LIGHT COMPOSITE FERMIONS AND ANOMALY MATCHING REVISITED

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DESY Bibliothek Notkestrasse 85 2 Hamburg 52 Germany LIGHT COMPOSITE FERMIONS AND ANOMALY MATCHING REVISITED

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A physically unique and simple solution of 't Hooft's anomaly matching equations in composite models of the type $SU(3)_{MC} \times SU(N)_{L} \times SU(N)_{R}$ is found for N = 6, if an additional selection criterion for composite "ground states" is introduced.

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Two years ago 't Hooft 1 formulated a "naturalness" set of conditions whereby light composite fermions with dimensions of order Λ_{MC}^{-1} , much smaller than their inverse masses, can be formed at high energies by a new "metacolor" gauge interaction which becomes strong at an energy scale $\Lambda_{MC}^{}$. Unfortunately the main conditions, triangle anomaly matching for preon and composite fields, the decoupling requirement and metaflavor independence proved to be so rigorous that no non-trivial solutions were found among SU(3) metacolor gauge groups possessing a chiral SU(N) x SU(N) 'x U(1) metaflavor symmetry.

Since then many authors 2-5 have carried out searches involving many different gauge groups for solutions of the anomaly-matching conditions, if need be relaxing the decoupling and N-independence conditions which are on a weaker footing than the first condition. Meanwhile it has been shown 5,6 that the assumption of no phase transition is required in addition to the Appelquist-Carazzone decoupling theorem in order to justify the decoupling condition. Some of these searches have been carried out in the framework of superalgebras, or in the case of one of the authors, by using a valence-like 3-preon model for composite quarks and leptons. Many solutions have been found but none are particularly attractive; for either they are too simple or so complex as to admit many composite states which have not been observed.

In this letter we reexamine the anomaly conditions and decoupling requirement and show that by a suitable modification it is possible to obtain a physically unique solution of the anomaly conditions applied to $SU(3)_{MC} \times SU(N) \times SU(N)$; this solution lies in the physically interesting metaflavour group $SU(6) \times SU(6)$. Consider the general chirally-symmetric case in a left-handed formulation with N preons in the fundamental 3 and N in the $\overline{3}$ of $SU(3)_{MC}$. The metaflavor group is then $SU(N) \times SU(N)$ and the two kinds of preons are left-handed Weyl spinors belonging to the representations

$$P = (\underline{3}; N, I) \equiv (\underline{\square}; \underline{\square}, I)$$

$$P' = (\underline{3}; I, \overline{N}) \equiv (\underline{\square}; I, \overline{\square})$$
(1)

To form (left-handed) composite states which are MC-singlets, we need only consider the 3-preon configurations PPP, PP' \dagger p' \dagger and P \rightleftharpoons P'. One arrives at the set of spin 1/2 composite fermions equivalent to those listed by 't Hooft¹

In the chirally-symmetric case, to each pair of states ψ_i and ψ_i' is associated the index L_i which can assume integer values.

Anomaly matching on the preon and composite levels leads to the two well-known 't Hooft constraint equations 1

$$(N^{2}-9)l_{1} - \frac{1}{2}N(N-7)l_{2} + \frac{1}{2}(N-6)(N-3)l_{3} - \frac{1}{2}N(N+7)l_{4} + \frac{1}{2}(N+6)(N+3)l_{5} = 3; N > 2$$
(3a)

from matching $[SU(N)]^3$ anomalies and

$$(N^{2}-3)l_{1} - \frac{1}{2}N(N-3)l_{2} + \frac{1}{2}(N-2)(N-3)l_{3}$$

$$-\frac{1}{2}N(N+3)l_{4} + \frac{1}{2}(N+2)(N+3)l_{5} = 1, N>1$$
(3b)

from matching $[SU(N)]^2 \times U(1)$ anomalies. There are a number of solutions to these equations for any N with the exception of N = 3, 6, 9, ..., where there exists none at all. 't Hooft's additional requirement of simultaneous decoupling of preons (if made virtually heavy) and their associated composites proved too strong a constraint

leaving only N = 2 as a solution. We feel that Preskill and Weinberg's observation 6 mentioned in the introduction justifies dropping the decoupling conditions. The purpose of this paper is to look for alternative constraints and/or modifications of 't Hooft's program as applied to SU(3) $_{MC}$ x.SU(N) x SU(N)' x U(1).

In the following we discuss two such modifications which, taken separately, do not change matters in a satisfactory way. Only if combined do they lead to a practically unique, simple and appealing solution.

- 1) The first modification is to introduce an additional strong constraint on the set of admitted composites. We single out candidates for "ground state" composites by simply combining the spins of the three preons to spin 1/2 and by applying 3,8 the Fermi principle to identical preons in the following restricted sense: we require total antisymmetry with respect to metacolor, metaflavor and Lorentz structure F2 (implying spatial symmetry). This reduces the list (2) of composites to the four composites $\psi_1,\,\psi_2,\,\psi_1'$ and ψ_2' with non-negative indices only. We immediately lose all solutions of 't Hooft's anomaly equations (3a,b) except the one for the trivial case of N = 2 where only Eq. (3b) applies. It seems rather remarkable that our ground state criteria reduce the plethora of solutions down to that singled out by 't Hooft's decoupling requirement.
- 2) As a second modification of 't Hooft's program for $SU(3)_{MC}$ x SU(N) x SU(N)' x U(1) we propose to break spontaneously the conserved U(1) symmetry well above the binding energy Λ_{MC} . The important observation is the following. 't Hooft's idea of keeping composites massless on the scale Λ_{MC} is to leave the full chiral metaflavor group unbroken. This idea is not invalidated by retaining only the chiral part SU(N) x SU(N)'. Spontaneous breaking of the U(1) symmetry above Λ_{MC} does not affect the masslessness of the preons, but it obviously has dramatic effects on the composite level, in so far as the $\int SU(N) \int_{-\infty}^{\infty} x U(1)$ anomaly matching condition (3b) gets lost.

Of course in dropping this condition we obtain a real proliferation of solutions to the anomaly Eq. (3a), including now also solutions for N=3, 6, 9, ... We remark in passing that imposition of the decoupling conditions would again eliminate all solutions except for N=2 as noted from a straight-forward computer search.

One realizes that the two modifications of the conventional anomaly-matching scenario, Eqs. (2) and (3a,b) have opposite effects: restriction to the "ground state" composites strongly reduces the number of solutions, whereas the spontaneous breaking of the U(1) symmetry increases it. This leads us to combine both modifications, i.e., we consider the SU(N) anomaly equation (3a) for the "ground state" composites ψ_1 , ψ_2 , ψ_1 and ψ_2 (with non-negative indices). The anomaly equation (3a) then simplifies to

$$(N^2-9)l_1 - \frac{1}{2}N(N-7)l_2 = 3$$
 (4)

It is straightforward to see that there is no solution at all for N=3, 4, and 5. For N=6 there is a unique and simple solution

$$SU(6) \times SU(6)' \text{ with } \boldsymbol{\ell}_1 = 0 \text{ and } \boldsymbol{\ell}_2 = 1$$
 (5)

Within a physically acceptable range of N and $\boldsymbol{\ell}_1$, $\boldsymbol{\ell}_2$ there is no further solution. To quantify this statement, a computer search for N \leq 100 and $\boldsymbol{\ell}_1$, $\boldsymbol{\ell}_2 \leq$ 20 was performed, and only three additional but unacceptable solutions were found, namely

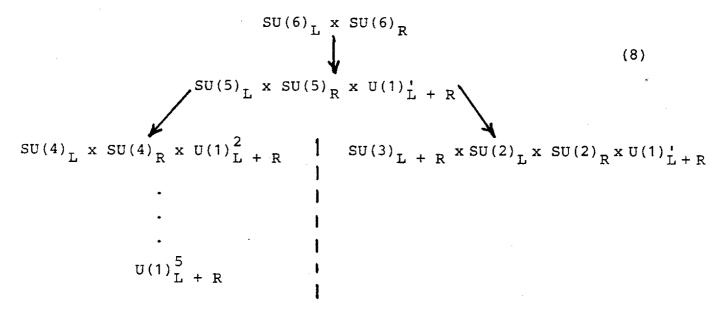
SU(8) x SU(8)' with
$$(\boldsymbol{L}_{1}, \boldsymbol{L}_{2}) = (1,13)$$

SU(10) x SU(10)' with $(\boldsymbol{L}_{1}, \boldsymbol{L}_{2}) = (3,18)$ (6)
SU(20) x SU(20)' with $(\boldsymbol{L}_{1}, \boldsymbol{L}_{2}) = (3,9)$

Hence we have singled out a physically unique solution. Not only is N=6 physically appealing, but also the composite structure is especially simple:

$$\begin{aligned} \Psi_2 &= (1; \Box, \Box) = (1; 6, 15) = PP^{\prime \dagger}P^{\prime \dagger} \\ \Psi_2' &= (1; \overline{\Box}, \overline{\Box}) = (1; \overline{15}, \overline{6}) = P^{\dagger}P^{\dagger}P^{\prime} \end{aligned}$$
(7)

both states appearing with unit multiplicity. $SU(6) \times SU(6)$ ' is obviously big enough to contain physically interesting subgroups like $SU(3)_{C} \times SU(2) \times U(1) = 0$ W-S. In subsequent papers we shall explore spontaneous dynamical symmetry breaking chains such as



arising due to SU(3)_{MC} singlet condensates caused by the strong metacolor force. The left-handed chain represents an interesting laboratory for studying successive decouplings of metaflavor degrees of freedom by giving <u>dynamical</u> masses to some of the preons and composites via spontaneous symmetry breaking at each step. Such a mechanism may be contrasted to 't Hooft's original decoupling requirement. The possible connection to reality of the right-hand chain is obvious.

Finally let us briefly speculate on how a spontaneous breakdown of the U(1) symmetry could be achieved dynamically for N = 6. An interesting candidate is a six preon condensate PPPPPP or P'P'P'P'P'P' which breaks the U(1) symmetry but can be made a singlet under $SU(3)_{MC} \times SU(6) \times SU(6)$ due to the fact that 6 is a multiple of 3.

After completion of this paper we received a preprint by Casalbuoni and Gatto^9 , which also discusses spontaneous breaking of the $\mathsf{U}(1)$ symmetry.

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Footnotes

- F1. Among the more interesting solutions are models reported by Bars and Yankielowicz⁴, which satisfy the decoupling condition as well. Albright and Sikivie⁵ found a particular example of this type based on $SU(4)_{MC} \times SU(N) \times SU(N)' \times U(1)$ ².
- F2. The same type of Fermi principle was applied³ in a search of composite models with the result that known solutions were recovered as well as new solutions found.
- F3. We tacitly assume that the broken U(1) is gauged.

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