

# Inclusive $B$ -Meson Production at the LHC in the GM-VFN Scheme

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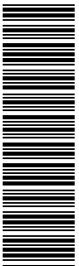
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## Abstract

We calculate the next-to-leading-order cross section for the inclusive production of  $B$  mesons in  $pp$  collisions in the general-mass variable-flavor-number scheme, an approach which takes into account the finite mass of the  $b$  quarks. We use realistic evolved nonperturbative fragmentation functions obtained from fits to  $e^+e^-$  data and compare our results for the transverse-momentum and rapidity distributions at a center-of-mass energy of 7 TeV with recent data from the CMS Collaboration at the CERN LHC. We find good agreement, in particular at large values of  $p_T$ .

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# 1 Introduction

Since the late eighties there has been much interest in the study of  $B$ -meson production in  $p\bar{p}$  and  $pp$  collisions at hadron colliders, both experimentally and theoretically. The first measurements were performed more than two decades ago by the UA1 Collaboration at the CERN  $S\bar{p}pS$  collider [1] operating at a center-of-mass energy of  $\sqrt{S} = 0.63$  TeV. More recent measurements were made by the CDF and D0 Collaborations at the Fermilab Tevatron running at  $\sqrt{S} = 1.8$  TeV [2, 3] and 1.96 TeV [4]. Just recently, the CMS Collaboration at the CERN LHC collider published first results for inclusive  $B^+$ - [5],  $B^0$ - [6], and  $B_s$ -meson [7] production in  $pp$  collisions at  $\sqrt{S} = 7$  TeV.  $B^+$  mesons were reconstructed via their decay  $B^+ \rightarrow J/\psi K^+$  followed by  $J/\psi \rightarrow \mu^+\mu^-$ , whereas  $B^0$  mesons were identified through the observation of  $J/\psi K_s^0$  final states with the subsequent decays  $J/\psi \rightarrow \mu^+\mu^-$  and  $K_s^0 \rightarrow \pi^+\pi^-$ . In the case of  $B_s$  mesons, the reconstructed final states were generated by the decay chain  $B_s \rightarrow J/\psi\phi$ ,  $J/\psi \rightarrow \mu^+\mu^-$ , and  $\phi \rightarrow K^+K^-$ . From all these measurements the differential cross sections  $d\sigma/dp_T$  and  $d\sigma/dy$  as well as the integrated cross section for  $p_T \geq 5$  GeV (for  $B^+$  and  $B^0$  mesons) or  $p_T \geq 8$  GeV (for  $B_s$  mesons) were reported.

The general-mass variable-flavor-number (GM-VFN) scheme provides a rigorous theoretical framework for the description of the inclusive production of single heavy-flavored hadrons, combining the fixed-flavor-number (FFN) [8] and zero-mass variable-flavor-number (ZM-VFN) [9] schemes, which are valid in complementary kinematic regions, in a unified approach that enjoys the virtues of both schemes and, at the same time, is bare of their flaws. Specifically, it resums large logarithms by the Dokshitzer-Gribov-Lipatov-Altarelli-Parisi (DGLAP) evolution of nonperturbative fragmentation functions (FFs), guarantees the universality of the latter as in the ZM-VFN scheme, and simultaneously retains the mass-dependent terms of the FFN scheme without additional theoretical assumptions. It was elaborated at next-to-leading order (NLO) for photoproduction [10] and hadroproduction [11] of charmed hadrons as well as for their production by  $e^+e^-$  annihilation [12]. It was also applied to obtain predictions for  $B$ -meson hadroproduction [13], which could be compared with recent CDF data [4]. An earlier implementation of such an interpolating scheme is the so-called fixed-order-next-to-leading-logarithm (FONLL) approach, in which the conventional cross section in the FFN scheme is linearly combined, with the help of a  $p_T$ -dependent weight function, with a suitably modified cross section in the ZM-VFN scheme implemented with perturbative FFs [14].

In Ref. [13], nonperturbative FFs for the transitions  $a \rightarrow B$ , where  $a$  is any parton, including  $b$  and  $\bar{b}$  quarks, were extracted at NLO in the  $\overline{\text{MS}}$  factorization scheme with  $n_f = 5$  flavors from the scaled-energy ( $x$ ) distributions  $d\sigma/dx$  of  $e^+e^- \rightarrow B + X$  measured by the ALEPH [15] and OPAL [16] Collaborations at the CERN LEP1 collider and by the SLD Collaboration [17] at the SLAC SLC collider. As explained in Ref. [13], these FFs may be consistently used in our GM-VFN framework. Working at NLO in the GM-VFN scheme with these  $B$ -meson FFs, we found excellent agreement with recent CDF measurements of  $d\sigma/dp_T$  for  $p\bar{p} \rightarrow B + X$  [4], especially in the upper  $p_T$  range,  $p_T \gtrsim 10$

GeV [13].

The content of this paper is as follows. In Sec. 2, we summarize our input choices of PDFs and  $B$ -meson FFs. In Sec. 3, we compare the predictions of the GM-VFN scheme with the CMS data from the recent LHC run at  $\sqrt{S} = 7$  TeV [5, 6, 7]. Our conclusions are given in Sec. 4.

## 2 Input PDFs and $B$ -meson FFs

As PDFs for the proton, we choose one of the most recent parametrizations of the CTEQ Collaboration, set CTEQ6.6M [18], which provides an improvement over the earlier version CTEQ6.5M. Both sets were obtained in the framework of a general-mass scheme using the input values  $m_c = 1.3$  GeV,  $m_b = 4.5$  GeV, and  $\alpha_s(m_Z) = 0.118$ . In both set, the  $b$ -quark PDF has its starting scale at  $\mu_0 = m_b$ .

The nonperturbative FFs describing the transition of the  $b$  and  $\bar{b}$  quarks into a  $B$  meson can be obtained only from experiment. In our earlier work on inclusive  $B$ -meson production at the Tevatron [13], we constructed such FFs using as input recent precise measurements of the cross section of inclusive  $B$ -meson production in  $e^+e^-$  annihilation obtained by the ALEPH [15], OPAL [16], and SLD [17] Collaborations.<sup>1</sup> These data were taken on the  $Z$ -boson resonance, so that finite- $m_b$  effects, being of relative order  $m_b^2/m_Z^2$ , are strongly suppressed, which means that we are in the asymptotic regime where the GM-VFN scheme is equivalent to the ZM-VFN scheme. The combined fit to the three data sets was performed using the NLO value  $\Lambda_{\overline{MS}}^{(5)} = 227$  MeV corresponding to  $\alpha_s^{(5)}(m_Z) = 0.1181$ , values adopted from Ref. [18]. The renormalization and factorization scales were chosen to be  $\mu_R = \mu_F = m_Z$ . In accordance with the chosen PDFs, the starting scale of the  $b \rightarrow B$  FF was taken to be  $\mu_0 = m_b$ , while the  $g, q \rightarrow B$  FFs, where  $q$  denotes the light quarks including the charm quark, were taken to vanish at  $\mu_F = \mu_0$ .

For fitting the data, we actually employed two different parametrizations for the  $b \rightarrow B$  FF at  $\mu_0 = m_b$ , namely the Peterson ansatz [20] and the simple power ansatz [21]. It turned out that the Peterson ansatz led to a very poor fit. Therefore, we shall use in this work only the FFs obtained with the power ansatz, whose parameters at the starting scale are listed in Table 1 of Ref. [13]. A comparison of the fit performed using this ansatz with the three input data sets may be found in Fig. 1 of that reference.

We note that the data from OPAL and SLD included all  $B$ -hadron final states, in particular those with  $\Lambda_b$  hadrons, while, in the ALEPH analysis, only final states with identified  $B^\pm$  and  $B^0$  mesons were taken into account. Our fit was based on the assumption that the FFs of all  $b$  hadrons had the same shape. The branching fraction of  $b \rightarrow B^+$  was taken equal to that of  $b \rightarrow B^0$  and fixed to 0.397. In our calculations for  $B_s$ -meson production to be presented below, we shall use the same FFs and rescale them by the factor

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<sup>1</sup> Recently, similar data became available also from the DELPHI Collaboration [19].

0.113/0.401, which uses the up-to-date values for the  $b \rightarrow B^+$  and  $b \rightarrow B_s$  branching fractions quoted by the Particle Data Group [22].

We should emphasize that, in the analysis of the available  $e^+e^-$  annihilation data, the charged and neutral  $B$  mesons were not separated. Furthermore, the charged states  $B^+$  and  $B^-$  could not be distinguished. The FFs obtained in Ref. [13] are, therefore, valid for the average of  $B^+$  and  $B^-$  and, similarly, for the average of  $B^0$  and  $\overline{B}^0$ .

The factorization scales related to the initial- and final-state singularities entering the PDFs and FFs, respectively, can in principle be chosen independently. We checked, however, that when estimating theoretical error bands by varying these scales by factors of 2 up and down, the extreme values are indeed obtained when the initial- and final-state factorization scales are identified. Our default choice of renormalization and factorization scales is  $\mu_R = \mu_F = m_T = \sqrt{p_T^2 + m_b^2}$ . Theoretical uncertainties will be estimated by setting  $\mu_R = \xi_R m_T$  and  $\mu_F = \xi_F m_T$ , and varying  $\xi_R$  and  $\xi_F$  about their default values  $\xi_R = \xi_F = 1$  by factors of 2 up and down, restricting the ratio to the range  $1/2 \leq \xi_R/\xi_F \leq 2$ .

### 3 Theoretical Predictions for $pp \rightarrow B + X$ and Comparisons with CMS Data

To obtain an overview of the  $p_T$  dependence of  $d\sigma/dp_T$ , we first show results for this observable, integrated over  $|y| \leq 2.4$ , for the case of  $B^+$  production in the GM-VFN scheme as described above. This differential cross section is shown in Fig. 1 (left) for  $p_T$  values between 5 and 30 GeV and in Fig. 1 (right) for larger  $p_T$  values, up to 100 GeV, where we expect data to come in the near future when the LHC experiments are accumulating more statistics.

In the  $p_T$  range between 5 and 30 GeV, the cross section falls off by three orders of magnitude. This is essentially due to the behavior of the PDFs as a function of the scaling variable  $x$  and less so from the behavior of the partonic cross sections. Towards low  $p_T$  values, both the upper edge of the error band and the cross section for the default choice of scales rise steadily with decreasing  $p_T$  value, down to  $p_T = 5$  GeV. This is caused by the scale dependence of the  $b$ -quark PDF and the FFs. With our choice of scales, they fade out and quench the cross section, leading to a turn-over of the  $p_T$  distributions only at  $p_T = 0$  and not already at some finite  $p_T$  value. The lower edge of the error band is obtained for  $\xi_F = 0.5$ . Here, both the  $b$ -quark PDF and the FFs vanish at  $p_T \approx 8$  GeV, corresponding to  $\mu_F = m_b = 4.5$  GeV. The line representing the lower edge of the error band therefore stops at this point.

The CMS Collaboration measured the differential cross section  $d\sigma/dp_T$  for the production of  $B^+$  mesons [5] (actually the average of  $B^+$  and  $B^-$  mesons), integrated over the  $y$  range  $|y| \leq 2.4$ , as a function of  $p_T$ . The measurement covered the  $p_T$  range from 5 GeV to