

J/ψ polarization at Tevatron and LHC: Nonrelativistic-QCD factorization at the crossroads

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Abstract

We study the polarization observables of J/ψ hadroproduction at next-to-leading order within the factorization formalism of nonrelativistic quantum chromodynamics. We complete the present knowledge of the relativistic corrections by also providing the contribution due to the intermediate ${}^3P_J^{[8]}$ color-octet states at this order, which turns out to be quite significant. Exploiting the color-octet long-distance matrix elements previously extracted through a global fit to experimental data of unpolarized J/ψ production, we provide theoretical predictions in the helicity and Collins-Soper frames and compare them with data taken by CDF at Fermilab Tevatron I and II and by ALICE at CERN LHC. The notorious CDF J/ψ polarization anomaly familiar from leading-order analyses persists at the quantum level, while the situation looks promising for the LHC, which is bound to bring final clarification.

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While the overly successful experiments at the LHC are closing in on the Higgs boson and are systematically searching for signals of physics beyond the standard model (SM), we must not be carried away losing track of a longstanding, unresolved puzzle in quantum chromodynamics (QCD), the otherwise well-established $SU(3)$ gauge theory of the strong interactions, right in the core of the SM. In fact, despite concerted experimental and theoretical efforts ever since the discovery of the J/ψ meson in the November revolution of 1974 (The Nobel Prize in Physics 1976), the genuine mechanism underlying the production and decay of heavy quarkonia, which are QCD bound states of a heavy quark $Q = c, b$ and its antiparticle \bar{Q} , has remained mysterious.

Nonrelativistic QCD (NRQCD) [1] endowed with an appropriate factorization theorem, which was conjectured in a seminal work by Bodwin, Braaten, and Lepage [2] and explicitly proven through next-to-next-to-leading order [3], arguably constitutes the most probable candidate theory at the present time. This implies a separation of process-dependent short-distance coefficients, to be calculated perturbatively as expansions in the strong-coupling constant α_s , from supposedly universal long-distance matrix elements (LDMEs), to be extracted from experiment. The relative importance of the latter can be estimated by means of velocity scaling rules, which predict each of the LDMEs to scale with a definite power of the heavy-quark velocity v in the limit $v \ll 1$. In this way, the theoretical predictions are organized as double expansions in α_s and v . A crucial feature of this formalism is that the $Q\bar{Q}$ pair can at short distances be produced in any Fock state $n = {}^{2S+1}L_J^{[a]}$ with definite spin S , orbital angular momentum L , total angular momentum J , and color multiplicity $a = 1, 8$. In particular, this formalism predicts the existence of intermediate color-octet (CO) states in nature, which subsequently evolve into physical, color-singlet (CS) quarkonia by the nonperturbative emission of soft gluons. In the limit $v \rightarrow 0$, the traditional CS model (CSM) is recovered in the case of S -wave quarkonia. In the case of J/ψ production, the CSM prediction is based just on the ${}^3S_1^{[1]}$ CS state, while the leading relativistic corrections, of relative order $\mathcal{O}(v^4)$, are built up by the ${}^1S_0^{[8]}$, ${}^3S_1^{[8]}$, and ${}^3P_J^{[8]}$ ($J = 0, 1, 2$) CO states.

The CSM is not a complete theory, as may be understood by noticing that the NLO treatment of P -wave quarkonia is plagued by uncanceled infrared singularities, which are, however, properly removed in NRQCD. In a way, NRQCD factorization [2], appropriately improved at large transverse momenta p_T by systematic expansion in powers of m_Q^2/p_T^2 [4], is the only game in town, which makes its experimental verification such a matter of paramount importance and general interest [5].

The experimental test of NRQCD factorization [2] has been among the most urgent tasks on the agenda of the international quarkonium community for the past fifteen years [5] and, with high-quality data being so copiously harvested at the LHC, is now more tantalizing than ever. The present status of testing NRQCD factorization in charmonium production is as follows. As for the unpolarized J/ψ yield, NRQCD factorization has recently been consolidated at NLO by a global fit to the world's data of hadroproduction, photoproduction, two-photon scattering, and e^+e^- annihilation [6], which successfully pinned down the three CO LDMEs in compliance with the velocity scaling rules and impressively supported their universality (see Table 1 in Ref. [7]). On the other hand, the

Tevatron II [8] data alone can just fix two linear combinations of the three CO LDMEs [9,10], and the fit results of Ref. [9] are incompatible with Ref. [6], as discussed in Ref. [11]. As for the J/ψ polarization observables, a complete NLO NRQCD analysis has so far only been performed for photoproduction [7]. The agreement with recent data from DESY HERA [12] was found to be satisfactory at sufficiently large values of p_T , where nonperturbative soft-gluon effects are negligible, provided that diffractive events were eliminated by an appropriate acceptance cut. The overall χ^2 achieved at NLO in NRQCD turned out to be more than a factor of 2 below the value obtained at NLO in the CSM [13]. However, the case for NRQCD factorization appeared here to be not as convincing as for the unpolarized J/ψ yield [6].

In this Letter, we take the next—and possibly decisive—step in the worldwide endeavor to put NRQCD factorization to the test and scrutinize polarized J/ψ hadroproduction at NLO in NRQCD. Measurements by CDF in $p\bar{p}$ collisions with c.m. energy $\sqrt{s} = 1.8$ TeV [14] and $\sqrt{s} = 1.96$ TeV [15] at the Tevatron and by ALICE [16] in pp collisions with $\sqrt{s} = 7$ TeV at the LHC are waiting to be rigorously interpreted. Previous NLO analyses were confined to the CSM [17] or included only the $^1S_0^{[8]}$ and $^3S_1^{[8]}$ contributions [18], which are deducible by well-established techniques. We close this gap by providing also the $^3P_J^{[8]}$ contributions at NLO, which are expected to be significant numerically. Their calculation is far more intricate because the applications of the respective projection operators to the short-distance scattering amplitudes produce particularly lengthy expressions involving complicated tensor loop integrals and exhibiting an entangled pattern of infrared singularities. Technical details will be presented in a forthcoming publication.

The polarization of the J/ψ meson is conveniently analyzed experimentally by measuring the angular distribution of its leptonic decays, which is customarily parametrized using the three polarization observables λ_θ , λ_ϕ , and $\lambda_{\theta\phi}$, as

$$W(\theta, \phi) \propto 1 + \lambda_\theta \cos^2 \theta + \lambda_\phi \sin^2 \theta \cos(2\phi) + \lambda_{\theta\phi} \sin(2\theta) \cos \phi, \quad (1)$$

where θ and ϕ are respectively the polar and azimuthal angles of l^+ in the J/ψ rest frame. This definition depends on the choice of coordinate frame. In the experimental analyses [14,15,16], the helicity and Collins-Soper frames were employed, in which the polar axes point in the directions of $-(\vec{p}_p + \vec{p}_{\bar{p}})$ and $\vec{p}_p/|\vec{p}_p| - \vec{p}_{\bar{p}}/|\vec{p}_{\bar{p}}|$, respectively. The values $\lambda_\theta = 0, +1, -1$ correspond to unpolarized, fully transversely polarized, and fully longitudinally polarized J/ψ mesons, respectively. In Refs. [14,15], λ_θ is called α . Working in the spin density matrix formalism and denoting the z component of S by $i, j = 0, \pm 1$, we have

$$\lambda_\theta = \frac{d\sigma_{11} - d\sigma_{00}}{d\sigma_{11} + d\sigma_{00}}, \quad \lambda_\phi = \frac{d\sigma_{1,-1}}{d\sigma_{11} + d\sigma_{00}}, \quad \lambda_{\theta\phi} = \frac{\sqrt{2} \operatorname{Re} d\sigma_{10}}{d\sigma_{11} + d\sigma_{00}}, \quad (2)$$

where $d\sigma_{ij}$ is the ij component of the $p\bar{p} \rightarrow J/\psi + X$ differential cross section. An expression of $d\sigma_{ij}$ in terms of parton density functions (PDFs) and partonic spin density matrix elements may be found in Eq. (3) of Ref. [7].

In our numerical analysis, we adopt the CO LDME values from Table I of Ref. [7] along with $\langle \mathcal{O}^{J/\psi}(^3S_1^{[1]}) \rangle = 1.32 \text{ GeV}^3$ [19], take the charm-quark mass, which we renormalize

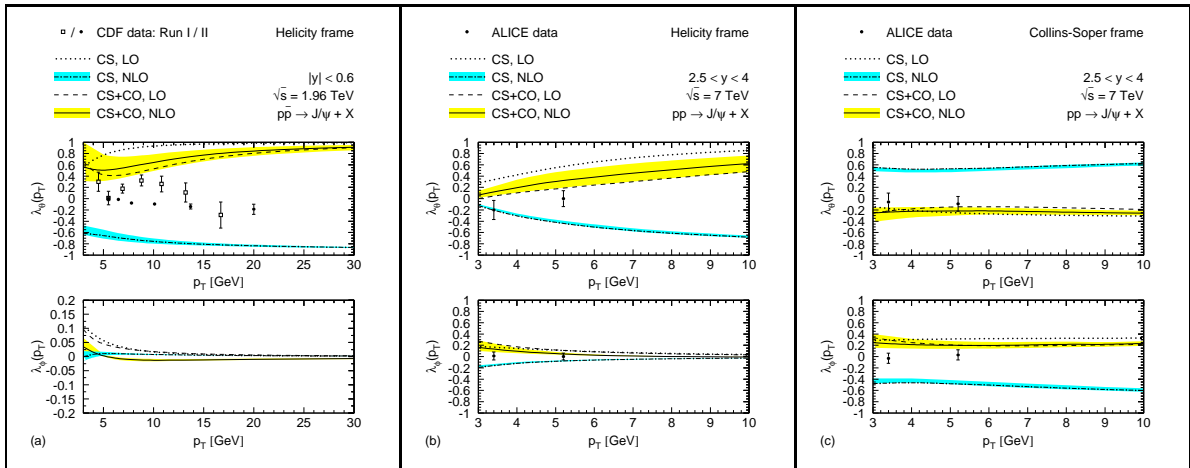


Figure 1: (color online) NLO NRQCD predictions (solid lines) for λ_θ and λ_ϕ as functions of p_T in the helicity and Collins-Soper frames including theoretical uncertainties (shaded/yellow bands) compared to CDF [14,15] and ALICE [16] data. For comparison, also the NLO CSM (dot-dashed lines) predictions including theoretical uncertainties (hatched/blue bands) as well as the LO NRQCD (dashed lines) and LO CSM (dotted lines) ones are shown.

according to the on-shell scheme, to be $m_c = 1.5$ GeV, and use the one-loop (two-loop) formula for $\alpha_s^{(n_f)}(\mu_r)$, with $n_f = 4$ active quark flavors, at LO (NLO). As for the proton PDFs, we use the CTEQ6L1 (CTEQ6M) set [20] at LO (NLO), which comes with an asymptotic scale parameter of $\Lambda_{\text{QCD}}^{(4)} = 215$ MeV (326 MeV). Our default choices for the $\overline{\text{MS}}$ renormalization, factorization, and NRQCD scales are $\mu_r = \mu_f = m_T$ and $\mu_\Lambda = m_c$, respectively, where $m_T = \sqrt{p_T^2 + 4m_c^2}$ is the J/ψ transverse mass. The theoretical uncertainty due to the lack of knowledge of corrections beyond NLO is estimated by varying μ_r , μ_f , and μ_Λ by a factor 2 up and down relative to their default values. In our NLO NRQCD predictions, we must also include the errors in the CO LDMEs, which reflect the errors on the experimental data included in the fit. To this end, we determine the maximum upward and downward shifts generated by independently varying their values according to Table I in Ref. [7] and add the resulting half-errors in quadrature to those due to scale variations.

In Fig. 1, we confront our NLO NRQCD predictions for λ_θ and λ_ϕ as functions of p_T in the helicity and Collins-Soper frames with the measurements by CDF [14,15] and ALICE [16]. Since the cross section ratios in Eq. (2) are very insensitive to the precise value of \sqrt{s} , we may safely overlay the data from $\sqrt{s} = 1.8$ TeV [14] with the predictions for $\sqrt{s} = 1.96$ TeV. For comparison, also the LO NRQCD as well as the LO and NLO CSM predictions are shown. In order to visualize the size of the NLO corrections to the hard-scattering cross sections, the LO predictions are evaluated with the same LDMEs. As in Ref. [6], we do not consider the range $p_T < 3$ GeV, where nonperturbative soft-gluon

radiation invalidates a fixed-order treatment. We observe that, in all the cases considered, the inclusion of the NLO corrections has a considerably less dramatic effect in NRQCD than in the CSM, where the normalizations and shapes of the various distributions are radically modified. This indicates that the perturbative expansion in α_s converges more rapidly in NRQCD than in the CSM. A similar observation has already been made for photoproduction [7]. Comparing the LO NRQCD prediction for λ_θ in Fig. 1(a) with the one referring to direct J/ψ production in Fig. 1(b) of Ref. [21], we encounter marked differences in normalization and shape, which mainly reflect the progress in our knowledge of the CO LDMEs during the dozen years between Ref. [21] and [6]. Comparing Figs. 1(a) and 1(b), we observe that, for $p_T \gg 2m_c$, the results are fairly stable when passing from the Tevatron to the LHC and from the central ($|y| < 0.6$) to the forward ($2.5 < y < 4$) rapidity region, as long as one stays in the helicity frame. However, switching from the helicity to the Collins-Soper frame has a radical impact on the various p_T distributions, as the comparison of Figs. 1(b) and 1(c) reveals. The most striking effect appears for λ_θ , where the NLO CSM and NRQCD results are, roughly speaking, inverted. As for λ_ϕ , the Collins-Soper frame clearly outperforms the helicity frame with regard to the power of NRQCD versus CSM discrimination. As expected, the theoretical uncertainties due to scale variations steadily decrease as the value of p_T increases, which just reflects asymptotic freedom.

Let us now compare experiment and theory. The Tevatron I data for λ_θ [14] systematically fall below the NLO NRQCD prediction and, unlike the latter, exhibit a downward trend for $p_T \gtrsim 10$ GeV, but their errors are too large for a firm conclusion. This is quite different for the Tevatron II data [15], which are rather precise and indicate that the J/ψ mesons are essentially unpolarized in the helicity frame, while NRQCD clearly predicts transverse polarization, with purity and precision steadily increasing with the value of p_T . A few caveats are in order here. While the CDF data cover prompt production, including the feed-down from the heavier χ_{cJ} and ψ' mesons, our predictions refer to direct production, devoid of feed-down. However, the inclusion of feed-down was found to have a minor effect on the p_T distribution of λ_θ at LO in NRQCD [21], which is expected to carry over to NLO. For $p_T < 12$ GeV, the measurements from Tevatron runs I [14] and II [15] are mutually incompatible, a feature that has never been satisfactorily clarified by the CDF Collaboration. Fortunately, the four LHC experiments are in a position to measure the J/ψ polarization with unprecedented precision, and ALICE has already presented first results for λ_θ and λ_ϕ [16], both in the helicity and Collins-Soper frames. We compare them with our NLO NRQCD predictions in Figs. 1(b) and 1(c), respectively, leaving out one data point in the p_T bin 2–3 GeV in each of the four cases. The degree of agreement is encouraging. All data points are at most one standard deviation away from the theoretical error bands; four of them even overlap with the latter. The agreement tends to improve with increasing value of p_T , as the influence of uncontrolled corrections beyond NLO fades. Except in the low- p_T bin of λ_θ in the helicity frame, the data clearly favor NRQCD over the CSM at NLO. However, also these comparisons have to be taken with a grain of salt, since, unlike our predictions, the ALICE data [16] also include J/ψ mesons from feed-down and B -meson decays. The fraction of J/ψ mesons from b -quark origin

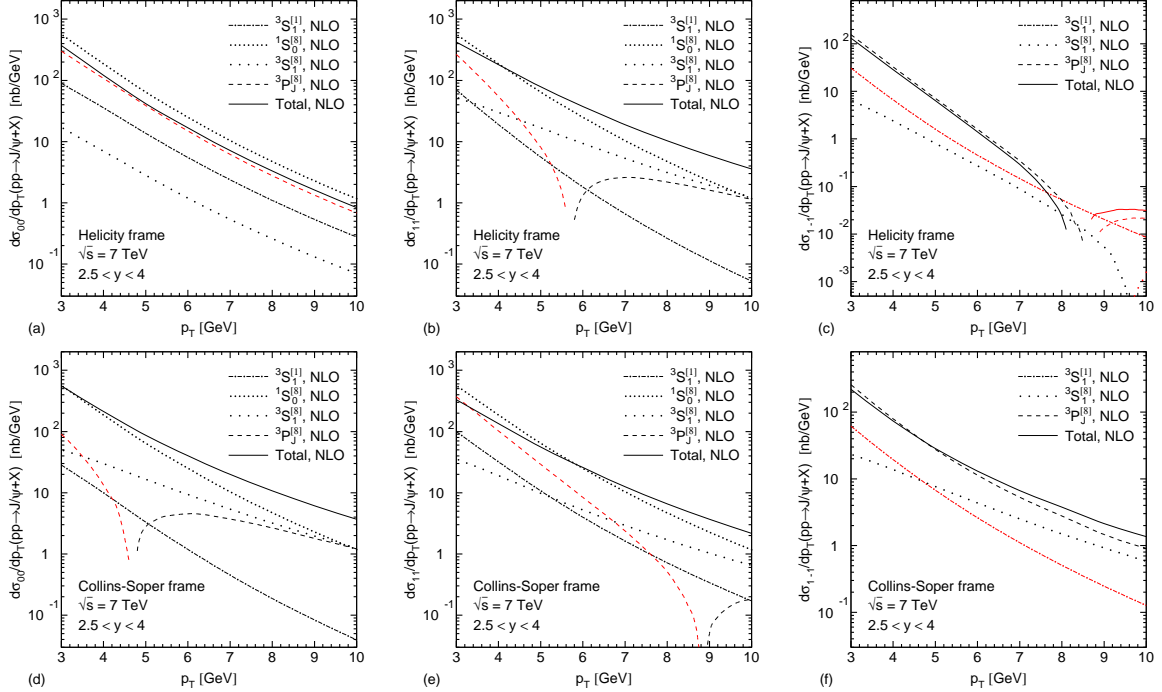


Figure 2: (color online) $d\sigma_{00}/dp_T$, $d\sigma_{11}/dp_T$, and $d\sigma_{1,-1}/dp_T$ for $pp \rightarrow J/\psi + X$ with $\sqrt{s} = 7$ TeV and $2.5 < y < 4$ in the helicity and Collins-Soper frames at NLO in NRQCD (solid lines) and their decompositions in the $^3S_1^{[1]}$ (dot-dashed lines), $^1S_0^{[8]}$ (dotted lines), $^3S_1^{[8]}$ (coarsely dotted lines), and $^3P_J^{[8]}$ (dashed lines) contributions. Negative values are marked red.

was measured by the LHCb Collaboration for unpolarized production to be below 15% in the p_T range considered here [22], so that their omission should have an effect negligible against the theoretical uncertainty.

In order to assess the relative importance of the individual $c\bar{c}$ Fock states n for λ_θ and λ_ϕ in the helicity and Collins-Soper frames, we detail their contributions to $d\sigma_{00}$, $d\sigma_{11}$, and $d\sigma_{1,-1}$ in Fig. 2. Note that the unpolarized cross section is recovered as $d\sigma_{00} + 2d\sigma_{11}$, while $d\sigma_{1,-1}$ is an auxiliary quantity, which is entitled to take on either sign and receives no contribution from the $^1S_0^{[8]}$ channel. As anticipated above, the previously unknown $^3P_J^{[8]}$ contributions play a dominant role in this game, and their omission is bound to yield meaningless results. As is familiar from the unpolarized case [6], the $^3P_J^{[8]}$ short-distance cross sections receive sizable NLO corrections that may even turn them negative beyond some values of p_T , as may be inferred from Figs. 2(b), (d), and (e) by recalling that our NLO value of $\langle \mathcal{O}^{J/\psi}(^3P_0^{[8]}) \rangle$ [6] is also negative. This is, however, unproblematic because a particular CO contribution represents an unphysical quantity depending on the choices of renormalization scheme and scale μ_Λ and is entitled to become negative as long as the full cross section remains positive.

At this point, we compare our results with the theoretical literature. We agree ¹ with the LO NRQCD results given in Eqs. (B26)–(B62) of Ref. [23]. We are able to nicely reproduce the LO and NLO ${}^3S_1^{[1]}$ and ${}^3S_1^{[8]}$ contributions to λ_θ shown as functions of p_T in Fig. 3 (9) of the first (second) paper in Ref. [17] and Fig. 4 of Ref. [18].

In conclusion, we presented the first complete NLO analysis of polarized J/ψ hadroproduction within NRQCD and, exploiting the knowledge of the CO LDMEs from a global fit of unpolarized J/ψ production data [6], thus managed to establish certainty about that the latest CDF measurement [15] is in severe conflict with NRQCD factorization [2]. As emphasized in Ref. [24], the measurement of λ_θ in the helicity frame alone provides only restricted access to the rich phenomenology of J/ψ polarization and might become ambiguous in want of statistics, in particular if the patches of solid angle in which simulations substitute data exceed a critical size. In this sense, the ALICE Collaboration [16] has made a first step into a bright future of heavy-quarkonium physics at the LHC, allowing for ultimate tests of NRQCD factorization.

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Note added. After the submission of this Letter, a preprint [25] appeared, in which λ_θ in the helicity frame is studied at NLO in NRQCD for J/ψ hadroproduction at the Tevatron. Adopting the LDME values specified in the first line of Table I in Ref. [25], we are able to reproduce the numerical results of Ref. [25]. Unfortunately, including the CDF data of Ref. [14,15] on top of those from Ref. [8], already used in Ref. [9], still does not allow for an independent determination of the three CO LDMEs, and the result is violently incompatible with the global fit of Ref. [6]. In particular, this set of CO LDMEs, as well as the two alternative ones specified in that table, are found [11] to yield NLO-NRQCD predictions for photoproduction which fail to describe the HERA data. As a consequence, the conclusions of Ref. [25] with regard to the compliance of the CDF measurements of λ_θ in the helicity frame [14,15] with NRQCD factorization at NLO are quite opposite to ours.

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¹In Eq. (B58) of Ref. [23], the factor $(4\pi\alpha_s)$ should be taken to the power 3.

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