

On the Relevance of Sharp Gamma-Ray Features for Indirect Dark Matter Searches

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Gamma rays from the annihilation of dark matter particles in the Galactic halo provide a particularly promising means of indirectly detecting dark matter. Here, we demonstrate that pronounced spectral features at energies near the dark matter particles' mass, which are a generic prediction for most models, can significantly improve the sensitivity of gamma-ray telescopes to dark matter signals. We derive projected limits on such features (including the traditionally looked-for line signals) and show that they can be much more efficient in constraining the nature of dark matter than the model-independent broad spectral features expected at lower energies.

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I. INTRODUCTION

Indirect dark matter (DM) searches aim at seeing an excess in cosmic rays from the annihilation or decay of DM in the Galactic halo [1]. Gamma rays play a pronounced role in this respect because they are produced rather copiously and directly trace their sources as they propagate essentially unperturbed through the galaxy. Powerful currently operating telescopes like Fermi LAT [2], H.E.S.S. [3], MAGIC [4] or VERITAS [5] now start to constrain viable DM models and next generation instruments like the planned CTA [6] will be able to dig quite a bit into the underlying parameter space of particle physics models, in a way complementary to both direct DM detection and searches at the CERN LHC [7].

Very often, indirect searches focus on *secondary photons* from the fragmentation of annihilation products, mostly via $\pi^0 \rightarrow \gamma\gamma$. The resulting spectrum is rather model-independent and would manifest itself as a broad bump-like excess over the expected background at energies considerably lower than the DM mass m_χ . Convincingly claiming a DM detection based on the observation of such a feature-less signal will generically be difficult.

In many models, however, *pronounced spectral features* are expected at the kinematic endpoint $E_\gamma = m_\chi$ include monochromatic gamma-ray lines [8], sharp steps or cut-offs [9, 10] as well as pronounced bumps [11]. The type and strength of these features are intricately linked to the particle nature of DM; a detection would thus not

only allow a convincing discrimination from astrophysical backgrounds but also to determine important DM model parameters (in particular, but not necessarily limited to, the value of m_χ). So far, only line-signals have explicitly been searched for [12]—despite the fact that they are loop-suppressed and thus generically subdominant compared to other spectral signatures [11].

Here, we present a general method to search for such features and show that these, indeed, help significantly to discriminate DM signals from astrophysical backgrounds. This allows us to derive very competitive (projected) limits on both the annihilation rate and nature of DM, which we believe will be very useful for DM searches.

II. METHOD

The defining aspect of the above-mentioned spectral features in the DM-induced gamma-ray emission is an abrupt change of the flux as function of energy; in the extreme cases of gamma-ray lines or cut-offs, *e.g.*, the corresponding energy range would simply be given by the energy resolution $\Delta E/E$ of the instrument. The basic idea that we will adopt here, following traditional gamma-ray line searches [12], is therefore to concentrate the search for spectral features on a small sliding energy window $[E_0, E_1]$, with $E_0 < m_\chi < E_1$ and $\varepsilon \equiv E_1/E_0 \sim \mathcal{O}(1-10)$. An important advantage of using small values for ε is that gamma-ray fluxes with astrophysical origin can often be very well described by a simple power-law. In that case, a corresponding fit to the data allows an effective determination of the background at the statistical limit, greatly reducing uncertainties related to astrophysical sources.

For deriving constraints on spectral features within the sliding energy window, we will use a binned profile likelihood method [13]. To this end, we split $[E_0, E_1]$ in

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	$A_{\text{eff}}(1 \text{ TeV})$	$\Delta E/E(1 \text{ TeV})$	ϵ_p	t_{obs}
IACT1	0.18 km ²	15%	10 ⁻¹	50 h
IACT2	2.3 km ²	9%	10 ⁻²	100 h
IACT3	23 km ²	7%	10 ⁻³	5000 h

TABLE I: IACT benchmark models that, from top to bottom, roughly correspond to the H.E.S.S. [3], the future CTA [6] and the proposed DMA [7] telescope characteristics.

many energy bins ΔE_i and define a likelihood function $L(\boldsymbol{\mu}|\mathbf{c}) = \prod_i P_{\mu_i}(c_i)$, where μ_i (c_i) denotes the expected (observed) count number in bin i and P_{μ} is the Poisson probability distribution with mean μ . Introducing the background normalization β , its spectral slope γ and the normalization of the DM signal α , we have

$$\frac{\mu_i}{t_{\text{obs}}} = \int_{\Delta E_i} dE \int dE' \mathcal{D}_{E,E'} A_{\text{eff}}(E') \left[\alpha \frac{dN_{\chi}}{dE'} + \beta E'^{-\gamma} \right], \quad (1)$$

where t_{obs} is the time of observation, A_{eff} the effective area and $\mathcal{D}_{E,E'}$ the energy dispersion of the instrument (in the following taken to be Gaussian). Maximizing $L(\boldsymbol{\mu}|\mathbf{c})$ for a given data set \mathbf{c} results in best-fit values of the model parameters α , β and γ within the considered window $[E_0, E_1]$. *Upper limits* on the signal strength at the 95.5% C.L. can then be derived by increasing α from its best-fit value until $-2 \log L$ (maximized with respect to β and γ) has changed by 4. On the other hand, a *detection* at the 5σ level (neglecting trial factors) could be claimed if the best-fit $-2 \log L$ values for background-only and background-plus-signal fits differ by at least 25.

Our main assumption here is that the astrophysical background *locally* takes the form of a power law. Obviously, this approximation can break down in case of large window sizes ε , depending on the collected statistics and, to first order, on the intrinsic curvature of the background flux $\kappa \equiv d^2 \log(dJ_{\text{BG}}/dE)/(d \log E)^2$: a change in the spectral index by $\Delta\gamma$, e.g., implies roughly $|\kappa| \sim \Delta\gamma^2/4$ at the transition point; κ could, however, also be affected by systematic uncertainties in A_{eff} . We will derive constraints on the maximally allowed window size ε_{max} by requiring that these effects do not significantly alter the resulting DM limits.

III. CHOICE OF TARGET AND INSTRUMENT SPECIFICATIONS

For concreteness, we will in the following focus on observations of the Galactic center region with Imaging Atmospheric Cherenkov Telescopes (IACTs). We consider the benchmark scenarios summarized in Tab. I, which roughly correspond to the telescope characteristics of the currently operating H.E.S.S. [3], the future CTA [6] and—as the most optimistic choice for indirect DM searches—the proposed Dark Matter Array (DMA) [7]. We implement the energy dependence of

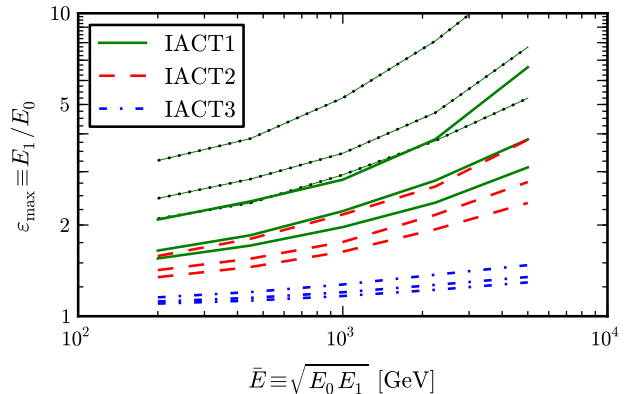


FIG. 1: Maximal sliding energy window size ε_{max} as function of the window position \bar{E} . We show for different intrinsic background curvatures $\kappa_{\text{max}} = 0.1, 0.2, 0.3$ (top to bottom) the window sizes above which DM limits are affected by more than 50%. The *dotted lines* show for IACT1 ε_{max} for which a power-law ansatz would still give a good fit to the background.

the effective area A_{eff} as given in Ref. [3] (Ref. [14]) for H.E.S.S. (CTA) and take $A_{\text{eff}}^{\text{DMA}} = 10 \cdot A_{\text{eff}}^{\text{CTA}}$. The proton, gamma-ray and electron efficiencies ϵ_{p,γ,e^-} in all three scenarios as well as the energy resolution $\Delta E/E$ in case of H.E.S.S. and DMA are taken to be energy independent; for CTA we adopt results from Ref. [6]. We will use $\epsilon_{\gamma} = \epsilon_{e^-} = 0.8$ throughout and assume that the proposed DMA can reject protons with efficiencies $\epsilon_p \approx 10^{-3}$.

For the background, we take into account cosmic-ray fluxes of electrons [15] and protons [16, 17], the diffuse gamma-ray flux [18] and the source HESS J1745-290 [19] at (or very close to) the Galactic center. A summary and more detailed description can be found in the Appendix; there, we also discuss which choice of target region $\Delta\Omega$ optimizes the signal-to-noise ratio \mathcal{S}/\mathcal{N} (see also Ref. [20]). For the Einasto and NFW DM profiles, with parameters as in Ref. [21], we will adopt a relatively small region $\Delta\Omega = 2^\circ \times 2^\circ$ around the Galactic center; larger regions would weaken the signal-to-background ratio, \mathcal{S}/\mathcal{B} . In case of a strong point source-like enhancement of the DM signal from the Galactic center (e.g. through the effect of the super-massive black hole [22, 23] or adiabatic compression [24–26]), it is favorable to focus on even much smaller target regions. As an example, we consider the case of an adiabatically compressed (AC) profile [25, 26] for which we choose a target region of $\Delta\Omega = 0.2^\circ \times 0.2^\circ$.

Let us now derive values for the tolerable window size ε_{max} in presence of maximal background curvatures κ_{max} . Using mock data sets with $\kappa = \pm\kappa_{\text{max}}$, we compare average DM limits (on the DM models introduced below) obtained when using the power-law ansatz for the background with the limits obtained when incorporating a (fixed) curvature κ in the background fit. In Fig. 1 we display as function of the sliding energy window position

DM particle	m_χ^{th} [TeV]	$\langle\sigma v\rangle^{\text{th}}$ [cm ³ s ⁻¹]	relevant channel	spectral feature
$\gamma\gamma$	any WIMP	$\mathcal{O}(10^{-30})$	$\gamma\gamma$	line
KK	$B^{(1)}$	$1.3 \cdot 10^{-26}$	$\ell^+\ell^-\gamma$	FSR step
BM3	neutralino	$0.23 \cdot 10^{-29}$	$\ell^+\ell^-\gamma$	IB bump
BM4	neutralino	$1.9 \cdot 10^{-27}$	$W^+W^-\gamma$	IB bump

TABLE II: DM benchmark models used in our analysis as examples for the typical spectral endpoint features to be expected in WIMP annihilations. For these particular models, we also state the annihilation channel that is most important in this context, as well as mass and total annihilation rate for thermally produced DM. See text for further details about the DM models and Fig. 2 for the corresponding photon spectra.

$\bar{E} \equiv \sqrt{E_0 E_1}$, and for different curvatures κ_{max} , the values of ε_{max} above which the DM limits are affected by more than 50%. For comparison, the dotted lines show for IACT1 the values for ε_{max} below which the power-law fit still appears to be in good agreement with the curved background (using as criterion that for at least 80% of the mock data sets the p -value of the power-law fit is larger than 0.05): obviously, a good quality of the power-law fit alone does not automatically exclude sizeable effects on the DM limits. Therefore, *a priori* assumptions on κ_{max} are indispensable; in our case, we employ $|\kappa| \leq \kappa_{\text{max}} \approx 0.2$ – which we checked to be satisfied for the background we adopt here – to determine optimal logarithmic window sizes for IACT1 and IACT2 according to Fig. 1 (for IACT3, see below).

IV. DARK MATTER SPECTRAL SIGNATURES

The DM signal flux from a sky region $\Delta\Omega$ is given by

$$\frac{dJ_\chi}{dE} \equiv \alpha \frac{dN_\chi}{dE} = \frac{\langle\sigma v\rangle}{8\pi m_\chi^2} \int_{\Delta\Omega} d\Omega \int_{\text{l.o.s.}} ds \rho_\chi(r(s, \Omega))^2 \frac{dN_\chi}{dE}, \quad (2)$$

where $\langle\sigma v\rangle$ is the annihilation rate, dN_χ/dE the differential number of photons per annihilation, $\rho_\chi(r)$ the Galactic DM profile and s runs over the line-of-sight. For any photon spectrum, and a given value of the dark matter particles' mass, we can now derive limits on α (aka $\langle\sigma v\rangle$) by scanning over all possible values of m_χ and applying the method described in detail in Section II. As a technical remark, we found that the best limits are actually obtained by choosing the center of the sliding energy window to lie slightly off-set from the kinematic endpoint $E = m_\chi$ of DM spectra at or slightly below which we expect to see the features we are looking for. For the instrument specifications and background model that we adopted here, in particular, the optimal choice turned out to be $\bar{E} = \varepsilon^{-0.25} m_\chi$ (not for line signals, however, for which we take $\bar{E} = m_\chi$).

In the following, we will discuss three types of typical endpoint features that arise from radiative corrections

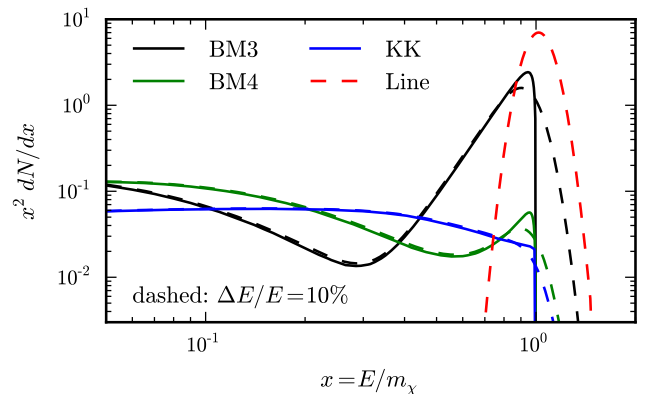


FIG. 2: Photon spectra for the DM benchmark models of Tab. II. Dashed lines show the same spectra, smeared with a Gaussian of width $\Delta x/x = 0.1$ to give a rough indication of how well a detector with such an energy resolution would in principle be able to discriminate these models from astrophysical (power-law) backgrounds, as well as from each other.

to the tree-level annihilation process. The most striking spectral signature, in terms of a possible discrimination from a power-law background, is a *gamma-ray line* at $E_\gamma = m_\chi$ ($E_\gamma = m_\chi[1 - m_{Z/H}^2/4m_\chi^2]$), which would result from the direct annihilation of DM into $\gamma\gamma$ ($Z\gamma$ or $H\gamma$) [8]. Generically, for thermal cross sections of DM in the form of weakly interacting massive particles (WIMPs), the annihilation rate is expected to be of the order of $\langle\sigma v\rangle_{\text{line}} \sim \alpha_{\text{em}}^2 \times \langle\sigma v\rangle_{\text{tree}} \sim 10^{-30} \text{cm}^3 \text{s}^{-1}$, but in some cases much stronger line signals are possible [27–29].

As an example for a step-like feature we use the gamma-ray spectrum [10] expected from annihilating *Kaluza-Klein (KK) DM* in models of universal extra dimensions [30]. In the minimal version of these models, the DM particle is the $B^{(1)}$, *i.e.* the first KK excitation of the weak hypercharge gauge boson, and the correct relic density is obtained for $m_{B^{(1)}} \sim 1.3 \text{TeV}$ [31]. Its total gamma-ray annihilation spectrum dN/dx (with $x \equiv E/m_\chi$) at high energies is dominated by final state radiation (FSR) off lepton final states and turns out to be essentially independent of $m_{B^{(1)}}$ and other model parameters.

Pronounced bump-like features at $E \simeq m_\chi$ may arise from internal bremsstrahlung (IB) in the annihilation of *neutralino DM* [11]. While these spectra are in general highly model-dependent, we follow here a simplified approach by defining two spectral templates dN/dx (which we take to be independent of m_χ) by referring to neutralino benchmark models introduced in Ref. [11]. Here, BM3 is a typical example for a neutralino in the stau co-annihilation region, where photon emission from virtual sleptons greatly enhances dN/dx ; BM4 refers to a situation in which IB from W^\pm final states dominates. We note that the Sommerfeld effect could strongly enhance these features, in particular in the case of BM4, in the same way as pointed out in Ref. [27] for line signals.

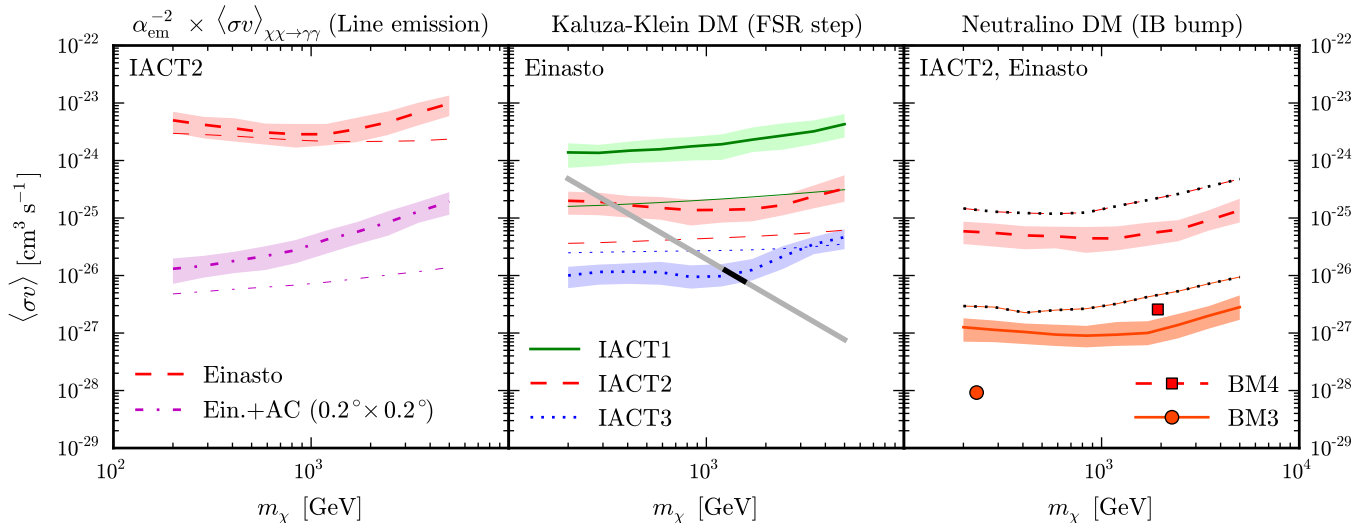


FIG. 3: *Thick lines*: Expected 2σ upper limits on $\langle\sigma v\rangle$ for selected DM models, DM profiles and observational scenarios; bands indicate the variance of these limits. *Thin lines*: Spectral feature of DM signal has $\mathcal{S}/\mathcal{B} \approx 1\%$ (after convolution with energy dispersion). The *left panel* shows limits on gamma-ray lines, rescaled by a loop-factor of α_{em}^{-2} for better comparison. In the *central panel*, the gray band indicates the expected $\langle\sigma v\rangle$ for KK DM, the black part being compatible with the observed relic density. In the *right panel*, we indicate the adopted neutralino benchmark points, and the *dotted lines* show the projected 5σ sensitivity.

In Tab. II, we shortly summarize the properties of the DM benchmark models described above, including for completeness the actual DM mass and total annihilation rate needed to obtain the observed relic density for thermally produced DM. Note, however, that we essentially treat these values as free parameters in our analysis and that we are rather interested in the spectral shape of the annihilation signal, represented by dN/dx ; in Fig. 2 we show these spectra for a direct comparison.

V. LIMITS AND DISCUSSION

In Fig. 3 we show our results for the expected 2σ upper limits (thick lines) on the above DM models as well as the variance of these limits among the 300 mock data sets that we created for this analysis. We find that in particular IB features in the spectrum (right panel) have the potential to constrain the annihilation rate at least down to values typically expected for thermal production, $\langle\sigma v\rangle \sim 3 \cdot 10^{-26} \text{cm}^3 \text{s}^{-1}$, already for modest assumptions about the DM distribution (we verified that NFW and Einasto profiles give similar results). This is very competitive compared to the best current limits from ACTs that only rely on secondary photons [32] – though we would like to stress that these limits provide rather complementary information on the DM nature and can thus usually not easily be compared.

For the case of not too strongly pronounced endpoint features (like line signals in most models or the step for Kaluza-Klein DM), secondary photons will usually be more powerful in constraining the total annihilation rate

$\langle\sigma v\rangle$; from the point of view of indirect DM searches, however, the *detection* of the kinematic cutoff will be much more interesting than the detection of secondary photons since it allows to draw firmer conclusions about the DM origin of the signal and even to determine important parameters like m_χ . For models with very large IB contributions like BM3, on the other hand, we find that our method provides even stronger *limits* on $\langle\sigma v\rangle$ than what was obtained by the HESS analysis of the Galactic center region assuming annihilation into $b\bar{b}$ [32].

In case of an adiabatically compressed profile our limits could improve by two orders of magnitude, as demonstrated for gamma-ray lines in the left panel; under such conditions, one could even hope to constrain models with very small annihilation rates like BM3 (recall that the annihilation rate for BM4 is anyway affected by the Sommerfeld enhancement [27] and thus likely considerably larger than what is shown in Fig. 3). As shown in the central panel of Fig. 3, the future CTA should be able to place limits about one order of magnitude stronger than currently possible, and the proposed DMA could further improve these by another factor of ten.¹

When probing a specific DM model, the corresponding

¹ Note that for DMA, as can be seen from Fig. 1, the statistics actually become so good that a spectrum with $\kappa \sim \mathcal{O}(0.1)$ curvature starts to deviate significantly from a power-law background already for rather small sliding energy windows. In order to obtain reasonable limits, we therefore included $\kappa \neq 0$ as a free parameter in the fit to allow for energy windows somewhat larger than shown in Fig. 1.

S/B is a good measure for the level on which spectral artefacts in the energy reconstruction of the instrument must be understood. As can be inferred from Fig. 3 (thin lines), most of our derived limits correspond to moderate S/B values of at least a few percent (except for IACT3), which should be well in reach of current instruments.

Limits on gamma-ray lines as shown in Fig. 3 are usually derived *neglecting* any secondary gamma-ray component from DM annihilation [12]; this approximation, however, breaks down for very small branching ratio into lines since part of the secondary component will leak into the sliding energy window. Assuming a dominant annihilation into $b\bar{b}$ final states, we find that for branching ratios into gamma-ray lines smaller than $\mathcal{O}(10^{-4})$, the presence of the secondary flux begins to alter the derived gamma-ray line limits significantly. This renders a naive application of standard line-search results on DM models with generic $\mathcal{O}(\alpha_{\text{em}}^2)$ branching ratios into gamma-ray lines questionable [33].

The dotted lines in the right panel of Fig. 3 show the projected *sensitivity* to see a 5σ signal in the IACT2 scenario (neglecting systematics and trial factors). Such an observation should of course be cross-checked by the non-observation of the same signature in control regions without large DM induced fluxes. A more detailed analysis for detectional prospects is beyond the scope of the present work and left for a subsequent publication [33].

VI. CONCLUSIONS

Gamma rays from DM annihilation often exhibit pronounced spectral features near photon energies close to the DM particles' mass. Here, we have shown that methods from gamma-ray line searches, which greatly reduce the uncertainties related to astrophysical background fluxes, can successfully be extended to look for such spectral features; this provides a probe of the DM nature that is complementary to DM searches relying only on the rather model-independent spectrum from secondary photons.

While these kind of features may generically be considered even more relevant for the *detection* of DM signals, because they would provide rather unambiguous evidence for the DM nature of the signal as well as allow to determine important parameters like the DM mass, we have demonstrated here that including the spectral information may even significantly improve *limits* on DM signals; steps or bump-like IB features can, in fact, be much more important in this respect than lines.

We stress that while we have considered constraints for IACT observations of the Galactic center region, the presented method is much more general and can be applied to both other targets and other instruments; we thus expect it to be useful for a wide range of applications in indirect DM searches. An obvious extension of the approach presented here, finally, is to apply it to the detection rather than exclusion of DM signals, as well as

to the *discrimination* of models [33].

Acknowledgments

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Appendix A: Dark matter searches in the Galactic Center region

Imaging Atmospheric Cherenkov Telescopes (IACTs) detect gamma rays by measuring the dim Cherenkov light produced by electromagnetic showers through the atmosphere. Very similar showers are induced by cosmic-ray electrons, which hence constitute a practically irreducible background. Proton-induced hadronic showers, on the other hand, differ in profile and energy density and can currently be rejected with efficiencies $\epsilon_p \sim \mathcal{O}(10^{-2}-10^{-1})$. Due to their large intrinsic fluxes, charged cosmic rays typically form the major background of IACT observations. For the flux of cosmic-ray electrons, we take $dJ_{e^-}/dEd\Omega = 1.17 \times 10^{-11} (E/\text{TeV})^{-3.9} (\text{GeV cm}^2 \text{ s sr})^{-1}$ above 1 TeV, which hardens below 1 TeV to a spectral index of -3.0 [15] (with a transition between the two fluxes that we assume to be proportional to their generalized mean with exponent -2). For the proton flux we take $dJ_p/dEd\Omega = 8.73 \times 10^{-9} (E/\text{TeV})^{-2.71} (\text{GeV cm}^2 \text{ s sr})^{-1}$ [16], which we shift to lower energies by a factor of 3 to take into account the reduced Cherenkov light output of hadronic showers, $E_p^{\text{recon.}} \approx E_p^{\text{true}}/3$ (see *e.g.* Ref. [17]).

For observations of the Galactic Center region (GC), we take as further background into account the HESS source J1745-290 [19], with $dJ_{\text{HESS}}/dE = 2.3 \times 10^{-15} (E/\text{TeV})^{-2.25} (\text{GeV cm}^2 \text{ s})^{-1}$. The diffuse photon emission measured by H.E.S.S. in a $-0.8^\circ \leq \ell \leq 0.8^\circ$ and $|b| \leq 0.3^\circ$ region around the GC is given by $dJ_{\text{diff}}/dE = 5.1 \times 10^{-15} (E/\text{TeV})^{-2.29} (\text{GeV cm}^2 \text{ s})^{-1}$ [18]. Unknown diffuse emission from outside this region will conservatively be accounted for by upscaling this flux by a factor of two within our $2^\circ \times 2^\circ$ target region. We summarize all these background contributions in Fig. 4.

The statistical significance of a spectral feature depends on the signal-to-noise ratio S/\mathcal{N} ($\mathcal{N} \simeq \sqrt{\mathcal{B} + \mathcal{S}}$) inside the target region. The number of expected background events \mathcal{B} within a target region $\Delta\Omega$ and energy range ΔE is calculated analogously to Eq. (1) by replacing the model flux by the sum of the above background fluxes after integrating over $\Delta\Omega$. In the same way, the

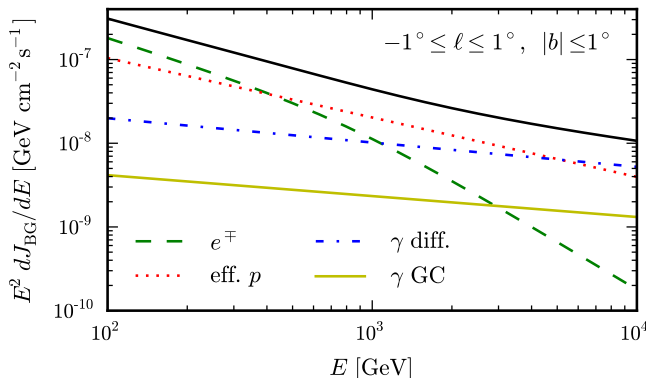


FIG. 4: Summary of adopted background fluxes in a $2^\circ \times 2^\circ$ region around the Galactic center, with an effective proton flux as it enters the IACT2 scenario. The black solid line shows the sum of all background fluxes.

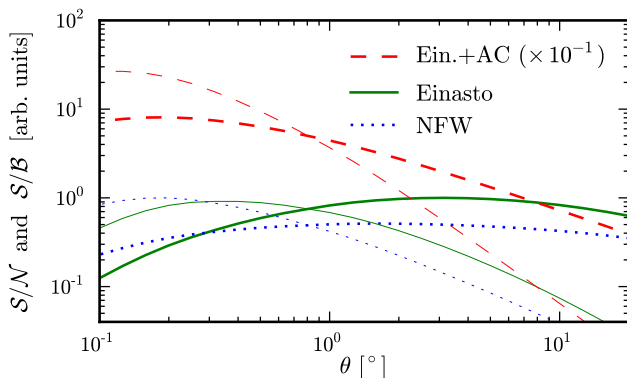


FIG. 5: S/\mathcal{N} (thick lines) and S/\mathcal{B} (thin lines) of DM signal inside a circular region around the GC with radius θ , for different DM halo profiles. For the Einasto profile, we also show the effect of adiabatic compression (AC). We assume $S \ll B$ and an energy threshold of 200 GeV, but for threshold energies 100 GeV–5 TeV we find similar results.

number of signal events \mathcal{S} follows from the DM annihilation flux as given in Eq. (2).

In Fig. 5, we show the S/\mathcal{N} (thick lines) of spectral features for a circular region around the GC with radius θ . We compare results for the standard Einasto and NFW DM profiles with parameters as in Ref. [21] (*i.e.* $r_s^{\text{NFW}} = 21$ kpc, $r_s^{\text{Ein.}} = 20$ kpc, $\alpha = 0.17$ and $\rho_\chi = 0.4 \text{ GeV cm}^{-3}$ at Sun's position $R_\odot = 8.5$ kpc). As can be seen from the figure radii of a few degree are required in order to maximize S/\mathcal{N} for these profiles (see also Ref.[20]).

For the optimal choice of $\Delta\Omega$ one should also consider the signal-to-background ratio S/\mathcal{B} which is shown in Fig. 5 for comparison (thin lines). S/\mathcal{B} is related to the importance of systematic instrumental effects for the statistical analysis, *i.e.* it gives an indication of how well artefacts and uncertainties in the reconstructed energy spectrum of the instrument must be understood. In most of our analysis, we use a relatively small $\Delta\Omega = 2^\circ \times 2^\circ$ region around the GC. As can be seen in Fig. 5, although a larger region could improve S/\mathcal{N} , it also would imply a significantly reduced S/\mathcal{B} .

In some cases, *e.g.* through the effect of the super-massive black hole [22] or adiabatic compression [24–26], the DM annihilation can be boosted in a region concentrated around the GC, leading to a qualitative change in the behavior of S/\mathcal{N} with respect to the above unboosted DM profiles. The effect of adiabatic compression is illustrated in Fig. 5 in case of the Einasto profile (Ein.+AC), where we exemplarily adopt the adiabatic contraction model of Gnedin *et al.* [25] together with the best fit parameters inferred from the hydrodynamical simulation S1 of Gustafsson *et al.* [26]. In this case, the profile inner slope steepens to $\rho \sim r^{-1.12}$. For such an enhancement, DM self-annihilations start to play a role and constrain the halo density to be at most $\rho_{\text{max}} \sim m_\chi / \langle \sigma v \rangle \tau_{\text{gal}}$ [23]; however, the cutoff radii obtained, $r \sim 10^{-9}$ kpc, are so small that this effect does not influence our results. As can be seen from Fig. 5, in the adopted boosted scenario it is preferable to consider much smaller target regions than in case of the above unboosted profiles; hence, we will use a $0.2^\circ \times 0.2^\circ$ region around the GC when calculating limits in presence of adiabatic compression.

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