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Measurement of harm and beauty production in deep inelastic ep scattering from decays into muons at HERA

ZEUS Collaboration

Abstract

The production of charm and beauty quarks in ep interactions has been measured with the ZEUS detector at HERA for squared four-momentum exchange $Q^2 > 20 \,\mathrm{GeV}$, using an integrated luminosity of 126 pb¹. Charm and beauty quarks were identified through their decays into muons. Differential cross sections were measured for muon transverse momenta $p_T^+ > 1.5$ GeV and pseudorapidities $-1.6 < \eta^{\mu} < 2.3$, as a function of $p_T^{\mu}, \eta^{\mu}, Q^2$ and Bjorken x. The charm and beauty contributions to the proton structure function F_2 were also extracted. The results agree with previous measurements based on independent techniques and are well des
ribed by QCD predi
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Introduction $\mathbf{1}$

The measurement of charm and beauty production in deep inelastic scattering (DIS) provides a stringent test of quantum hromodynami
s (QCD) sin
e the large quark masses provide hard s
ales that make perturbative al
ulations appli
able. At leading order, $_{\rm{Heavv}}$ quarks (HQs) are produced in DIS via boson-gluon fusion (BGF) (γ $q \rightarrow qq$). A precise measurement of HQ production in DIS therefore provides a direct constraint on the gluon parton density fun
tion (PDF) of the proton.

Charm production in DIS at HERA has been measured previously using reconstructed charmed mesons $[1, 2]$ or inclusively by exploiting the long lifetime of charmed hadrons $[3]$. Beauty production in DIS has been studied in events with muons and jets [4, 5] and from lifetime information $[3]$. The existing data are generally in good agreement with nextto-leading-order (NLO) QCD predictions. The largest differences were observed in the muon analyses [4, 5] where the measured beauty cross section was about two standard deviations above the theoretical expectation.

In this paper, a simultaneous measurement of beauty and charm production using semileptonic (SL) decays into muons is presented. The fractions of muons originating from charm, beauty and light flavours (LF) were extracted by exploiting three discriminating variables: the muon impa
t parameter, the muon momentum omponent transverse to the asso
iated jet axis and the missing transverse momentum, whi
h is sensitive to the neutrino from SL decays.

The analysis focused on data with large squared four-momentum exchange at the electron vertex, Q^{\ast} , where charm measurements based on muons are competitive with those based on identied harmed mesons.

The cross sections for muons from charm and beauty decays were measured for Q^2 20 GeV $^{\circ},$ muon transverse momenta $p_T^r > 1.5$ GeV and pseudorapidities $^{\circ}$ –1.6 $< \eta^{\mu} < 2.3$ as a function of $p_{T}^{r},~\eta^{\mu},~Q^{2},$ and of the Bjorken scaling variable x [6] and compared to $\overline{}$ QCD predictions. The muon cross sections, measured in bins of x and Q^{\pm} , were used to extract the heavy quark contributions to the proton structure function F_2 which were ompared to previous results and to QCD predi
tions.

The data used in this analysis were collected with the ZEUS detector in the 2005 running period during whi
h HERA ollided ele
trons with energy Ee ⁼ 27:5 GeV with protons with $E_p = 920 \text{ GeV}$ corresponding to a centre-of-mass energy $\sqrt{s} = 318 \text{ GeV}$. The corresponding integrated luminosity was $\mathcal{L} = 120.0 \pm 3.3$ pb $^{-1}$.

 $\,$ - The ZEUs coordinate system is a right-handed Cartesian system, with the Z axis pointing in the proton beam direction, referred to as the "forward direction", and the X axis pointing towards the centre of HERA. The pseudorapidity is defined as $n = -\ln(\tan \frac{\theta}{2})$, where is the polar angles and polar angles.

Theoretical predictions $\overline{2}$

Heavy quark production in DIS has been calculated at hext-to-leading order $(O(\alpha_s^-))$ in the so-called fixed flavour number scheme (FFNS) in which only light flavours are present in the proton and heavy quarks are produced in the interaction $[7]$. The results of this analysis have been compared to NLO calculations performed with the Hvq pis program $[8, 9]$. The renormalisation and factorisation scales were set to $\mu_R = \mu_F =$ $Q^2 + 4m_q^2$ and the quark masses to $m_c = 1.5 \,\mathrm{GeV}$ and $m_b = 4.75 \,\mathrm{GeV}$. The PDFs were obtained by repeating the ZEUS-S [10] PDF fit in the FFNS with quark masses set to the same values as in the Hyqpis calculation.

To calculate muon observables, the partonic results were interfaced to a model of HQ fragmentation into weakly decaying heavy hadrons and of the decay of heavy hadrons into muons. The hadron momentum was obtained by scaling the quark momentum according tion function charm and $\epsilon_b = 0.0035$ for beauty. This choice of ϵ_c corresponds to $\epsilon_c = 0.035$ for D mesons $[12]$ since kinematic considerations $[13]$ and direct measurements $[14]$ show that, on average, the momentum of the weakly decaying hadrons is $\approx 5\%$ lower than that of D^* mesons.

The semileptonic decay spectrum for charm was taken from a recent CLEO measurement $[15]$. The decay spectrum for beauty hadrons was taken from the PYTHIA $[16]$ Monte Carlo (MC), mixing direct SL decays and cascade decays through charm according to the measured branching ratios [17]. It was checked that the MC described BELLE and BABAR data [18] well. The branching ratios were set to $\mathcal{B}(c \to \mu) = 0.096 \pm 0.004$ and $\mathcal{B}(b \to \mu) = 0.209 \pm 0.004$ [17].

The uncertainty on the theoretical predictions was evaluated by independently varying \mathbb{P}^{α} and \mathbb{P}^{α} for the HQ masses simultaneously to \mathbb{P}^{α} and \mathbb{P}^{α} for \mathbb{P}^{α} and $\$ $(1.3, 4.5), (1.7, 5.0)$ GeV in the calculation and in the PDF fit; by varying the proton PDFs by their experimental uncertainty and by varying the fragmentation parameters within 0.04 $\lt \epsilon_c \lt 0.12$ (corresponding to 0.025 $\lt \epsilon_c \lt 0.085$ for D -mesons [19]) and order and the further that the further the further the further than the further and the function α sum of the energy and the momentum parallel to the HQ direction, $E+p_{||}$, rather than the HQ momentum. The total theoreti
al un
ertainty was obtained by adding in quadrature the effects of each variation. In the beauty case, the total uncertainty is dominated by the mass while for the mass while for the mass while for the variation of α ontribution.

The calculations of $F_2^{\alpha\alpha}$ and $F_2^{\alpha\alpha}$ in the FFNS were performed using HVQDIS and cross checked with the QCD evolution code [20] used in the ZEUS PDF fit.

3 Monte Carlo samples

Charm and beauty MC samples were generated using RAPGAP 3.00 [21] to simulate the leading order BGF pro
ess. Parton shower te
hniques were used to simulate higher order QCD effects. Higher order QED effects were included through HERACLES 4.6 [22]. The CTEST constant were used and the HQ masses were set to masses were set to masses were set to masses were s \cdots u \cdots

Light flavour MC events were extracted from an inclusive DIS sample generated with a contracted and part interface of the hadronic to a matter of the part in the hadronic contracted compute state with the matrix element plus parton shower (MEPS) model and to HERACLES 4.6 to include electroweak radiative corrections. The CTEQ5D [23] parton density was used.

Inelastic J/ψ production was simulated with CASCADE [26] since that model generally describes the DIS data of a previous publication [27].

The above samples corresponded to at least five times the luminosity of the data. A smaller light quark sample was generated with RAPGAP and mixed with the heavy quark Rapgap samples for the study of the in
lusive DIS ontrol sample (Se
tion [6\)](#page-12-0).

Fragmentation and particle decays were simulated using the JETSET/PYTHIA model [28, 16. The lepton energy spectrum from charm decays was reweighted to agree with CLEO data [15]. The MC events were passed through a full simulation of the ZEUS detector based on GEANT 3.21 [29]. They were then subjected to the same trigger criteria and reconstructed with the same programs as used for the data.

Experimental set-up $\overline{4}$

A detailed description of the ZEUS detector can be found elsewhere [30]. A brief outline of the omponents that were most relevant for this analysis is given below.

Charged particles were tracked in the silicon microvertex detector (MVD) [31] and in the central tracking detector (CTD) [32], which operated in a magnetic field of 1.43 T provided by a thin super
ondu
ting solenoid. The MVD onsisted of a barrel (BMVD) and a forward (FMVD) section with three cylindrical layers and four vertical planes of singlesided silicon detectors, respectively. The CTD consisted of 72 cylindrical drift chamber layers, organised in 9 superlayers covering the polar-angle region 15 $\,<\,\theta\,<\,104$. Alter alignment, the single-hit resolution of the BMVD was $25 \mu m$ and the impact parameter resolution of the CTD-BMVD system for high-momentum tracks was $\approx 100 \mu$ m.

The high-resolution uranium-scintillator calorimeter (CAL) [33] consisted of three parts: the forward (FCAL), the barrel (BCAL) and the rear (RCAL) calorimeters. Each part was subdivided transversely into towers and longitudinally into one electromagnetic section and either one (in RCAL) or two (in BCAL and FCAL) hadronic sections. Under testbeam conditions, the CAL single-particle relative energy resolutions were $\sigma(E)/E$ = \blacksquare provided and the control of Experimentally define a set of the distribution \mathbb{R}^n . The distribution of \mathbb{R}^n is the distribution of \mathbb{R}^n provided and the contract of the $E = E$ in GeV. The energy of the energy ele
trons hitting the RCAL was orre
ted for the presen
e of dead material using the rear presampler detector (PRES) [34] and the small angle rear tracking detector (SRTD) [35].

The muon system consisted of rear/barrel $(R/BMUON)$ [36] and forward (FMUON) [30] tracking detectors. The B/RMUON consisted of limited-streamer (LS) tube chambers pla
ed behind the BCAL (RCAL), inside and outside a magnetised iron yoke surrounding the CAL. The barrel and rear muon chambers cover polar angles from 54° to 155° and from 135 to 171 , respectively. The FMUON consisted of six trigger planes of LS tubes and four planes of drift chambers covering the angular region from 5° to 52° . The muon system exploited the magnetic field of the iron yoke and, in the forward direction, of two iron toroids magnetised to ≈ 1.6 T to provide an independent measurement of the muon momentum.

The luminosity was measured using the Bethe-Heitler reaction $ep \rightarrow e\gamma p$ with the luminosity detector which consisted of two independent systems, a photon calorimeter [37] and a magnetic spectrometer [38].

5 Event re
onstru
tion and sele
tion

A three-level trigger was used to select events online [30, 39]. DIS events were selected by requiring a s
attered ele
tron in the CAL.

A scattered electron with energy $E_e > 8 \,\mathrm{GeV}$ was required oinine. The primary vertex had to be within ± 30 cm in Z from the nominal interaction point.

Muons were reconstructed by matching a $CTD+MVD$ track to a track segment in the inner or outer B/RMUON chambers or to an FMUON track crossing at least four FMUON planes. This B/RMUON sele
tion was looser than in some previous analyses, whi
h required the muons to reach the external chambers $[4, 40]$, allowing a lower threshold for the muon transverse momentum.

The central track associated to a B/RMUON candidate was required to pass at least three CTD superlayers and to have at least four hits in the MVD to allow a good impa
t parameter measurement. The tra
ks asso
iated to FMUON andidates were required to pass at least one CTD superlayer, orresponding to at least four degrees of freedom in the track fit.

Muons were accepted in the kinematic region defined by

$$
p_T^{\mu} > 1.5 \,\text{GeV}, -1.6 < \eta^{\mu} < 2.3
$$

The hadronic system (including the muon) was reconstructed from energy flow objects (EFOs) [41] that combine the information from calorimetry and tracking, corrected for energy loss in the dead material. The EFOs were corrected using the measured momenta of identified muons [40, 42]. A reconstructed four-momentum $(p_X^{}, p_Y^{}, p_Z^{}, E^{\times})$ was assigned to each EFO *i*.

To select a clean DIS sample, the following cuts on global variables were applied:

$$
(E - P_Z)_{\text{tot}} = (E - P_Z)_h + E'_e (1 - \cos \theta_e) \quad \subset [40, 80] \,\text{GeV}
$$
\n
$$
y_e = 1 - E'_e (1 - \cos \theta_e) / (2E_e) \quad < 0.7
$$
\n
$$
y_{\text{JB}} = (E - P_Z)_h / (2E_e) \quad > 0.01
$$
\n
$$
Q^2_{\Sigma} = (E'_e \sin \theta_e)^2 / (1 - y_{\Sigma}) \quad > 20 \,\text{GeV}^2,
$$

where $(E-P_Z)_h = \sum_{i\in E\text{FOs}} E^i - p_Z^i$, $y_\Sigma = (E-P_Z)_h / (E-P_Z)_{\text{tot}}$ [43], and θ_e is the electron polar angle. These cuts restricted the accessible inelasticity $y = Q^2/(xs)$ and Q^2 to $0.01 < y < 0.7$ and $Q^2 > 20\,\mathrm{GeV}$. The DIS variables x and Q^2 were reconstructed using the \triangle estimators Q_{Σ} and $x_{\Sigma} = Q_{\Sigma}/(sy_{\Sigma})$ [45].

To remove background events with isolated muons ($\gamma\gamma \to \mu^+ \mu^-$, J/ψ and T decays) and residual cosmic muons, an anti-isolation cut was applied by requiring that the hadronic energy in a cone of radius 1 in the $\eta - \phi$ plane around the muon candidate, excluding the muon itself, was $E^{iso} > 0.5 \,\text{GeV}$. From MC studies this cut was 98% (90%) efficient for harm (beauty).

Jets were reconstructed from EFT and the the construction \mathcal{A} in the longitudinal later than \mathcal{A} invariant mode [45]. About 96% of the muon candidates were associated to a jet with transverse momentum (including the muon) p_T T , T and ω or T and ω for further and ω further analysis. After the above selection, the final sample contained 11126 muons. A subsample of 35 events with more than one muon was found, zo of which consisted of $\mu^+\mu^-$ pairs. A J/ψ signal of 9 events was observed in the $\mu^+\mu^-$ invariant mass distribution. The total contamination from J/ψ production was estimated with the CASCADE MC, normalised to the observed J/ψ signal. It was found to be $(0.9 \pm 0.3)\%$ and was neglected in the analysis.

6 Extraction of the charm and beauty fractions

The sample of sele
ted muon andidates ontained signal muons from harm and beauty decays and background from in-inght π^- and K^- decays and from the punch through of hadronic jets in the muon chambers. Candidates from in-flight decays and punch through. which are subsequently denoted as "false muons", were present both in the LF events and in events ontaining HQs.

The fractions of muons originating from charm, beauty or LF events were determined from a simultaneous fit of three discriminating variables sensitive to different aspects of HQ de
ays:

- \bullet $p_{\overline{T}}$, the muon momentum component transverse to the axis of the associated jet, $p_T^-=|{\bf p}\cap\times{\bf p}^{\tau+}|/|{\bf p}^{\tau+}|.$ Due to the large σ mass, muons from beauty hadron decays have a harder p_T^{\perp} spectrum than those from charm or light quarks;
- δ , the distance of closest approach of the muon track to the centre of the interaction region (beam spot) in the X, Y plane. A positive sign was assigned to δ if the muon track crosses the axis of the associated jet in the jet hemisphere, negative otherwise. The beam spot position was obtained by fitting the reconstructed primary vertex distribution for every 2000 ep events. The size of the interaction region was $\delta 0\times 20~\mu{\rm m}$. in the community from decomplete the strenger of the strenger of the strenger of the strenger μ and the community tracks originating from the primary interaction have a symmetric δ distribution around zero, orresponding to the experimental resolution.
- \bullet p_T^{max} , the missing transverse momentum parallel to the muon direction. The missing transverse momentum ve
tor was al
ulated using the ele
tron and the EFOs. The p_T^{max} distribution has a positive tail of events containing semileptonic HQ decays due to the presen
e of the neutrino.

A ontrol sample of in
lusive DIS data, sele
ted similarly to the muon sample but without any muon requirement, was used to test the quality of the simulation of these variables. The control sample is dominated by LF events, containing, according to MC, about 18% (1%) of c (b) events. The p_T^{\perp} distribution of inclusive tracks in the control sample was reasonably well reprodu
ed by both the DjangoH and the Rapgap in
lusive DIS samples. The small differences (at most 10% at p_T $>$ 2 GeV) were corrected for by applying a bin-by-bin correction to the p_T^{\perp} distribution of the LF and charm MC samples similarly to a previous publication [40]. The quality of the MC description of $p_T^{(m)}$ \mathbf{I} was a set of \mathbf{I} also evaluated in the missing and α similar populated in the missing and α transverse momentum parallel to the electron $p_T^{\rm{mean}}$ T . The best description of the $p_T^{\rm mean}$ distribution of the inclusive DIS sample was obtained by shifting the hadronic transverse momentum by (0.1 ± 0.1) GeV in the MC and by increasing the hadronic transverse momentum resolution by $(5 \pm 5)\%$ in the case of RAPGAP and by $(0 \pm 5)\%$ in the case of DJANGOH. The resolution on δ was studied using tracks in the inclusive DIS sample. since it was underteached in the MC by ψ -dependent small ψ and ψ is ψ applied to the MC, similarly to what was done in a previous publication $[47]$.

The fractions of b , c and LF events were obtained by fitting a combination of MC distributions to the measured three-dimensional distribution of the discriminating variables [48]. The fit range was $|\delta| < 0.1$ cm, $p_T^{\text{\tiny{tot}}} < 2.5\,\text{GeV}$ and $|p_T^{\text{\tiny{inner}}}|^{p}$ T j is the second of presence measurement of δ was only possible inside the region covered by the BMVD. Hence for events with muons reconstructed in the FMUON (4% of the total) only p_T^{rec} and p_T^{rec} were used in the fit. A Poisson likelihood fit was used, taking into account the limited MC statistics.

The global charm and beauty fractions resulting from the fit were

$$
f_c = 0.456 \pm 0.029
$$
(stat.); $f_b = 0.122 \pm 0.013$ (stat.)

with a orrelation oeÆ
ient b ⁼ 0:43. Figure [1\(](#page-26-0)a) shows the distributions of the three dis
riminating variables ompared to the MC distributions with the normalisation corresponding to the fit. While δ and p_T^{--} provide discrimination between LF and π s, p_T^+ discriminates between beauty and the other components. Figure 1(d) shows the distribution of $p_T^{\scriptscriptstyle{(}}{}^{\scriptscriptstyle{(}}$ for a signal-enriched subsample. The distributions of $p_T^{\scriptscriptstyle{(}}{}^{\scriptscriptstyle{(}}\,,\,\eta^{\mu},\,p_T^{\scriptscriptstyle{(}}\,,\, \, \cdot)$ $\overline{}$ $\overline{}$ $E = F_Z, \, Q_{\Sigma}$ and x_{Σ} for the data and for the MC samples normalised according to the fit are shown in Fig. [2.](#page-27-0) The overall agreement is satisfactory.

7 Acceptance and QED corrections

The visible cross sections for muons from charm and beauty decays, including beauty cascade decays via c, \bar{c}, τ and ψ , were measured in the kinematic range

$$
Q^2 > 20 \text{ GeV}^2; \ 0.01 < y < 0.7; \ p_T^{\mu} > 1.5 \text{ GeV}; \ -1.6 < \eta^{\mu} < 2.3. \tag{1}
$$

The cross sections were calculated using

$$
\sigma^q = \frac{f_q N}{A_q \mathcal{L}} C_r,
$$

where α is the HQ fraction from the HQ from the HQ fraction from the number of the number of the number of α is the a

eptan
e, Cr is the QED radiative orre
tion, and ^q ⁼ ; b. Dierential ross sections were measured by repeating the fit in bins of the reconstructed variable V as $d\sigma/dV = \sigma_i^2$ $\frac{1}{i}/\Delta V_i$, where σ_i^* $\frac{1}{l}$

e and a construction from the MC simulation as the MC simulation as the MC simulation as the material construction as muons divided by the number of true muons from decays of the quark q . This definition takes into account the charm and beauty events in which a "false muon" is reconstructed rather than a signal muon from a HQ decay. The acceptance included the efficiency of muon reconstruction (which in turn includes the efficiency of the muon chambers and of the mat
hing with entral tra
king) that was evaluated from an independent ex
lusive dim uon sample as explained in previous publications [40, 42]. The muon reconstruction efficiency was around 50% for central muons with p_{τ}^c Γ and Γ ranged from 23% (16%) at 1.5 \leq $p_{\scriptscriptstyle T}^{\scriptscriptstyle C}$ $T_T < 2.5\,{\rm GeV}$ to \approx 35% (25%) at p_T^{ω} T is a 2:5 GeV. The T difference in acceptance between c and b was mainly due to the different contribution from "false muons" which was $\approx 25\%$ for c and $\approx 3\%$ for b

According to the MC simulation, the probability to find a "false muon" in a DIS event (before any muon selection) is $\mathcal{P}_{\text{false}} \approx 0.1\%$, almost independently from the event being c, b or LF. The ability of the MC to reproduce $\mathcal{P}_{\text{false}}$ was studied by comparing the number of LF events in the data, as obtained from the fit, to the absolute prediction by DJANGOH. The data/MC ratio, $P_{\text{false}}/P_{\text{false}}$, was estimated as 0.80 ± 0.20 in the RMUON, 1.10 ± 0.20 in the BMUON, and 1.05 ± 0.40 in the FMUON, in agreement with previous studies [49].

The cross sections were corrected to the QED Born level, calculated using a running coupling costant α_{em} , such that they can be compared directly to the QCD predictions from the Hvqdis program (Se
tion [2\)](#page-9-0). The radiative orre
tions were obtained as Cr ⁼ $\sigma_{\rm Born}/\sigma_{\rm rad}$, where $\sigma_{\rm Born}$ is the RAPGAP cross section with the QED corrections turned off but keeping α_{em} running and σ_{rad} is the RAPGAP cross section with the full QED orrested MC standard McCare McCare McCare McCare (1999) ally Cr the Standard McCare McCare (1995) and the Stan and at maximum 1.10 in the highest Q^\ast bin.

8 Systemati un
ertainties 8

The following systematic uncertainties were considered (the effects on the total visible cross section for c and for b is given in parentheses):

- 1. B/RMUON efficiency: it was varied by its uncertainty of on average $\pm 5\%$ ($\mp 5, \mp 5\%$);
- 2. FMUON efficiency: it was varied by $\pm 20\%$ ($\mp 2, \mp 5\%$)
- 3. "false muon" probability: it was varied within the corresponding uncertainty for each muon detector $\binom{1}{+4}, +1$ /%;
- 4. global energy scale: it was varied by \pm 2 $\%$ ($_{+5},_{+2}$) $\%$;
- 5. calibration of p_T^{max} \mathbf{I} is was evaluated by variance momentum the hadronic transverse momentum \mathbf{I} in the MC by ± 0.1 GeV, as allowed by the transverse momentum balance in the control sample $(\pm 12,_{+1})\%;$
- 6. hadronic energy resolution: it was varied in the MC by $\pm 5\%$ as allowed by the transverse momentum balance in the control sample $(\frac{1}{2}, +1)\%$;
- 7. simulation of the tails of p_T^{max} \overline{T} : the fits were redone in the restricted range $|p_T^{\rm{mean}}|$ $T = \square$ $5 \,\text{GeV}$ $(0, -6)\%$;
- 8. resolution on δ : the smearing applied to the MC was varied by $\pm 25\%$ as allowed by the control sample $\binom{1}{2}, \binom{3}{2}$ /%;
- 9. p_T^{\perp} shape of LF and charm: it was evaluated by varying the p_T^{\perp} correction by \pm 50% $(+1.5,-5)/0;$
- 10. hadronic energy flow near the muon: it was evaluated by varying the cut on E^{iso} by $_{-0.25}$ GeV (0, 0)%;
- 11. jet description: the cut on p_T T_T was varied by $\pm 0.5\,{\rm GeV}$ ($\pm 2.5,_{+2.5}$)%;
- 12. charm SL decay spectrum: the reweighting to the CLEO model was varied by $\pm 50\%$. $\left(\frac{1}{2},\frac{3}{2}\right)$ %;
- 13. MC model dependence: the RAPGAP c and b samples were reweighted to reproduce the corresponding measured differential cross sections in Q^2 or in p_T^2 and the largest deviation from the nominal cross section was taken $(+6, +20)\%$;
- 14. higher order effects: this uncertainty was evaluated by varying the HQ distribution before parton showering in RAPGAP by the difference between NLO and leading order, as evaluated with HVQDIS (\perp_{10}, \perp_3) %;
- 15. MVD efficiency: the efficiency of the cut on the number of MVD hits of $(90 \pm 3)\%$ was varied by its uncertainty $(7-3, 7-3)\%$;
- 16. CTD simulation: tracks were required to pass \geq 4 superlayers in the B/RMUON region and to have ≥ 7 degress of freedom in the FMUON region $(+1,0)\%$;
- 17. integrated luminosity: measurement uncertainty $(\pm 2.6, \pm 2.6)$ %.

The above uncertainties were summed in quadrature to obtain the total systematic uncertainty $\left(-19,-17\right)$ %.

Cross sections 9

The visible cross sections for muons from charm and beauty decays in the kinematic region of Eq. (1) are

$$
\sigma^{c} = 164 \pm 10 \text{(stat.)} \, ^{+30}_{-31} \text{(syst.)} \, \text{pb}
$$
\n
$$
\sigma^{b} = 63 \pm 7 \text{(stat.)} \, ^{+18}_{-11} \text{(syst.)} \, \text{pb}
$$

to be compared with the NLO QCD cross sections obtained with HvQDIS of σ^c = 184^{+20}_{-40} pb and $\sigma^2 = 33 \pm 5$ pb. The agreement is good for charm while the beauty cross section is 2.3 (1.9) standard deviations above the central (upper) HvQDIS result. The visible cross sections are a factor 1.04 and 2.27 higher than the Rapgap MC predictions for c and b , respectively.

The differential cross sections as a function of p_T^r , η^{μ} , Q^2 , and x are presented in Table [1](#page-23-0) and compared in Fig. [3](#page-28-0) to the NLO QCD predictions based on HvQDIS. The RAPGAP MC predictions are also shown, normalised according to the result of the global fit. Charm and beauty cross sections are similar for $p_{\scriptscriptstyle T}^{\scriptscriptstyle -}$ \mathbf{I} , since \mathbf{I}

The charm cross sections are in good agreement with the HvQDIS calculations. The tendency of the beauty cross section to lie above the central NLO prediction is concentrated at low p_{T}^{τ} and low $Q^{\ast}.$ The statistical significance of the difference between the data and $\overline{}$ the NLO predicitons is similar to that obtained for the total visible cross section since the un
ertainties are dominated by orrelated systemati
s.

Both NLO calculations and the RAPGAP MC give in general a good description of the shape of the differential cross sections. The Q^\ast distributions for beauty is somewhat steeper than predicited by RAPGAP and HVQDIS.

\sim

The heavy quark contribution to the proton structure functions, $F_2^{\tau_1}, F_L^{\tau_2}$ and the reduced c ross section $\sigma^{_{12}}$ are defined in analogy with the inclusive case from the double differential cross section in x and Q^2 for the production of the quark q :

$$
\frac{d^2\sigma^{q\bar{q}}}{dx\,dQ^2} = \mathcal{K}\left[F_2^{q\bar{q}}(x,Q^2) - \frac{y^2}{Y_+}F_L^{q\bar{q}}(x,Q^2)\right] = \mathcal{K}\,\,\tilde{\sigma}^{q\bar{q}}(x,Q^2,s),
$$

where $\mathcal{L} = Y_+(Z \pi \alpha_{em}^-)/(x Q^2)$ and $Y_+ = 1 + (1 - y)^2$.

The muon cross sections, σ^q , measured in bins of x and Q^2 , were used to extract $F_2^{\tau^2}$ at a reference points in the x, \mathcal{Q} –plane by:

$$
F_2^{q\bar{q}}(x,Q^2) = \sigma^q \frac{F_2^{q\bar{q},\text{th}}(x,Q^2)}{\sigma^{q,\text{th}}},
$$

where $F_2^{\tau_2,\cdots}(x,Q^2)$ and $\sigma^{q,\cdots}$ were calculated at NLO in the FFNS using the HVQDIS program. The reference points were chosen close to the average x and Q for the events within each bin. Charm produced in θ decays was not included in the definition of θ^* .

This procedure contains several corrections: the extrapolation from the restricted muon kinematic range ($p_{\scriptscriptstyle T}^c$ $T_T > 1.5$ GeV, $-1.6 < T_T < 2.5$) to the full muon phase space; the $q\rightarrow \mu$ branching ratio; the correction for the longitudinal structure function $F_L^{\tau_1}$ and the orre
tion from a bin-averaged ross se
tion to a point value (bin entring).

The largest un
ertainty is related to the extrapolation to the full muon phase spa
e. The kinematic acceptance, \mathcal{A} , defined as the fraction of muons from HQ decays that was generated in the restricted kinematic region is, on average, $\langle A \rangle = 13\% (27\%)$, for charm (beauty). According to HvQDIS, in the charm case, A becomes sizeable $(A > 0.25 \langle A \rangle)$ when one of the two states in the event has pT \mathbf{f} and its rapidity is in the event has pT \mathbf{f} the range $(-1.5 : 2.5)$, which corresponds to the phase space containing 88% of the cross section. In the beauty case, A is sizeable over the full HQ phase space.

The theoretical uncertainty in the extraction of F_2^{α} was evaluated by varying the HVQDIS parameters as explained in Section [2](#page-9-0) and by using a different PDF set (CTEQ5F). It is dominated by the fragmentation uncertainty. As a further check, $F_2^{\tau_1}$ was also evaluated taking A from RAPGAP and found to be consistent within the quoted uncertainties.

The muon cross sections in bins of x and \mathcal{Q}^+ are given in Table [2.](#page-24-0) The extracted F_2^+ and $F_2^{b\bar{b}}$ are presented in Tables [3](#page-24-1) and [4](#page-29-0) and shown in Figs. 4 and [5.](#page-30-0) Also given in Tables [3](#page-24-1) and [4](#page-25-0) are the factor A and the correction for the longitudinal structure function $C_L = \sigma^{qq}/F_2^{31}$ as obtained from the NLO theory. The effects of the individual sources of systematic and theoretical uncertainty are given in Tables [5](#page-33-0) and [6](#page-34-0) in the Appendix ⁻.

r igure [4](#page-29-0) also comtains a comparison of r_2 – with previous results based on the measurement of D^* mesons from ZEUS [2] and to results from the H1 collaboration based on inclusive lifetime tagging (VTA) [3]. The previous results were corrected to the Q^{\pm} values of the present analysis, using the NLO theory. The agreement of the different data sets, obtained with different charm tagging techniques, is good. At high Q^\ast , the precision of present data is similar or better than for the previous results. The NLO QCD calculations are also shown.

Figure [5](#page-30-0) shows the extracted F_2^{ω} from this analysis and also a previous H1 result [3], corrected to the reference Q^π values used in the present analysis. The two data sets are in good agreement. The precision of the present measurement is similar to that of the H1 data at high Q² . The QCD al
ulations are also shown.

The structure functions F_2^{α} and F_2^{α} are also presented in Figs. [6](#page-31-0) and [7](#page-32-0) as functions of Q^{\star} for fixed values of $x,$ compared to previous results corrected to the same reference x used in the present analysis.

² The ee
ts of the individual sour
es of systemati and theoreti
al un
ertainty are also available from http://www-zeus.desy.de/public_results/functiondb.php?id=ZEUS-pub-09-003.

11 Summary

The production of charm and beauty quarks was measured in DIS using their decay into muons. Total and differential cross sections for muons from c and b decays were measured in the kinematic region

$$
Q^2 > 20 \text{ GeV}^2; \ 0.01 < y < 0.7; \ p_T^{\mu} > 1.5 \text{ GeV}; \ -1.6 < \eta^{\mu} < 2.3
$$

 $\overline{}$

and compared to NLO QCD calculations. The agreement is good for charm. Beauty is about a factor two above the central QCD prediction although still compatible within statisti
al and systemati un
ertainties. The heavy quark ontribution to the proton structure function F_2 was also measured and found to agree well with other measurements based on independent tecnniques. For $Q^2 \geq 00 \ {\rm GeV}$ the present results are of comparable or higher pre
ision than those previously existing.

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| p_T^{μ} | $d\sigma^c/dp_T^{\mu}$ | $\Delta_{\text{stat.}}$ | $\Delta_{\rm syst.}$ | $d\sigma^b/dp_T^{\mu}$ | $\Delta_{\text{stat.}}$ | $\Delta_{\rm syst.}$ | $\rho_{c,b}$ |
|------------------|------------------------|----------------------------|--|------------------------|----------------------------|--------------------------|--------------|
| (GeV) | | (pb/GeV) | | | (pb/GeV) | | |
| 1.5: 2.5 | 113 | ± 10 | $+21$ -23 | 48 | ± 8 | $+15$ $-13\,$ | -0.48 |
| 2.5: 3.5 | 32.8 | ± 3.8 | $+5.7$ -5.4 | 15.4 | ± 2.7 | $+4.1$ -2.8 | -0.46 |
| 5.0 3.5: | 6.0 | ± 1.4 | $+1.4$ -1.6 | 6.3 | ± 1.1 | $+0.9$ $\!-0.7$ | -0.48 |
| 5.0 : 10.0 | 0.97 | ± 0.21 | $+0.13$ -0.20 | 0.76 | ± 0.22 | $+0.10$ -0.15 | -0.45 |
| η^{μ} | $d\sigma^c/d\eta^\mu$ | $\Delta_{\text{stat.}}$ | $\Delta_{\rm syst.}$ | $d\sigma^b/d\eta^\mu$ | $\Delta_{\text{stat.}}$ | $\Delta_{\rm syst.}$ | $\rho_{c,b}$ |
| | | (pb) | | | (pb) | | |
| $-1.60: -0.90$ | 20.4 | ± 3.3 | $+4.2$ -4.1 | $5.0\,$ | ± 2.0 | $+1.9$ -1.6 | -0.36 |
| $-0.90: -0.40$ | 40.7 | ± 6.0 | $+7.7$ -8.0 | 13.6 | ± 3.5 | $+4.1$ -1.9 | -0.20 |
| $-0.40 : +0.00$ | 60.9 | ± 7.8 | $+11.8$ -14.2 | 17.3 | ± 4.8 | $+4.9$ $-3.5\,$ | -0.37 |
| $+0.00 : +0.50$ | 67.0 | ± 7.1 | $+10.2$ -12.3 | 21.2 | ± 4.4 | $+6.4$ -3.6 | -0.42 |
| $+0.50 : +1.48$ | 47.7 | ± 6.4 | $+8.9$ -8.8 | 20.7 | ± 4.3 | | -0.49 |
| $+1.48 : +2.30$ | 33.4 | ± 10.0 | $+15.3$ -8.9 | 16.4 | ± 6.9 | $+5.7$ -8.4 | -0.41 |
| | | | | | | | |
| Q^2 | $d\sigma^c/dQ^2$ | $\Delta_{\text{stat.}}$ | $\Delta_{\rm syst.}$ | $d\sigma^b/dQ^2$ | $\Delta_{\text{stat.}}$ | $\Delta_{\rm syst.}$ | $\rho_{c,b}$ |
| (GeV^2) | | (pb/GeV^2) | | | (pb/GeV^2) | | |
| 20: 40 | 3.43 | ± 0.40 | $+0.72$ -0.66 | 1.46 | ± 0.24 | $+0.30$ -0.39 | -0.44 |
| $40:$ 80 | 1.22 | ± 0.13 | $+0.18$ -0.22 | 0.546 | ±0.086 | $+0.109$ -0.098 | -0.41 |
| 80: 200 | 0.289 | ± 0.031 | $+0.053$ -0.054 | 0.124 | ± 0.023 | $+0.020$ -0.019 | -0.36 |
| 200 : 500 | 0.0447 | ± 0.0071 | $+0.0050$ -0.0083 | 0.0131 | ± 0.0049 | $+0.0035$ -0.0024 | -0.47 |
| 500:10000 | 0.00063 | ± 0.00013 | $\begin{array}{c} +0.00014 \\[-4pt] -0.00010\end{array}$ | 0.00013 | ± 0.00008 | $+0.00005$ -0.00003 | -0.38 |
| \boldsymbol{x} | $d\sigma^c/dx$ | $\Delta_{\text{stat.}}$ | $\Delta_{\rm syst.}$ | $d\sigma^b/dx$ | $\Delta_{\text{stat.}}$ | $\Delta_{\rm syst.}$ | $\rho_{c,b}$ |
| | | (nb) | | | (nb) | | |
| 0.0003 : 0.0010 | 35.3 | ± 5.6 | $+10.2$ -6.2 | 17.4 | ± 3.9 | $+3.5$ -3.6 | -0.16 |
| 0.0010 : 0.0020 | 35.2 | ± 4.1 | $+4.6$ -7.1 | 12.4 | ± 2.6 | $+2.7$ -3.0 | -0.39 |
| 0.0020 : 0.0040 | 16.1 | ± 2.2 | $+3.8$ -3.7 | 8.0 | ± 1.4 | $+1.6$ -1.2 | -0.51 |
| 0.0040 : 0.0100 | 7.38 | ± 0.72 | $+1.22$ -1.30 | 2.04 | ± 0.45 | $+0.52$ -0.39 | -0.45 |

Table 1: Muon dierential ross se
tions for harm and beauty as a fun
tion of η^{μ} , p_T^{μ} $T_{T},~Q$ and x. The last column shows the statistical correlation coefficient between harm and beauty.

| bin | Q^2 | \mathcal{X} | σ^c | $\Delta_{\text{stat.}}$ | $\Delta_{\rm syst.}$ | σ^b | $\Delta_{\text{stat.}}$ | $\Delta_{\rm syst.}$ | $\rho_{c,b}$ |
|----------------|------------|-----------------|-----------------|-------------------------|----------------------|------------|-------------------------|----------------------|--------------|
| | (GeV^2) | | (pb) | | | | (pb) | | |
| $\mathbf{1}$ | 60 20: | 0.0003:0.0012 | 32.9 | ± 4.6 | $+8.1$ -5.9 | 13.9 | ± 2.9 | $+3.2$ -2.3 | -0.29 |
| $\overline{2}$ | 20: 60 | 0.0012:0.0020 | 17.7 | ± 3.1 | $+1.9$ -4.9 | 5.7 | ± 2.0 | $+1.4$ -1.2 | -0.42 |
| 3 | 60 20: | 0.0020 : 0.0035 | 16.2 | ± 3.3 | $+3.7$ -3.0 | 5.5 | ± 2.0 | $+1.8$ -1.6 | -0.51 |
| $\overline{4}$ | 60 20: | 0.0035:0.0060 | 35.1 | ± 5.7 | $+10.9$ -7.2 | 7.9 | ± 3.6 | $+4.2$ -4.0 | -0.56 |
| $\overline{5}$ | 60: 400 | 0.0009 : 0.0035 | 17.2 | ± 2.7 | $+3.8$ -2.7 | 8.8 | ± 1.9 | $+1.6$ -1.4 | -0.38 |
| 6 | 400 60: | 0.0035:0.0070 | 18.4 | ± 2.3 | $+3.0$ -3.4 | 4.2 | ± 1.5 | $+1.2$ -0.9 | -0.35 |
| $\overline{7}$ | 60: 400 | 0.0070 : 0.0400 | 33.6 | ± 3.5 | $+6.1$ -6.4 | 8.6 | ± 2.3 | $+2.1$ -2.1 | -0.46 |
| 8 | 400:10000 | 0.0050 : 1.0000 | 7.6 | ± 1.5 | $+1.2$ -1.4 | 1.6 | ± 0.9 | $+0.4$ -0.4 | -0.45 |

Table 2: Muon cross secuons for charm and beauty in bins of Q^2 and x. The last olumn shows the statisti
al orrelation oeÆ
ient between harm and beauty.

| bin | Q^2 (GeV^2) | \mathcal{X} | $F_2^{c\bar{c}}$ | $\Delta_{\text{stat.}}$ | $\Delta_{\rm syst.}$ | Δ_{theo} | $\mathcal A$ | C_L |
|----------------|--------------------|---------------|------------------|-------------------------|----------------------|------------------------|--------------|-------|
| 1 | 30 | 0.0008 | 0.318 | ± 0.044 | $+0.078$ -0.057 | $+0.061$ -0.042 | 0.096 | 0.980 |
| $\overline{2}$ | 30 | 0.0016 | 0.219 | ± 0.038 | $+0.024$ -0.061 | $+0.043$ -0.016 | 0.114 | 0.996 |
| 3 | 30 | 0.0025 | 0.176 | ± 0.036 | $+0.040$ -0.033 | $+0.032$ -0.021 | 0.113 | 0.998 |
| 4 | 30 | 0.0055 | 0.143 | ± 0.023 | $+0.044$ -0.029 | $+0.028$ -0.009 | 0.096 | 1.000 |
| 5 | 130 | 0.0025 | 0.298 | ± 0.047 | $+0.066$ -0.046 | $+0.044$ -0.025 | 0.175 | 0.955 |
| 6 | 130 | 0.0055 | 0.228 | ± 0.029 | $+0.037$ -0.042 | $+0.030$ -0.015 | 0.220 | 0.993 |
| 7 | 130 | 0.0130 | 0.151 | ± 0.016 | $+0.027$ -0.029 | $+0.021$ -0.011 | 0.209 | 0.999 |
| 8 | 1000 | 0.0300 | 0.114 | ± 0.023 | $+0.018$ -0.021 | $+0.010$ -0.007 | 0.371 | 0.987 |

Table 3: The structure function $\mathbf{r}_2(x, Q)$. The last two columns show the muon eptan en and the longitudinal structure for the longitudinal structure function, and the longitudinal structure C_L .

| bin | Q^2 (GeV ²) | \mathcal{X} | $F_2^{b\bar{b}}$ | $\Delta_{\text{stat.}}$ | $\Delta_{\rm syst.}$ | Δ_{theo} | $\mathcal A$ | C_L |
|----------------|---------------------------|---------------|------------------|-------------------------|------------------------|------------------------|--------------|-------|
| 1 | 30 | 0.0008 | 0.0220 | ± 0.0047 | $+0.0049$ -0.0037 | $+0.0011$ -0.0010 | 0.260 | 0.992 |
| $\overline{2}$ | 30 | 0.0016 | 0.0131 | ± 0.0047 | $+0.0032$ -0.0028 | $+0.0009$ -0.0003 | 0.264 | 0.998 |
| 3 | 30 | 0.0025 | 0.0114 | ± 0.0043 | $+0.0037$ -0.0034 | $+0.0005$ -0.0004 | 0.251 | 0.999 |
| 4 | 30 | 0.0055 | 0.0080 | ± 0.0036 | $+0.0041$ -0.0041 | $+0.0004$ -0.0003 | 0.189 | 1.000 |
| 5 | 130 | 0.0025 | 0.0489 | ± 0.0105 | $+0.0088$ -0.0076 | $+0.0024$ -0.0018 | 0.300 | 0.962 |
| 6 | 130 | 0.0055 | 0.0175 | ± 0.0064 | $+0.0052$ -0.0039 | $+0.0007$ -0.0007 | 0.319 | 0.994 |
| $\overline{7}$ | 130 | 0.0130 | 0.0149 | ± 0.0039 | $+0.0037$ -0.0037 | $+0.0007$ -0.0006 | 0.281 | 0.999 |
| 8 | 1000 | 0.0300 | 0.0104 | ± 0.0061 | $+0.0028$ -0.0025 | $+0.0004$ -0.0004 | 0.420 | 0.983 |

Table 4: The structure function $F_2^{\omega}(x, Q^2)$. The last two columns show the muon erre tion for the longitudinal structure for the longitudinal structure function, and the longitudinal structur $\mathcal{C}_L.$

Figure 1: Distributions of (a) p_T in $_{T}$, (0) 0, (c) p_{T} for the selected sample of muons in DIS, and of (d) p_T^{ref} for a signal-enriched subsample with p_T^{ref} Γ \sim 2 GeV. and either a muon in \widehat{FMUON} or $\delta > 0.01$ cm. The data (points) are compared to the MC expectation (solid line) with the normalisation of the c (dotted line), b (shaded histogram) and light flavours (dashed line), LF, components obtained from the global fit. The error bars correspond to the square root of the number of entries.

Figure 2: Distributions of (a) p_T^r T_f , (b) η^{μ} , (c) p_T^{μ} T_f , (a) $(L - F_Z)_{\text{tot}},$ (e) Q_{Σ} and that in the selection in District of muons in Selection are the data (points) and selection in District the da to the MC expectation with the normalisation of the c, b and light flavours, LF , $components obtained from the global fit.$

Figure 3: Differential muon cross sections for c and b as a function of (a) p_T^r , (b) η^{μ} , (c) Q^2 , and (d) x. The inner error bars show the statistical uncertainty while the outer error bars show the systematic and statistical uncertainties added in quadrature. The bands show the NLO QCD predictions obtained with the HVQDIS program and the corresponding uncertainties. The differential cross sections from RAPGAP, scaled by the factors corresponding to the result of the global fit $(1.04$ for c and 2.27 for b), are also shown.

r igure 4: The structure function r_2 (fined symbols) compared to previous results (open symbols) and to the NLO QCD predi
tions in the FFNS using the ZEUS-S PDF fit. The inner error bars are the statistical uncertainty while the outer bars represent the statistical, systematic and theoretical uncertainties added in quadrature. The band represents the uncertainty on the NLO QCD prediction. Previous aata nave been correctea to the reference ω values used in this analysis. ZEUS D $500 \rightarrow 1000$ GeV $^{\circ}$; H1 VTA 25 \rightarrow 30, 200 \rightarrow 130, 650 \rightarrow 1000 GeV $^{\circ}$.

Figure 5: The structure function $F_2^{\nu\sigma}$ (filled symbols) compared to previous results (open symbols) and to the NLO QCD predi
tions in the FFNS using the ZEUS-S PDF fit. The inner error bars are the statistical uncertainty while the outer bars represent the statistical, systematic and theoretical uncertainties added in quadrature. The band represents the uncertainty on the NLO QCD prediction. Previous aata nave been corrected to the reference Q^- values used in this analysis: $z_0 \rightarrow z_0$, $200 \rightarrow 130$, 050 $\rightarrow 1000$ GeV $^{-1}$.

r igure $\boldsymbol{\sigma}$: The structure function \boldsymbol{r}_2 (futed symbols) piotied as a function of Q ⁻ for fixed x values. The curves represent the NLO QCD predictions in the FFNS using the ZEUS-S PDF fit. The inner error bars are the statistical uncertainty while the outer bars represent the statistical, systematic and theoretical uncertainties added in quadrature. The band represents the uncertainty on the NLO QCD prediction. A selection of previous data (open symbols) is also shown, corrected to the reference x values used in this analysis: ZEUS D : 0.001 \rightarrow 0.0000, 0.0015 \rightarrow 0.0010, $0.003 \rightarrow 0.0025, 0.006 \rightarrow 0.0055, 0.012 \rightarrow 0.013$; H1 VTX: $0.0005 \rightarrow 0.0008$, $0.002 \rightarrow 0.0025, 0.005 \rightarrow 0.0055, 0.032 \rightarrow 0.030.$

Figure 7: The structure function F_2^{∞} (filled symbols) plotted as a function of Q^2 for xed x values. The urves represent the NLO QCD predi
tions in the FFNS using the ZEUS-S PDF fit. The inner error bars are the statistical uncertainty while the outer bars represent the statistical, systematic and theoretical uncertainties added in quadrature. The band represents the uncertainty on the NLO QCD prediction. All the previous data (open symbols) are also shown, corrected to the reference x values used in this analysis: $0.0005 \to 0.0008$, $0.002 \to 0.0025$, $0.005 \to 0.0055$, $0.032 \rightarrow 0.030$.

Appendix: Tables of systematic and theoretical uncertainties

| Syst. | | | | $F_2^{c\bar{c}}$ | bin | | | | | | | $F_2^{b\bar{b}}$ | bin | | | |
|-----------------|------------------|----------------|-----------------|------------------|------------------|------------------|-----------------|----------------|------------------|----------------|----------------|------------------|------------------|------------------|------------------|------------------|
| | $\mathbf{1}$ | $\overline{2}$ | 3 | $\overline{4}$ | $\overline{5}$ | $\boldsymbol{6}$ | 7 | 8 | $\mathbf{1}$ | $\overline{2}$ | 3 | $\overline{4}$ | $\bf 5$ | 6 | 7 | 8 |
| 1a | -5 | -6 | -6 | -4 | -6 | -6 | -6 | -6 | -6 | -5 | -2 | $\overline{7}$ | -6 | -6 | -2 | -5 |
| 1 _b | $\,6\,$ | $\overline{7}$ | $\overline{6}$ | $\,4\,$ | $\,$ 6 $\,$ | $\,6$ | $\sqrt{6}$ | $\overline{7}$ | $\overline{7}$ | $\bf 5$ | $\mathbf{1}$ | -7 | $\,6$ | $\boldsymbol{6}$ | $\mathbf{1}$ | $\overline{4}$ |
| 2a | $\boldsymbol{0}$ | $\mathbf{1}$ | -1 | -6 | $\mathbf 1$ | $\overline{0}$ | -1 | $\mathbf{1}$ | -2 | -6 | -12 | -37 | -2 | -4 | -14 | -6 |
| 2 _b | $\overline{0}$ | -1 | $\mathbf{1}$ | $\rm 5$ | -1 | $\overline{0}$ | $\mathbf{1}$ | -1 | $\sqrt{2}$ | $\rm 5$ | 11 | 43 | $\sqrt{2}$ | 3 | $14\,$ | $\boldsymbol{6}$ |
| 3a | -3 | -2 | -3 | -3 | -4 | -3 | -2 | -2 | $\overline{0}$ | -2 | $\overline{0}$ | -8 | $\,1\,$ | $\mathbf{1}$ | -2 | -3 |
| 3 _b | $\boldsymbol{3}$ | $\overline{2}$ | 3 | $\overline{4}$ | $\overline{4}$ | 3 | $\overline{2}$ | $\mathbf{1}$ | $\boldsymbol{0}$ | 3 | $\mathbf{1}$ | 11 | -1 | -1 | $\overline{4}$ | $\overline{5}$ |
| 4a | $\overline{2}$ | -11 | 8 | -3 | -1 | -6 | -6 | -9 | $\sqrt{2}$ | $\overline{7}$ | -8 | 14 | -7 | 10 | $\mathbf{1}$ | -8 |
| 4 _b | -2 | -1 | $\overline{2}$ | $\overline{5}$ | 15 | $\sqrt{2}$ | $\overline{5}$ | 12 | $\overline{9}$ | -9 | -8 | 13 | -7 | 11 | $\overline{0}$ | -4 |
| 5a | $\sqrt{4}$ | $\overline{4}$ | $\overline{17}$ | $\overline{20}$ | $\boldsymbol{9}$ | 11 | $\overline{12}$ | 3 | $\sqrt{2}$ | -3 | $\overline{0}$ | $\overline{5}$ | $\overline{-2}$ | $\overline{4}$ | -6 | 3 |
| 5 _b | -4 | -20 | -10 | -15 | -1 | $\mbox{--}9$ | -11 | -2 | $\bf 5$ | $1\,1$ | -1 | $10\,$ | $\textbf{-3}$ | -9 | 3 | -5 |
| 6a | 19 | -5 | $\overline{1}$ | $\mathbf{1}$ | $\overline{0}$ | -2 | -10 | $\overline{0}$ | $\overline{3}$ | $\overline{5}$ | -13 | -28 | -2 | -9 | -3 | -7 |
| 6 _b | -9 | $\overline{0}$ | 3 | 19 | $\,4\,$ | $\sqrt{2}$ | 8 | 3 | $\sqrt{6}$ | -3 | 22 | 3 | $\sqrt{2}$ | 11 | -1 | $\overline{4}$ |
| $\overline{7}$ | $\,8\,$ | -5 | -2 | $\,1\,$ | -5 | $^{\rm -4}$ | $\overline{4}$ | $\overline{4}$ | $\,1$ | -8 | $\overline{7}$ | -8 | -4 | 11 | -16 | -9 |
| 8a | $\overline{0}$ | -2 | -1 | $\mathbf{1}$ | $\overline{0}$ | $\sqrt{2}$ | -1 | -3 | 11 | 6 | -4 | -1 | 8 | $\overline{6}$ | 11 | 21 |
| 8 _b | $\boldsymbol{0}$ | $\overline{4}$ | -3 | $\sqrt{3}$ | $\sqrt{3}$ | $\overline{0}$ | -3 | $\overline{4}$ | -11 | -10 | -5 | -10 | -5 | -7 | -1 | -16 |
| 9a | $\overline{2}$ | -1 | -4 | $\overline{1}$ | $\overline{0}$ | -1 | $\overline{-2}$ | -1 | -5 | $\overline{7}$ | 14 | $\overline{2}$ | $\overline{5}$ | 10 | 8 | $\overline{6}$ |
| 9 _b | $^{\rm -1}$ | $\,1\,$ | $\overline{3}$ | -1 | $\overline{0}$ | $\mathbf{1}$ | $\mathbf{1}$ | $\overline{0}$ | $\,4\,$ | -4 | -9 | -1 | -3 | -6 | -5 | -3 |
| 10a | -2 | $\overline{4}$ | $\overline{1}$ | $\overline{1}$ | -2 | -1 | $\overline{0}$ | $\overline{0}$ | -1 | -4 | -1 | -1 | -1 | -1 | $\sqrt{2}$ | $\mathbf{1}$ |
| 10 _b | $\,1\,$ | -5 | $\overline{0}$ | $\sqrt{2}$ | -2 | -1 | $\overline{2}$ | -1 | -4 | $\overline{3}$ | $\overline{4}$ | -5 | $\boldsymbol{6}$ | -6 | $\boldsymbol{0}$ | $\overline{5}$ |
| 11a | $\overline{0}$ | -1 | 3 | $\overline{9}$ | $\overline{6}$ | -2 | $\mathbf{1}$ | $\overline{0}$ | -5 | $\sqrt{6}$ | 11 | -8 | -3 | -2 | -1 | 3 |
| 11 _b | $\boldsymbol{0}$ | -7 | -9 | -4 | $\overline{2}$ | $\sqrt{2}$ | $\overline{0}$ | $\overline{0}$ | $\mathbf{1}$ | $\overline{5}$ | 3 | $\,$ 6 $\,$ | $^{\rm -2}$ | -3 | $\mathbf{1}$ | $\overline{2}$ |
| 12a | -3 | $\overline{0}$ | -2 | $\boldsymbol{0}$ | -3 | -3 | -2 | θ | $\overline{2}$ | -2 | $\overline{2}$ | -7 | $\overline{4}$ | $\boldsymbol{6}$ | $\overline{4}$ | $\overline{5}$ |
| 12 _b | $\sqrt{2}$ | $\overline{0}$ | $\mathbf{1}$ | -1 | $\overline{2}$ | $\sqrt{2}$ | $\overline{2}$ | -1 | -1 | $\overline{2}$ | -1 | 9 | -3 | -5 | -3 | -3 |
| 13 | -1 | -1 | -2 | $\mathbf{1}$ | -2 | $\overline{0}$ | -1 | $\overline{0}$ | $\boldsymbol{9}$ | 10 | $\overline{5}$ | -2 | $\boldsymbol{9}$ | $\overline{5}$ | $\sqrt{6}$ | $\mathbf{1}$ |
| 14a | $\,6\,$ | $\overline{1}$ | $\overline{3}$ | $\mathbf{1}$ | $\overline{4}$ | $\overline{6}$ | $\overline{3}$ | $\overline{0}$ | $\overline{4}$ | $\overline{5}$ | $\overline{5}$ | $\overline{3}$ | -2 | -8 | $\overline{6}$ | 8 |
| 14 _b | -12 | -7 | -8 | -9 | -11 | $\textbf{-}12$ | -7 | -10 | -6 | -8 | -11 | $\sqrt{4}$ | $\sqrt{3}$ | 12 | -6 | $\overline{2}$ |
| 15a | $^{\rm -3}$ | -3 | -3 | -2 | -3 | -3 | -3 | -3 | $\textbf{-3}$ | -2 | -1 | 3 | -3 | -2 | -1 | -2 |
| 15 _b | $\overline{3}$ | 3 | 3 | $\overline{2}$ | 3 | $\overline{3}$ | 3 | 3 | $\overline{3}$ | $\overline{2}$ | $\mathbf 1$ | -3 | 3 | $\overline{2}$ | $\,1$ | $\overline{2}$ |
| 16 | $\sqrt{6}$ | -2 | $\overline{5}$ | -5 | $\overline{4}$ | 3 | -2 | -8 | $\mathbf{1}$ | $\overline{6}$ | -12 | -5 | $\overline{0}$ | -6 | $\overline{5}$ | $\overline{2}$ |
| 17a | -3 | -3 | -3 | -3 | -3 | -3 | -3 | -3 | -3 | -3 | -3 | -3 | -3 | -3 | -3 | -3 |
| 17 _b | $\overline{3}$ | 3 | 3 | 3 | 3 | $\overline{3}$ | 3 | 3 | $\overline{3}$ | 3 | 3 | 3 | 3 | 3 | $\overline{3}$ | 3 |

Table 5: Systematic uncertainties of the r_2^2 and r_2^2 measurements. The first orintetion gives the systematic sentences in Sentence in September 2013 November 1997 - 1997 - 1998 - 1998 - 1 and "b" corresponding to variations in opposite directions. The other columns list the effect of each variation on the measurements in percent.

| Syst. | $F_2^{c\bar{c}}$ bin | | | | | | | | | $F_2^{b\bar{b}}$ bin | | | | | | |
|--------------------------|----------------------|----------------|----------------|----------------|------------|------------------|----------------|----------------|----------------|----------------------|----------------|------------------|----------------|----------------|----------------|----------------|
| | 1 | $\sqrt{2}$ | 3 | $\overline{4}$ | $\bf 5$ | $\boldsymbol{6}$ | $\overline{7}$ | 8 | 1 | $\sqrt{2}$ | 3 | 4 | $\rm 5$ | 6 | 7 | 8 |
| $\mu_F \times 2$ | $\overline{4}$ | 3 | 1 | $\overline{2}$ | 1 | 1 | $\overline{0}$ | $\overline{0}$ | $\mathbf{1}$ | $\sqrt{2}$ | $\overline{0}$ | -1 | $\overline{0}$ | θ | -1 | Ω |
| $\sqrt{2}$ | $-8\,$ | -2 | -7 | θ | -4 | -2 | θ | $\mathbf{1}$ | -1 | $\boldsymbol{0}$ | -1 | $\boldsymbol{0}$ | $^{-1}$ | θ | 1 | Ω |
| $\mu_R \times 2$ | 1 | | -3 | -2 | -2 | -2 | -3 | -2 | $\overline{0}$ | | θ | -2 | θ | θ | -1 | -1 |
| /2 | -1 | $\overline{0}$ | $\overline{2}$ | $\,6\,$ | 1 | $\overline{2}$ | $\bf 5$ | 3 | -1 | 1 | 1 | 1 | 1 | θ | 1 | 1 |
| $m_q +$ | -8 | -5 | -3 | -2 | $-{\bf 3}$ | -1 | -1 | -2 | $-{\bf 2}$ | -1 | -1 | $\overline{0}$ | -1 | -1 | Ω | -1 |
| | $\bf 5$ | $\overline{4}$ | 3 | 3 | 3 | $\overline{2}$ | $\overline{2}$ | 1 | $\overline{2}$ | $\overline{2}$ | $\mathbf 1$ | $\overline{0}$ | 1 | | $\overline{2}$ | θ |
| PDF $+$ | $\overline{2}$ | | -1 | θ | 1 | θ | $\overline{2}$ | θ | $\overline{0}$ | 1 | -1 | -1 | θ | θ | -1 | -1 |
| $\overline{}$ | -1 | $\mathbf{1}$ | -2 | -1 | | $\overline{0}$ | $\overline{0}$ | θ | $\overline{0}$ | 1 | $\overline{0}$ | 1 | $\overline{0}$ | θ | 1 | Ω |
| CTEQ | $\overline{4}$ | 1 | —1 | | | $\overline{0}$ | $\overline{2}$ | $\overline{2}$ | $\overline{0}$ | $\mathbf{1}$ | -1 | 3 | θ | | $\overline{2}$ | |
| $\epsilon +$ | 16 | 17 | 17 | 17 | 13 | 12 | 12 | $\overline{7}$ | $\overline{2}$ | $\overline{4}$ | $\overline{2}$ | $\overline{2}$ | $\mathbf{3}$ | 3 | 3 | $\overline{2}$ |
| $\overline{}$ | -6 | -2 | -8 | -4 | -5 | -4 | -5 | -4 | -3 | -1 | -3 | -2 | -3 | -3 | -3 | -2 |
| $E + p_{\parallel}$ | $\overline{5}$ | 6 | $\overline{4}$ | $\overline{4}$ | 3 | 3 | $\overline{2}$ | θ | 3 | 5 | 3 | $\overline{2}$ | 3 | 3 | $\overline{2}$ | Ω |
| $\mathcal{B}+$ | -4 | 4 | | | 4 | | 4 | -4 | -2 | -2 | -2 | $^{-2}$ | -2 | -2 | -2 | -2 |
| | 4 | $\overline{4}$ | $\overline{4}$ | $\overline{4}$ | 4 | 4 | $\overline{4}$ | $\overline{4}$ | $\sqrt{2}$ | $\overline{2}$ | $\overline{2}$ | $\overline{2}$ | $\overline{2}$ | $\overline{2}$ | $\overline{2}$ | $\overline{2}$ |

Table 6: Theoretical uncertainties of the r_2^2 and r_2^2 measurements. The first column gives the parameter varied in the calculation as reported in Sections 2 and torisation (Fall) and renormalisation (Fall section) (Fall) and HQ α and HQ), the variation of the ZEUS PDF by its un
ertainty (PDF), the use of the CTEQ5 PDF (CTEQ), the Peterson fragmentation parameter (ϵ) , the use an alternative fragmentation variable $(E + p_{\parallel})$ and the SL branching ratio (B). The other columns list the effect of each variation on the measurements in percent.