introduce the process studied and define necessary notation. We then provide details of the calculation of the loop corrections in sec. 3, including details of the renormalization scheme used. In sec. 4 we further discuss the method employed in order to fit to the MSSM parameters, define the scenarios considered, and present our results. Finally in sec. 5 we discuss the implications of the results of the fits.

2 Process studied and tree-level relations

In this paper we study the determination of the fundamental parameters in the chargino–neutralino sector of the MSSM, via chargino production at a LC. The charginos, $\tilde{\chi}^\pm$, and neutralinos, $\tilde{\chi}^0$, are the mass eigenstates of the gauginos and higgsinos, as seen from the relevant part of the MSSM Lagrangian [25],

$$\begin{aligned} \mathcal{L}_{\tilde{\chi}} = & \overline{\tilde{\chi}_i^-} (\not{p} \delta_{ij} - P_L (U^* X V^\dagger)_{ij} - P_R (V X^\dagger U^T)_{ij}) \tilde{\chi}_j^- \\ & + \frac{1}{2} \overline{\tilde{\chi}_i^0} (\not{p} \delta_{ij} - P_L (N^* Y N^\dagger)_{ij} - P_R (N Y^\dagger N^T)_{ij}) \tilde{\chi}_j^0, \end{aligned} \quad (1)$$

where $P_{L/R} = 1/2(1 \mp \gamma_5)$. The mass matrix for the charginos is given by

$$X = \begin{pmatrix} M_2 & \sqrt{2} M_W s_\beta \\ \sqrt{2} M_W c_\beta & \mu \end{pmatrix}, \quad (2)$$

where $s_\beta/c_\beta \equiv \sin \beta / \cos \beta$, and M_W is the mass of the W boson. This matrix is diagonalised via the bi-unitary transformation $\mathbf{M}_{\tilde{\chi}^+} = U^* X V^\dagger$, where U and V are complex unitary matrices. The mass matrix for the neutralinos in

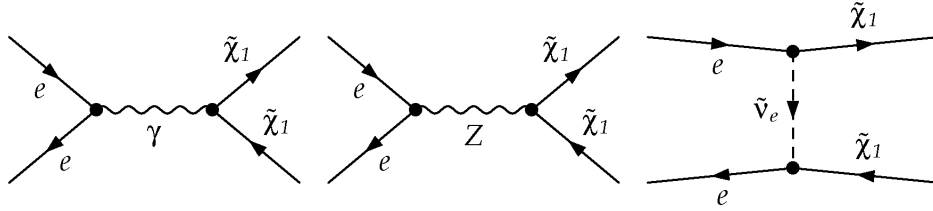


Figure 1: Tree-level diagrams for the production of charginos $\tilde{\chi}_1^+$ and $\tilde{\chi}_1^-$ at the LC.

the $(\tilde{B}, \tilde{W}, \tilde{H}_1, \tilde{H}_2)$ basis is given by

$$Y = \begin{pmatrix} M_1 & 0 & -M_Z c_\beta s_W & M_Z s_\beta s_W \\ 0 & M_2 & M_Z c_\beta c_W & -M_Z s_\beta c_W \\ -M_Z c_\beta s_W & M_Z c_\beta c_W & 0 & -\mu \\ M_Z s_\beta s_W & -M_Z s_\beta c_W & -\mu & 0 \end{pmatrix}, \quad (3)$$

where $s_W(c_W)$ is the sin(cos) of the weak mixing angle θ_W . Since Y is complex symmetric, its diagonalisation requires only one unitary matrix N , via $\mathbf{M}_{\tilde{\chi}^0} = N^* Y N^\dagger$.

As described in detail in sec. 4, in addition to the experimental determination of the masses of the charginos and neutralinos the parameter determination relies on the measurement of the polarised cross-section for the pair production of charginos, $\tilde{\chi}_1^\pm$,

$$\sigma(e^+e^- \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^-), \quad (4)$$

and the forward-backward asymmetry defined by,

$$A_{FB} = \frac{\sigma(\cos\theta > 0) - \sigma(\cos\theta < 0)}{\sigma(\cos\theta > 0) + \sigma(\cos\theta < 0)}, \quad (5)$$

for the unpolarised cross-section, where θ is the angle of the momentum of the chargino $\tilde{\chi}_1^-$ with respect to the momentum of the incoming electron e^- . Neglecting the electron-Higgs couplings, the relevant process occurs at leading order via three diagrams, as seen in fig. 1.

The transition matrix element can be written as [26],

$$\mathcal{M}_{\alpha\beta}(e^+e^- \rightarrow \tilde{\chi}_i^+ \tilde{\chi}_j^-) = \frac{e}{s} Q_{\alpha\beta} [\bar{v}(e^+) \gamma_\mu P_\alpha u(e^-)] [\bar{u}(\tilde{\chi}_j^-) \gamma^\mu P_\beta v(\tilde{\chi}_i^+)], \quad (6)$$

where $Q_{\alpha\beta}$ denotes the bilinear charges, $\alpha = L, R$ refers to the chirality of the e^+e^- current and $\beta = L, R$ to that of the $\tilde{\chi}_i^+ \tilde{\chi}_j^-$ current. The summation

over α and β is implied. In our notation, the bilinear charges are comprised of the propagators and couplings

$$\begin{aligned}
Q_{LL} &= C_{\tilde{\chi}_i^+ \tilde{\chi}_j^- \gamma}^L - D_Z G_L C_{\tilde{\chi}_i^+ \tilde{\chi}_j^- Z}^L, \\
Q_{RL} &= C_{\tilde{\chi}_i^+ \tilde{\chi}_j^- \gamma}^L - D_Z G_R C_{\tilde{\chi}_i^+ \tilde{\chi}_j^- Z}^L, \\
Q_{LR} &= C_{\tilde{\chi}_i^+ \tilde{\chi}_j^- \gamma}^R + D_Z G_L \left(C_{\tilde{\chi}_i^+ \tilde{\chi}_j^- Z}^R \right)^* + \frac{i}{2e} D_{\tilde{\nu}} \left(C_{\tilde{\nu}_e e^+ \tilde{\chi}_i^-}^R \right)^* C_{\tilde{\nu}_e e^+ \tilde{\chi}_j^-}^R, \\
Q_{RR} &= C_{\tilde{\chi}_i^+ \tilde{\chi}_j^- \gamma}^R + D_Z G_R \left(C_{\tilde{\chi}_i^+ \tilde{\chi}_j^- Z}^R \right)^*, \tag{7}
\end{aligned}$$

for which the required MSSM couplings for the $\tilde{\chi}_i^+ \tilde{\chi}_j^- \gamma$, $\tilde{\chi}_i^+ \tilde{\chi}_j^- Z$ and $e \tilde{\nu}_e \tilde{\chi}_i^+$ vertices are given by

$$\begin{aligned}
C_{\tilde{\chi}_i^+ \tilde{\chi}_j^- \gamma}^{L/R} &= ie \delta_{ij}, \\
C_{\tilde{\chi}_i^+ \tilde{\chi}_j^- Z}^L &= -\frac{ie}{c_W s_W} \left(s_W^2 \delta_{ij} - U_{j1}^* U_{i1} - \frac{1}{2} U_{j2}^* U_{i2} \right), \\
C_{\tilde{\chi}_i^+ \tilde{\chi}_j^- Z}^R &= C_{\tilde{\chi}_i^+ \tilde{\chi}_j^- Z}^L (U \rightarrow V^*), \\
C_{\tilde{\nu}_e e^+ \tilde{\chi}_i^-}^R &= -\frac{ie}{s_W} V_{i1}, \tag{8}
\end{aligned}$$

and G_L , G_R , D_Z and $D_{\tilde{\nu}}$ are defined via

$$\begin{aligned}
G_L &= \frac{s_W^2 - \frac{1}{2}}{s_W c_W}, & G_R &= \frac{s_W}{c_W}, \\
D_Z &= \frac{s}{s - M_Z^2}, & D_{\tilde{\nu}} &= \frac{s}{t - m_{\tilde{\nu}}^2}. \tag{9}
\end{aligned}$$

In the equations above, e denotes the electric charge, m_e and M_Z are the masses of the electron and Z boson. D_Z and $D_{\tilde{\nu}}$ refer to the propagators of the Z boson and sneutrino (of mass $m_{\tilde{\nu}}$), in terms of the Mandelstam variables s and t .

Therefore in order to express the transition matrix element eq. (6) at leading order, the necessary MSSM parameters are M_2 , μ , $\tan \beta$ and $m_{\tilde{\nu}}$. However, the expected accuracy of the measurements at the linear collider is such that one-loop corrections become relevant, and we shall see in the following section that at higher orders eq. (6) depends on many additional MSSM parameters.

3 NLO contributions and renormalization

We have calculated the full one-loop corrections to the forward-backward asymmetry for process $e^+ e^- \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^-$, within the complex MSSM; the corre-

sponding corrections to the cross section were calculated in ref. [18]. Examples for the contributing self-energy, vertex and box diagrams are shown in fig. 2. As in ref. [18], for the calculation we have used the program `FeynArts` [27–31], which allowed an automated generation of the Feynman diagrams and amplitudes. Together with the packages `FormCalc` [32–34] and `LoopTools` [32] we derived the final matrix elements and loop integrals. We assume a unit CKM matrix. We regularise using dimensional reduction [35–37], which ensures that SUSY is preserved, via the implementation described in refs. [32, 38].

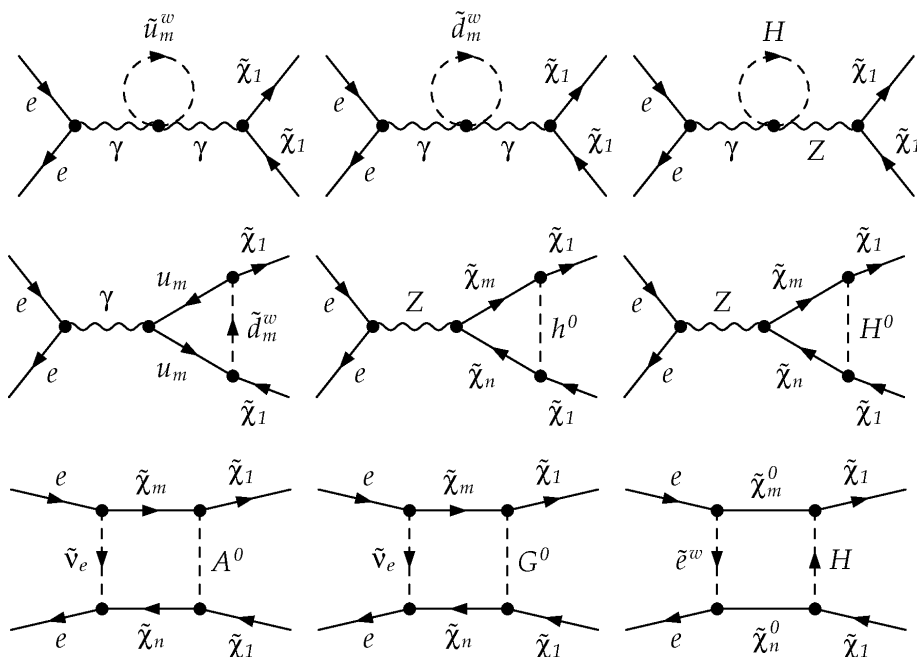


Figure 2: Examples of one-loop self-energy (upper), vertex (middle) and box (lower) diagrams for the production of charginos $\tilde{\chi}_1^+$ and $\tilde{\chi}_1^-$ at the LC.

A number of one-loop calculations in the gaugino-higgsino sector can be found in the literature, mainly in the CP-conserving MSSM [14, 39–46], but some of which apply a renormalization scheme that is also applicable for complex parameters [14, 45]. CP-odd observables have also been calculated at the one-loop level, for instance in refs. [48–50], but no dedicated renormalization scheme was required in these cases as the observables studied were UV-finite. Since we intend to extend the current study to the case of complex parameters, we follow the approach of refs. [18, 20] closely, where a dedicated on-shell renormalization scheme for the chargino and neutralino sector of the

MSSM with complex parameters was developed. In the following we will therefore only briefly discuss the parameter renormalization of the chargino and neutralino sector, relevant for the definitions of the parameters at loop level, and for further details about the chargino field renormalization and the renormalization of other sectors refer the reader to refs. [18, 20, 21, 24].

The mass matrix in the chargino sector, eq. (2), is renormalized via

$$X \rightarrow X + \delta X, \quad (10)$$

where δX is defined by

$$\delta X = \begin{pmatrix} \delta M_2 & \sqrt{2}\delta(M_W s_\beta) \\ \sqrt{2}\delta(M_W c_\beta) & \delta\mu \end{pmatrix}, \quad (11)$$

and contains the renormalization constants δM_2 and $\delta\mu$, as well as renormalization constants (RCs) from other sectors, δc_β , δs_β (which can be expressed in terms of $\delta \tan \beta$), and δM_W , defined in ref. [18]. The neutralino mass matrix, eq. (3), is similarly renormalized via

$$Y \rightarrow Y + \delta Y, \quad (12)$$

where δY is defined analogously to δX in eq. (11) and contains the additional RC δM_1 , cf. eq. (3).

Following e.g. ref. [20], δM_1 , δM_2 and $\delta\mu$ are determined by choosing three out of the total six physical masses of the charginos and neutralinos to be on-shell, i.e. the tree-level masses, $m_{\tilde{\chi}_i}$, coincide with the one-loop renormalized masses, $M_{\tilde{\chi}_i} = m_{\tilde{\chi}_i} + \Delta m_{\tilde{\chi}_i}$,

$$\begin{aligned} \Delta m_{\tilde{\chi}_i} &\equiv -\frac{m_{\tilde{\chi}_i}}{2} \text{Re}[\hat{\Sigma}_{ii}^L(m_{\tilde{\chi}_i}^2) + \hat{\Sigma}_{ii}^R(m_{\tilde{\chi}_i}^2)] - \frac{1}{2} \text{Re}[\hat{\Sigma}_{ii}^{SL}(m_{\tilde{\chi}_i}^2) + \hat{\Sigma}_{ii}^{SR}(m_{\tilde{\chi}_i}^2)] \\ &= 0. \end{aligned} \quad (13)$$

We define the coefficients $\Sigma_{ij}^{L/R}(p^2)$ and $\Sigma_{ij}^{SL/SR}(p^2)$ of the self energy via

$$\Sigma_{ij}(p^2) = \not{P}_L \Sigma_{ij}^L(p^2) + \not{P}_R \Sigma_{ij}^R(p^2) + P_L \Sigma_{ij}^{SL}(p^2) + P_R \Sigma_{ij}^{SR}(p^2), \quad (14)$$

and define the left and right handed vector and scalar coefficients of the renormalized self-energy analogously via $\hat{\Sigma}_{ij}^{L/R}(p^2)$ and $\hat{\Sigma}_{ij}^{SL/SR}(p^2)$ respectively.

As stated earlier, we consider the parameter renormalization as for the complex MSSM, such that our setup is easily adaptable for future extensions. In ref. [18, 21], it was shown that in the CP violating case, the 1-loop corrections to the phases of M_1 and μ , i.e. ϕ_{M_1} and ϕ_μ respectively¹ are UV

¹ We adopt the convention that M_2 is real.

finite, and it is argued that these phases can therefore be left unrenormalized. Adopting this approach, one can determine expressions for $\delta|M_1|$, $\delta|M_2|$ and $\delta|\mu|$, depending on which three physical masses are chosen to be on-shell. As we have two external charginos, and in order to easily extend our setup to the case of $\tilde{\chi}_1^+ \tilde{\chi}_2^-$ production, we assume the NCC scheme with $\tilde{\chi}_1^0$, $\tilde{\chi}_1^\pm$ and $\tilde{\chi}_2^\pm$ on-shell [18, 20–22]. Note that in choosing a scheme, it is desirable that the on-shell particles should contain significant bino, wino and higgsino components, in order that the M_1 , M_2 and μ parameters are accessible [18, 20–22]. For the above choice, these conditions are satisfied for all the scenarios defined in sec. 4, in which the lightest neutralino always has a sizeable bino-like component. The parameters in question of the chargino mass matrix can then be renormalized via expressions given in refs. [18, 21, 24], which we list here for completeness,

$$\begin{aligned} \delta|M_1| = & - \frac{1}{\text{Re}(e^{-i\phi_{M_1}} N_{i1}^2) F} \\ & \left((2\text{Re}(e^{-i\phi_\mu} N_{i3} N_{i4}) \text{Re}(U_{j1} V_{j1}) + \text{Re} N_{i2}^2 \text{Re}(e^{-i\phi_\mu} U_{j2} V_{j2})) C_k \right. \\ & + (\text{Re}(U_{j1} V_{j1}) \text{Re}(e^{-i\phi_\mu} U_{k2} V_{k2}) - \text{Re}(e^{-i\phi_\mu} U_{j2} V_{j2}) \text{Re}(U_{k1} V_{k1})) N_i \\ & \left. - (\text{Re} N_{i2}^2 \text{Re}(e^{-i\phi_\mu} U_{k2} V_{k2}) + 2\text{Re}(e^{-i\phi_\mu} N_{i3} N_{i4}) \text{Re}(U_{k1} V_{k1})) C_j \right), \end{aligned} \quad (15)$$

$$\delta|M_2| = \frac{1}{F} \left(\text{Re}(e^{-i\phi_\mu} U_{j2} V_{j2}) C_k - \text{Re}(e^{-i\phi_\mu} U_{k2} V_{k2}) C_j \right), \quad (16)$$

$$\delta|\mu| = - \frac{1}{F} \left(\text{Re}(U_{j1} V_{j1}) C_k - \text{Re}(U_{k1} V_{k1}) C_j \right), \quad (17)$$

where F , C_i and N_i are defined by

$$F = 2 \left(\text{Re}(U_{k1} V_{k1}) \text{Re}(e^{-i\phi_\mu} U_{j2} V_{j2}) - \text{Re}(U_{j1} V_{j1}) \text{Re}(e^{-i\phi_\mu} U_{k2} V_{k2}) \right), \quad (18)$$

$$\begin{aligned} C_i = & \text{Re} \left[m_{\tilde{\chi}_i^+} [\Sigma_{\pm,ii}^L(m_{\tilde{\chi}_i^+}^2) + \Sigma_{\pm,ii}^R(m_{\tilde{\chi}_i^+}^2)] + \Sigma_{\pm,ii}^{SL}(m_{\tilde{\chi}_i^+}^2) + \Sigma_{\pm,ii}^{SR}(m_{\tilde{\chi}_i^+}^2) \right] \\ & - \sum_{\substack{j=1,2 \\ k=1,2}} 2\delta X_{jk} \text{Re}(U_{ij} V_{ik}), \end{aligned} \quad (19)$$

$$\begin{aligned} N_i = & \text{Re} \left[m_{\tilde{\chi}_i^0} [\Sigma_{0,ii}^L(m_{\tilde{\chi}_i^0}^2) + \Sigma_{0,ii}^R(m_{\tilde{\chi}_i^0}^2)] + \Sigma_{0,ii}^{SL}(m_{\tilde{\chi}_i^0}^2) + \Sigma_{0,ii}^{SR}(m_{\tilde{\chi}_i^0}^2) \right] \\ & - \sum_{\substack{j=1,2 \\ k=3,4}} 4\delta Y_{jk} \text{Re}(N_{ij} N_{ik}), \end{aligned} \quad (20)$$

and the subscripts \pm and 0 identify the coefficients of the chargino and neutralino self-energy respectively.

Finite results for the process of interest at one-loop are obtained by adding the counterterm diagrams shown in fig. 3. Although **FeynArts** generates

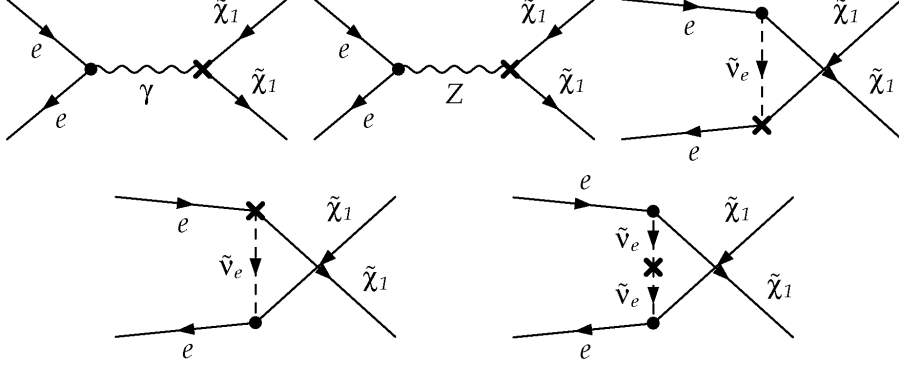


Figure 3: Counterterm diagrams in the MSSM for the production of charginos $\tilde{\chi}_1^+$ and $\tilde{\chi}_1^-$ at the LC.

these diagrams, expressions for the counterterms which renormalize the couplings defined at tree-level in eq. (6), calculated in ref. [18], are required as input, and therefore, again for completeness, we provide expressions for these explicitly. For the $\gamma\tilde{\chi}_i^+\tilde{\chi}_j^-$, $Z\tilde{\chi}_i^+\tilde{\chi}_j^-$ and $e\tilde{\nu}_e\tilde{\chi}_i^+$ vertices, these can be expressed as follows,

$$\begin{aligned} \delta C_{\tilde{\chi}_i^+\tilde{\chi}_j^-\gamma}^L &= C_{\tilde{\chi}_i^+\tilde{\chi}_j^-\gamma}^L \left(\delta Z_e + \frac{\delta Z_{\gamma\gamma}}{2} \right) + C_{\tilde{\chi}_i^+\tilde{\chi}_j^-Z}^L \frac{\delta Z_{Z\gamma}}{2} + \frac{ie}{2} (\delta Z_{\pm,ij}^L + \delta \bar{Z}_{\pm,ij}^L), \\ \delta C_{\tilde{\chi}_i^+\tilde{\chi}_j^-Z}^L &= C_{\tilde{\chi}_i^+\tilde{\chi}_j^-Z}^L \left(\delta Z_e - \frac{\delta c_W}{c_W} - \frac{\delta s_W}{s_W} + \frac{\delta Z_{ZZ}}{2} \right) + C_{\tilde{\chi}_i^+\tilde{\chi}_j^-\gamma}^L \frac{\delta Z_{\gamma Z}}{2} \\ &\quad - 2ie \frac{\delta s_W}{c_W} \delta_{ij} + \frac{1}{2} \sum_{n=1,2} \left(\delta C_{\tilde{\chi}_i^+\tilde{\chi}_n^-Z}^L Z_{\pm,nj}^L + C_{\tilde{\chi}_n^+\tilde{\chi}_j^-Z}^L \delta \bar{Z}_{\pm,in}^L \right), \end{aligned} \quad (21)$$

where the analogous right-handed parts are obtained by the replacement $L \rightarrow R$, and

$$\begin{aligned} \delta C_{\tilde{\nu}_e e^+ \tilde{\chi}_i^-}^R &= C_{\tilde{\nu}_e e^+ \tilde{\chi}_i^-}^R \left(\delta Z_e - \frac{\delta s_W}{s_W} + \frac{1}{2} (\delta Z_{\tilde{\nu}_e} + \delta Z_e^{L*}) \right) \\ &\quad + \frac{1}{2} \left(C_{\tilde{\nu}_e e^+ \tilde{\chi}_1^-}^R \delta Z_{\pm,1i}^R + C_{\tilde{\nu}_e e^+ \tilde{\chi}_2^-}^R \delta Z_{\pm,2i}^R \right). \end{aligned} \quad (22)$$

Note that the renormalization constants of the SM fields, i.e. Z_{VV} ($V = \gamma, Z$) and δZ_e^L for the vector bosons and electron, and parameters, i.e. δZ_e and

$\delta c_W(s_W)$ for the electric charge and $\cos(\sin)$ of the weak mixing angle respectively, can be found in ref. [18]. The renormalization for the chargino fields is performed in the most general manner, making use of separate RCs for the incoming and outgoing fields, i.e. coefficients $\delta Z_{\pm,ij}^{L/R}$ and $\delta \bar{Z}_{\pm,ij}^{L/R}$ respectively for left and right-handed charginos as given in ref. [18]. Finally, the counterterm for the sneutrino self energy takes the form

$$\delta C_{\tilde{\nu}_i \tilde{\nu}_j} = i\delta_{ij} \left(\frac{1}{2}(\delta Z_{\tilde{\nu}_i} + \delta Z_{\tilde{\nu}_i}^*)p^2 - \delta m_{\tilde{\nu}_i}^2 - \frac{m_{\tilde{\nu}_i}^2}{2}(\delta Z_{\tilde{\nu}_i} + \delta Z_{\tilde{\nu}_i}^*) \right), \quad (23)$$

for $\tilde{\nu}_i = \tilde{\nu}_e, \tilde{\nu}_\mu, \tilde{\nu}_\tau$, where the sneutrino field and mass RCs, $\delta Z_{\tilde{\nu}_i}^*$ and $\delta m_{\tilde{\nu}_i}$, are also defined following ref. [18].

Initial and final state soft radiation must also be included to obtain an infra-red finite result as the incoming and outgoing particles are charged, and this is done as described in detail in ref. [18], using the phase-space slicing method to define the singular soft and collinear contributions in the regions $E < \Delta E$ and $\theta < \Delta\theta$ respectively. In the soft and collinear limit, the results are regularised using electron and photon masses, respectively, and factorised into analytically integrable expressions proportional to the tree-level cross-section $\sigma^{\text{tree}}(e^+e^- \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^-)$. However the result is cut-off dependent (i.e. on ΔE and $\Delta\theta$), and removing this dependence requires a calculation of the cross section for the three body final state, excluding the soft and collinear regions, which we perform using `FeynArts` and `FormCalc`. We further require that soft photon radiation is included in the cross-section obtained from `FormCalc`. Finally we obtain a complete IR safe and cut-off independent result by adding the collinear contribution, which is calculated following the procedure outlined in ref. [14].

4 Fit strategy and numerical results

4.1 Obtaining MSSM parameters from the fit

With the loop corrections calculated as in section 3, we can determine the fundamental parameters of the MSSM at NLO. From now on, we will restrict our study to the case of real parameters. In the chargino and neutralino sectors there are four real parameters, see sec. 2, which we fit to,

$$M_1, \quad M_2, \quad \mu, \quad \tan\beta. \quad (24)$$

We additionally fit to the sneutrino mass, as this enters at tree level and will therefore significantly affect cross sections and forward-backward asymmetries. However in those scenarios where the sneutrino would already have

been observed at the LC, its mass is assumed to be known. At the loop level, a large number of MSSM parameters will contribute. Depending on the scenario, only limited knowledge about some of these may be available. In particular LHC data may only provide limited information about the parameters of the stop sector, and direct production at the LC might not be possible. However, our analysis also offers good sensitivity to these parameters at the LC, as stops could significantly contribute to chargino/neutralino observables at NLO.

At the LC, the accessible masses are expected to be measured with high precision using different methods [1]. In the following we adopt the experimental precision which could be achieved using the threshold scan method, however we also investigate how the fit precision would change if the masses were obtained from the continuum. In case of the cross sections, the experimental uncertainty is dominated by the statistical uncertainty [51],

$$\frac{\Delta\sigma}{\sigma} = \frac{\sqrt{S+B}}{S}, \quad (25)$$

where S and B are the signal and background contributions, respectively. In addition, we assume that the statistical uncertainties for the cross sections correspond to an integrated luminosity of $\mathcal{L} = 200 \text{ fb}^{-1}$ per polarisation assuming the efficiency of $\epsilon = 15\%$, which includes branching ratios for semileptonic final states and a selection efficiency of 50% [51]. Similarly, for the forward-backward asymmetry we have

$$\delta A_{FB}^{\text{stat}} = \sqrt{\frac{1 - A_{FB}^2}{N}}, \quad (26)$$

and the total number of events $N = N_+ + N_-$ [51].

In order to estimate the theoretical uncertainty on the masses, cross-sections and forward backward asymmetries, we consider the size of possible effects due either to neglected higher order corrections or to unknown MSSM parameters not included in the fit. NNLO corrections are an important source of theoretical uncertainty, however, at present, corrections of this kind are only known for chargino and neutralino masses, for which the leading SUSY-QCD NNLO corrections were calculated in ref. [46]. Based on these results we estimate the uncertainty on the masses due to NNLO corrections to be of the order of 0.5 GeV, i.e. comparable to the expected experimental uncertainty. Note that the masses chosen on-shell are assigned no theoretical uncertainty. We further neglect the currently unknown uncertainties arising due to NNLO corrections to the cross-sections and forward

backward asymmetries, assuming that in the future NNLO results for these could be incorporated. However, we do include the additional uncertainty arising due to any unknown MSSM parameters which are not included in the fit, dominated by the contribution from the heavy pseudoscalar Higgs boson mass m_{A^0} . We perform a multi-dimensional χ^2 fit using `Minuit` [52, 53]

$$\chi^2 = \sum_i \left| \frac{\mathcal{O}_i - \bar{\mathcal{O}}_i}{\delta\mathcal{O}_i} \right|^2, \quad (27)$$

where the sum runs over the input observables \mathcal{O}_i , depending on the scenario, with their corresponding experimental uncertainties $\delta\mathcal{O}_i$.

4.2 Scenarios studied and motivation

We carry out the fit for three scenarios, S1, S2 and S3, shown in tab. 1, chosen in order to realistically assess the sensitivity to the desired parameters in a variety of possible situations. Due to the current status of direct LHC searches [54, 55], in all scenarios we require heavy first and second generation squarks and gluinos, while the stop sector is assumed to be relatively light.² In S1 and S2 we take the masses of the stops, $m_{\tilde{t}_1}$ and $m_{\tilde{t}_2}$, to be 400 GeV and 800 GeV respectively, and the mixing angle to be $\cos\theta_t = 0$. The sbottom sector is then obtained by defining $m_{\tilde{b}_1} = 400$ GeV and $\cos\theta_b = 0$. On the other hand in S3, in order to obtain $m_h = 125$ GeV, calculated using `FeynHiggs 2.9.1` [56–59], such that it is compatible with the recent Higgs results from the LHC [60, 61], the stop sector parameters are chosen to be $m_{u_3} = 450$ GeV, $m_{q_3} = 1500$ GeV and $A_t = -1850$ GeV, ensuring large mixing between the stops, such that $\cos\theta_t = 0.148$. The sbottom sector is then obtained by defining $m_{\tilde{b}_1} = 450$ GeV and $\cos\theta_b = 0$. In fig. 4 the mass corrections for neutralinos $\tilde{\chi}_2^0$ and $\tilde{\chi}_3^0$ are seen to be sensitive to the stop mixing angle for each of the studied scenarios.

As a result of indirect limits (checked using `micrOmegas 2.4.1` [62, 63]), we have chosen mixed gaugino higgsino scenarios favoured by the relic density measurements [64] and relatively high pseudoscalar Higgs masses in light of flavour physics constraints, e.g. due to the dependence of the branching ratio $\mathcal{B}(b \rightarrow s\gamma)$ on the charged Higgs mass. We also check that our scenarios agree with the experimental results for branching ratio $\mathcal{B}(b \rightarrow s\gamma)$ and the anomalous magnetic moment of the muon $\Delta(g_\mu - 2)/2$. Further, in S2 we study the sensitivity of the fit to large values of M_2 , such that the wino-like

²Note that in light of current LHC limits, the value $M_3=700$ GeV in S1 and S2 means that the gluino mass is rather low, however our results are largely independent of this choice as M_3 only enters our calculations via two loop corrections to m_h .

Scenario 1/2			
M_1	125	M_2	250/2000
μ	180	m_{A^0}	1000
M_3	700	$\tan \beta$	10
$M_{q_{1,2}}$	1500	$A_{q_{1,2}}$	650
$M_{l/e_{1,2}}$	1500	A_{l_i}	650
M_{l_3}	800	M_{e_3}	400
Scenario 3			
M_1	106	M_2	212
μ	180	m_{A^0}	500
M_3	1500	$\tan \beta$	12
$M_{q_{1,2}}$	1500	$A_{q_{1,2}}$	-1850
M_{l_i}	180	A_{l_i}	-1850
$M_{e_{1,2}}$	125	M_{e_3}	106

Table 1: Parameters for scenarios 1/2 and 3 (S1/S2 and S3), in GeV with the exception of $\tan \beta$. Here $M_{(l/q)_i}$ ($M_{(e/u/d)_i}$) represent the left (right) handed mass parameters for a slepton/squark of generation i respectively, and A_f is the trilinear coupling for a sfermion f . See text for stop and sbottom parameter definitions.

chargino and neutralino are heavy and decoupled from the bino and higgsino-like particles. Finally, in S1/S2 we consider the case that the sleptons (with the exception of the light stau) and pseudoscalar Higgs bosons are at the TeV scale, and in S3 the case that they are relatively light. Therefore, while S1/S2 are not in keeping with the 125 GeV Higgs boson, they provide illustrative examples of the potential of the LC in scenarios complementary to S3.³

4.3 Results for scenario 1

In this scenario, only the charginos and three neutralinos will be accessible at the LC. As input for the fit we therefore use:

- the masses of the charginos ($\tilde{\chi}_1^\pm, \tilde{\chi}_2^\pm$) and three lightest neutralinos ($\tilde{\chi}_1^0, \tilde{\chi}_2^0, \tilde{\chi}_3^0$)

³Note that in S1(S2) a Higgs mass of $m_h = 125$ GeV can also be achieved by adopting $\cos \theta_t = -0.4$ (-0.5).

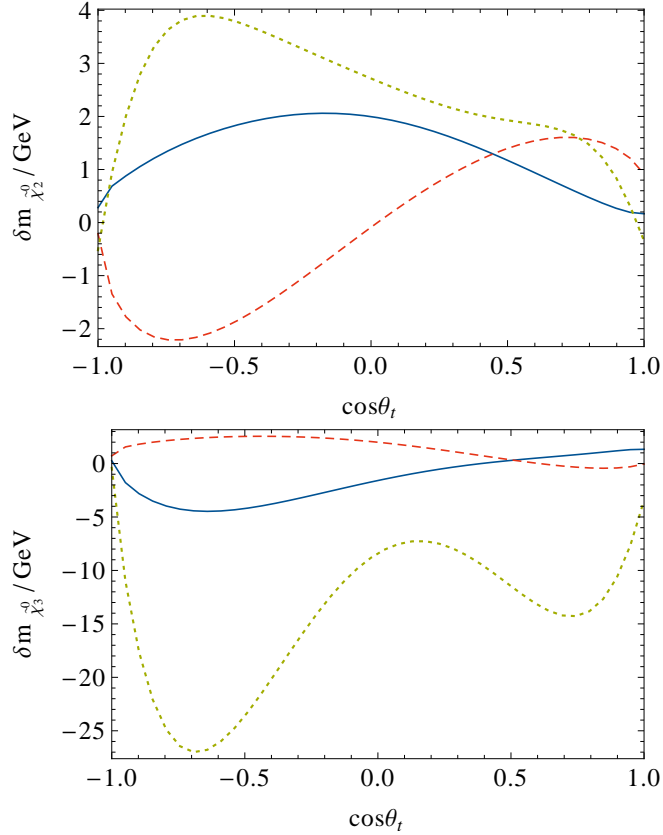


Figure 4: One-loop corrections to the masses of neutralinos $\tilde{\chi}_2^0$ (upper) and $\tilde{\chi}_3^0$ (lower) as a function of the stop mixing angle $\cos\theta_t$, for scenarios S1 (blue), S2 (red, dashed) and S3 (green, dotted).

- the light chargino production cross section $\sigma(\tilde{\chi}_1^+ \tilde{\chi}_1^-)$ with polarised beams at $\sqrt{s} = 350$ and 500 GeV
- the forward-backward asymmetry A_{FB} at $\sqrt{s} = 350$ and 500 GeV
- the branching ratio $\mathcal{B}(b \rightarrow s\gamma)$ calculated using `micrOmegas 2.4.1` [62, 63].

The input variables, together with errors, namely the assumed experimental precision of the prospective LC measurements as well as the theoretical uncertainties, are listed in tab. 4.3. It is interesting to observe the large NLO corrections to A_{FB} , which even result in a change of sign. Note that $\mathcal{B}(b \rightarrow s\gamma)$ is included in order to increase sensitivity to the third generation squark sector, and an estimated experimental precision of $0.3 \cdot 10^{-4}$, taken

Observable	Tree value	Loop corr.	Error exp.	Error th.
$m_{\tilde{\chi}_1^\pm}$	149.6	–	0.1 (0.2)	–
$m_{\tilde{\chi}_2^\pm}$	292.3	–	0.5 (2.0)	–
$m_{\tilde{\chi}_1^0}$	106.9	–	0.2	–
$m_{\tilde{\chi}_2^0}$	164.0	2.0	0.5 (1.0)	0.5
$m_{\tilde{\chi}_3^0}$	188.6	–1.5	0.5 (1.0)	0.5
$\sigma(\tilde{\chi}_1^+ \tilde{\chi}_1^-)_{(-0.8,0.6)}^{350}$	2347.5	–291.3	8.7	2.0
$\sigma(\tilde{\chi}_1^+ \tilde{\chi}_1^-)_{(0.8,-0.6)}^{350}$	224.4	7.6	2.7	0.5
$\sigma(\tilde{\chi}_1^+ \tilde{\chi}_1^-)_{(-0.8,0.6)}^{500}$	1450.6	–24.4	8.7	2.0
$\sigma(\tilde{\chi}_1^+ \tilde{\chi}_1^-)_{(0.8,-0.6)}^{500}$	154.8	12.7	2.0	0.5
$A_{FB}^{350}(\%)$	–2.2	6.8	0.8	0.1
$A_{FB}^{500}(\%)$	–2.6	5.3	1.0	0.1

Table 2: Observables (masses in GeV, cross sections in fb) used as input for the fit in S1, tree-level values and loop corrections are specified. Here the superscript on σ and A_{FB} denotes \sqrt{s} in GeV, and the subscript on σ denotes the beam polarisation ($\mathcal{P}(e^-), \mathcal{P}(e^+)$). Errors in brackets are for masses obtained from the continuum. The central value of the theoretical prediction, $\mathcal{B}(b \rightarrow s\gamma) = 3.3 \cdot 10^{-4}$ GeV is also included in the fit. See text for details of the calculation and error estimation.

from ref. [65], is adopted. We found that the impact of the muon anomalous magnetic moment is negligible in this scenario, mainly due to the heavy smuon sector. It should be possible to probe the supersymmetric QCD sector, with squark masses of ~ 1.5 TeV and the gluino mass of ~ 700 GeV, at the LHC, such that the theoretical uncertainty arising due to these parameters is small in comparison to that due to the unknown m_{A^0} . We therefore include the small dependence on the A^0 mass as an additional source of error, having explicitly checked that the impact of all other parameters is negligible. Note that there are no theoretical errors for masses chosen to be on-shell. Even at one loop, these masses are related to the fundamental parameters via the tree level relations, and are included in the fit.

Parameter	Threshold fit	Continuum fit
M_1	125 ± 0.3 (± 0.7)	125 ± 0.6 (± 1.2)
M_2	250 ± 0.6 (± 1.3)	250 ± 1.6 (± 3)
μ	180 ± 0.4 (± 0.8)	180 ± 0.7 (± 1.3)
$\tan \beta$	10 ± 0.5 (± 1)	10 ± 1.3 (± 2.6)
$m_{\tilde{\nu}}$	1500 ± 24 ($^{+60}_{-40}$)	1500 ± 20 (± 40)
$\cos \theta_t$	0 ± 0.15 ($^{+0.4}_{-0.3}$)	—
$m_{\tilde{t}_1}$	400^{+180}_{-120} (at limit at limit)	—
$m_{\tilde{t}_2}$	800^{+300}_{-170} ($^{+1000}_{-290}$)	800^{+350}_{-220} (at limit at limit)

Table 3: Fit results (masses in GeV) for S1, for masses obtained from threshold scans (threshold fit) and from the continuum (continuum fit). Numbers in brackets denote 2σ errors.

In S1 we fit 8 MSSM parameters: M_1 , M_2 , μ , $\tan \beta$, $m_{\tilde{\nu}}$, $\cos \theta_t$, $m_{\tilde{t}_1}$, and $m_{\tilde{t}_2}$. The results of the fit are given in tab. 3. We find that the gaugino and higgsino mass parameters are determined with an accuracy better than 1%, while $\tan \beta$ is determined with an accuracy of 5%. Excellent precision of 2-3% is obtained for the mass of the otherwise unobservable sneutrino. Including NLO effects even allows us to constrain the parameters of the stop sector. Although the precision shown in tab. 3 is rather limited, this could lead to an important hint concerning the masses of the stops, which, if not already seen, might allow for a well-targeted search at the LHC. This could be another example of LC-LHC interplay [66].

Finally, in tab. 3 we compare the fit results using masses of the charginos and neutralinos obtained from threshold scans and from the continuum. For the latter, the accuracy at which the parameters can be determined is seen to deteriorate, with errors on the fundamental parameters almost doubling, clearly indicating the need to measure chargino and neutralino masses via threshold scans.

4.4 Results for scenario 2

In this scenario, where the M_2 parameter is set to 2 TeV, only the light chargino and three lightest neutralinos will be accessible at the LC. As input

Observable	Tree value	Loop corr.	Error exp.	Error th.
$m_{\tilde{\chi}_1^\pm}$	179.1	—	0.1	—
$m_{\tilde{\chi}_1^0}$	111.1	—	0.2	—
$m_{\tilde{\chi}_2^0}$	183.6	0.07	0.5	0.5
$m_{\tilde{\chi}_3^0}$	194.2	1.9	0.5	0.5
$\sigma(\tilde{\chi}_1^+ \tilde{\chi}_1^-)_{(-0.8,0.6)}^{400}$	1214.9	-344.7	6.0	0.1
$\sigma(\tilde{\chi}_1^+ \tilde{\chi}_1^-)_{(0.8,-0.6)}^{400}$	250.6	-32.4	2.7	0.1
$\sigma(\tilde{\chi}_1^+ \tilde{\chi}_1^-)_{(-0.8,0.6)}^{500}$	1079.2	-194.8	6.0	0.1
$\sigma(\tilde{\chi}_1^+ \tilde{\chi}_1^-)_{(0.8,-0.6)}^{500}$	229.6	-8.7	2.7	0.1
$A_{FB}^{400}(\%)$	0.0	3.0	1.0	0.1
$A_{FB}^{500}(\%)$	0.0	5.0	1.0	0.1

Table 4: Observables (masses in GeV, cross sections in fb) used as an input for the fit in S2, as in tab. 4. The central value of the theoretical prediction, $\mathcal{B}(b \rightarrow s\gamma) = 3.3 \cdot 10^{-4}$ GeV is also included in the fit. See text for details of the calculation and error estimation.

for the fit we therefore use:

- the masses of the lighter chargino ($\tilde{\chi}_1^\pm$) and neutralinos ($\tilde{\chi}_1^0, \tilde{\chi}_2^0, \tilde{\chi}_3^0$)
- the light chargino production cross section $\sigma(\tilde{\chi}_1^+ \tilde{\chi}_1^-)$ with polarised beams at $\sqrt{s} = 400$ and 500 GeV
- the forward-backward asymmetry A_{FB} at $\sqrt{s} = 400$ and 500 GeV
- the branching ratio $\mathcal{B}(b \rightarrow s\gamma)$.

As we again find that the muon anomalous magnetic moment has a negligible impact, it is not used in the fit. The input variables, together with errors, namely the assumed experimental precision of the prospective LC measurements as well as the theoretical uncertainties, are listed in tab. 4. While A_{FB} is negligible at LO, the NLO corrections to it are again found to be large.

We again fit 8 MSSM parameters: $M_1, M_2, \mu, \tan \beta, m_{\tilde{\nu}}, \cos \theta_t, m_{\tilde{t}_1},$ and $m_{\tilde{t}_2}$. The impact of other parameters, except the heavy Higgs boson mass, can be neglected. The results from the fit are given in tab. 5. The higgsino

Parameter	Fit result
M_1	$125_{-0.6}^{+0.9}$ ($_{-1.2}^{+2.1}$)
M_2	2000 ± 200 ($_{-400}^{+600}$)
μ	180 ± 0.2 ($_{-0.3}^{+0.5}$)
$\tan \beta$	10 ± 2 ($_{-4}^{+5}$)
$m_{\tilde{\nu}}$	unconstrained
$\cos \theta_t$	$0_{-0.09}^{+0.13}$ ($_{-0.3}^{+0.4}$)
$m_{\tilde{t}_1}$	400_{-50}^{+250} ($_{-80}^{+500}$)
$m_{\tilde{t}_2}$	800_{-200}^{+300} ($_{-400}^{+900}$)

Table 5: Fit results (in GeV with the exception of $\tan \beta$ and $\cos \theta_t$) for S2, as in tab. 3, where numbers in brackets denote 2σ errors.

and bino mass parameters are well constrained in this scenario since bino-like neutralino and all higgsinos are directly accessible. Even though the winos are not directly accessible, the wino mass parameter M_2 can be constrained with 10% accuracy at 1σ level. An accuracy of 20% is achieved for $\tan \beta$, significantly worse than in S1. This can be understood by the fact that the mixing in S2 between chargino states is weak due to M_2 being heavy, and the constraint on $\tan \beta$ is dependent on this mixing. No limits can be derived on the sneutrino mass, due to the Yukawa suppressed coupling of the higgsino-like $\tilde{\chi}_1^\pm$ to the electron and sneutrino. We are however, as shown in tab. 5, still able to derive limits on the stop masses and mixing angle.

4.5 Results for scenario 3

This final scenario features the richest phenomenology of the studied benchmark scenarios. As input for the fit we therefore use:

- the masses of the charginos ($\tilde{\chi}_1^\pm, \tilde{\chi}_2^\pm$) and neutralinos ($\tilde{\chi}_1^0, \tilde{\chi}_2^0, \tilde{\chi}_3^0$)
- the light chargino production cross section $\sigma(\tilde{\chi}_1^+ \tilde{\chi}_1^-)$ with polarised beams at $\sqrt{s} = 400$ and 500 GeV
- the forward-backward asymmetry A_{FB} at $\sqrt{s} = 400$ and 500 GeV
- the Higgs boson mass, m_h

- the branching ratio $\mathcal{B}(b \rightarrow s\gamma)$
- the anomalous muon magnetic moment

Compared to the previous scenarios, these observables are supplemented by the Higgs boson mass, m_h , calculated using `FeynHiggs 2.9.1` [56–59]. The estimated experimental precision at the LC for m_h , taken from ref. [1], is adopted. We further assume the future theoretical uncertainty on the Higgs boson mass to be 1 GeV [59]. As before, the remaining two observables, the branching ratio $\mathcal{B}(b \rightarrow s\gamma)$ and the anomalous muon magnetic moment are calculated using `micrOmegas 2.4.1` [62, 63], and a projected experimental error on the anomalous muon magnetic moment of $3.4 \cdot 10^{-10}$ is employed [67], which we assume would dominate over the theoretical uncertainty. The input variables, together with errors, namely the assumed experimental precision of the prospective LC measurements and the theoretical uncertainties, are summarised in tab. 6. As the sneutrino is now directly accessible, we assume that its mass has been measured and it is therefore not included in the fit. On the other hand, due to the stronger dependence of the NLO cross-section and forward-backward asymmetry on m_{A^0} , this is now used as an additional fit parameter. We neglect the remaining theoretical uncertainty on the cross-sections, as it is found to be negligible in comparison to the experimental error.

This means that in scenario 3, we fit to M_1 , M_2 , μ , $\tan\beta$, $\cos\theta_t$, $m_{\tilde{t}_1}$, $m_{\tilde{t}_2}$ and m_{A^0} . The results of the fit are collected in tab. 7. The parameters of the electroweak gaugino-higgsino sector are determined with high precision. Due to a significant mixing in the stop sector, and the improvement in the fit quality due to the inclusion of the higgs mass, we find that the fit is now also more sensitive to the mass of the heavy stop. The accuracy is better than 20% for this particle even though it is far beyond the reach of the LC and also most likely of the LHC. In addition, in this scenario an upper limit on the mass of the heavy Higgs boson can be placed at 1000 GeV, at the 2σ level. It is the particular sensitivity of the NLO corrections to m_{A^0} which presents this unique opportunity to set such an upper bound.

5 Conclusions

The evidence for the Higgs boson and dark matter, when examined in the context of supersymmetry, suggests the possibility of a light μ and M_1 . We have extended previous analyses, which fitted observables for chargino production at the LC to extract fundamental MSSM parameters, by incorporating NLO corrections. The loop corrections are calculated for all observables

Observable	Tree value	Loop corr.	Error exp.	Error th.
$m_{\tilde{\chi}_1^\pm}$	139.3	—	0.1	—
$m_{\tilde{\chi}_2^\pm}$	266.2	—	0.5	—
$m_{\tilde{\chi}_1^0}$	92.8	—	0.2	—
$m_{\tilde{\chi}_2^0}$	148.5	2.4	0.5	0.5
$m_{\tilde{\chi}_3^0}$	189.7	−7.3	0.5	0.5
$\sigma(\tilde{\chi}_1^+ \tilde{\chi}_1^-)_{(-0.8,0.6)}^{400}$	709.7	−85.1	4.5	—
$\sigma(\tilde{\chi}_1^+ \tilde{\chi}_1^-)_{(0.8,-0.6)}^{400}$	129.8	20.0	2.0	—
$\sigma(\tilde{\chi}_1^+ \tilde{\chi}_1^-)_{(-0.8,0.6)}^{500}$	560.0	−70.1	4.5	—
$\sigma(\tilde{\chi}_1^+ \tilde{\chi}_1^-)_{(0.8,-0.6)}^{500}$	97.1	16.4	2.0	—
$A_{FB}^{400}(\%)$	24.7	−2.8	1.4	0.1
$A_{FB}^{500}(\%)$	39.2	−5.8	1.5	0.1

Table 6: Observables (masses in GeV, cross sections in fb) used as an input for the fit in S3, as in tab. 4.3. The central values of the theoretical predictions $\mathcal{B}(b \rightarrow s\gamma) = 2.7 \cdot 10^{-4}$, $\Delta(g_\mu - 2)/2 = 2.4 \cdot 10^{-9}$ and $m_h = 125$ GeV are also included in the fit. See text for details of the calculation and error estimation.

fitted, namely the polarised cross-sections and forward backward asymmetry for chargino production as well as the $\tilde{\chi}_1^\pm, \tilde{\chi}_2^\pm$ and $\tilde{\chi}_1^0, \tilde{\chi}_2^0, \tilde{\chi}_3^0$ masses, in an on-shell scheme which facilitates the extension to the complex case. We have fitted these observables in three complementary scenarios.

On including NLO corrections, we found that when M_1, M_2 and μ are light they can be determined to percent-level accuracy, and $\tan\beta$ to $< 5\%$. Further we showed that if masses of the charginos and neutralinos are obtained from the continuum as opposed to via threshold scans, the uncertainty on the fundamental parameters would almost double, reinforcing the importance of threshold scans for mass measurements. As a heavy M_2 is still a viable possibility, we also considered $M_2 = 2000$ GeV, and found that the sensitivity to M_2 is approximately 10%. However in this case the error on $\tan\beta$, dependent on the degree of mixing in the chargino sector, increases to $\sim 20\%$. Note that the inclusion of $\mathcal{B}(b \rightarrow s\gamma)$ in the fit, in combination with the use of masses determined via threshold scanning, was seen to improve

Parameter	Fit result
M_1	106 ± 0.3 (± 0.5)
M_2	212 ± 0.5 (± 1.0)
μ	180 ± 0.4 (± 0.9)
$\tan \beta$	12 ± 0.3 (± 0.7)
$\cos \theta_t$	$0.15^{+0.08}_{-0.06}$ ($^{+0.16}_{-0.09}$)
$m_{\tilde{t}_1}$	430^{+200}_{-130} ($^{+300}_{-400}$)
$m_{\tilde{t}_2}$	1520^{+200}_{-300} ($^{+300}_{-400}$)
m_{A^0}	< 650 (< 1000)

Table 7: Fit results (in GeV with the exception of $\tan \beta$ and $\cos \theta_t$) for S3, including results for the masses of the heavier stop mass ($m_{\tilde{t}_2}$) and the pseudoscalar higgs boson (m_{A^0}).

the sensitivity to the stop sector.

The final scenario we considered was compatible with the latest Higgs results. Here we found that including $\mathcal{B}(b \rightarrow s\gamma)$, $\Delta(g_\mu - 2)/2$ and m_h in the fit, as well as the fact that there was significant mixing in the stop sector, helped to obtain an accuracy better than 20% on the mass of the heavy stop, even though this particle is far beyond the reach of the LC and also most likely of the LHC. We also included m_{A^0} in the fit, and found that, due to the particular sensitivity of the NLO corrections to m_{A^0} , it would even be possible to place a 2σ upper bound on this parameter of 1000 GeV. In summary, we have shown that incorporating NLO corrections is required for the precise determination of the fundamental parameters of the chargino and neutralino sector at the LC, and could further provide sensitivity to the parameters describing particles which contribute via loop corrections.

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