DEUTSCHES ELEKTRONEN-SYNCHROTRON DESY



Comment on the Phases of Inelastic Partial Waves and their Comparison with the Quark Model, the Current to Constituent Quark Transformation, SU(6)_W, and Vector Dominance

bу

Soding

2.HAMBURG 52 . NOTKESTIEG 1

To be sure that your preprints are promptly included in the HIGH ENERGY PHYSICS INDEX, send them to the following address (if possible by air mail):



Comment on the Phases of Inelastic Partial Waves and their Comparison with the Quark Model, the Current to Constituent Quark Transformation, $SU(6)_W$, and Vector Dominance

bу

P. Söding

Deutsches Elektronen-Synchrotron DESY, Hamburg

Abstract

It is shown that the phases of inelastic πN partial wave amplitudes can be absolutely determined, using results from photoproduction. The signs obtained for the resonant amplitudes confirm the agreement with the relativistic quark model, the Melosh transformation, the broken SU(6) $_{W}$ scheme, and with vector dominance in the comparison with photoproduction.

Recently, from a partial wave analysis of the reaction $\pi N \to \pi \pi N$ the resonance amplitudes in the reactions

$$\pi N \rightarrow N^* \rightarrow \pi \Delta(1236) \tag{1}$$

and
$$\pi N \to N^* \to \rho N$$
 (2)

have been obtained. 1 The signs of these SU(3)-inelastic amplitudes are of particular significance. They are characteristic of the quark model state assignments of the N*'s and allow stringent tests of symmetries, of the transformation from current to constituent quarks, and of vector meson dominance by comparison with photoproduction. 2 In these tests, however one had an overall $^{\pm}$ sign ambiguity in the amplitudes of (1) and (2), and the same ambiguity in the comparison between (2) and photoproduction. We resolve these ambiguities (i.e. we determine the phase of the resonant amplitudes of (1) and (2) in an absolute sense), with the help of measurements of the photoproduction reaction

$$\gamma N \rightarrow \pi \Delta$$
. (3)

We first have to adopt a convention for the (unobservable) relative phase between the ground state [8] and [10] baryon states. We do this by defining the NN π and Δ N π coupling constants, g and g*, to have identical signs. This convention implies the customary choice of phases of the quark model wave functions (as used, e.g. in ref. 4), if pionic transitions are calculated from matrix elements of the divergence of the axial quark current.

With this convention the Born terms for the reactions $\gamma N \to \pi N$ and $\gamma N \to \pi \Delta$ have well defined relative signs. Therefore, observation of an interference of any s channel resonance with the Born terms in both of these reactions will tell us the relative sign of the amplitudes for decay of this resonance into πN and $\pi \Delta$. Since the $\pi N \to \pi N$ signs are fixed by the optical theorem, the sign of the resonance amplitude in reaction (1), and with it also the signs of all the interfering amplitudes in reactions (1) and (2), are then unambiguously determined.

Results from our measurement at DESY of reaction (3) in the charge state $\pi^-\Delta^{++}$, in the energy region 1.3 GeV < \sqrt{s} < 1.8 GeV, are shown in fig.1. The interference pattern observed can be uniquely attributed to the

 $D_{13}(1520)$ interfering with the (large) electric Born partial wave in the $J^P=\frac{3}{2}$, final S wave state. We calculated this gauge-invariant Born partial wave as well as the corresponding one ($J^P=\frac{3}{2}$, final D wave) for the reaction $\gamma p \to \pi^+ n$; they turn out to have the same sign. From the analysis of single pion photoproduction it is clearly established that the $D_{13}(1520)$ resonance interferes with the electric Born term in the reaction $\gamma p \to \pi^+ n$ with the same relative sign as in fig. 1. Dividing out the isospin factors ($\sqrt{\frac{1}{2}}$ and $\sqrt{\frac{1}{3}}$ respectively the amplitude for the reaction

$$\pi N \rightarrow D_{13}(1520) \rightarrow \pi \Delta(\ell = 0)$$

is therefore found to have sign "up" (Im T > 0 at resonance). With this established, the phases of all the mutually interfering amplitudes measured for the reactions (1) and (2) are absolutely calibrated. They are summarized in Table 1.

The comparison with the theoretical signs is now unique. In the quark model calculations by Moorhouse and Parsons 10 the phases were chosen in accord with our convention on g and g* so that the results can be directly compared. In fact, all their unambiguously defined signs agree with the experimental ones. The phase convention adopted in the predictions from broken $SU(6)_W$, and from the current to constituent quark transformation, of refs. 11 and 12 amounts to an additional overall factor -1 in the amplitudes for reaction (1). Removing it we again obtain agreement in absolute phase.

We proceed to a comparison of the amplitudes for the reaction $\pi N \to \rho_{\rm trans}^{\ N}$ with the photoproduction amplitudes for isovector $\gamma N \to \pi N$, to check whether ρ dominance holds. We now no longer consider the Δ a stable particle but include its decay amplitude. We note that the phase of the amplitude for the reaction $\gamma N \to \pi \pi N$ via an intermediate $D_{13}(1520) \to \pi \Delta(\lambda=0)$ is absolutely determined independently of any assumptions, since the electric Born term with which it interferes depends on the product e g^{*2} of coupling constants and is therefore absolutely known. It then follows from our discussion above that the sign of the amplitude for $\pi N \to \pi \pi N$ via this same intermediate resonant state is determined relative to sign g (as the relative sign of the resonance decay amplitudes into the πN and γN channels is defined relative to sign g which occurs in the $\gamma N \to \pi N$ Born term). The same holds then for all the resonant amplitudes for the processes

$$\pi N \to \left\{ \begin{array}{c} \pi \Delta \\ \rho N \end{array} \right\} \to \pi \pi N. \tag{4}$$

Converting from an amplitude for

$$\pi N \rightarrow \rho_{\text{trans}}^{0} N \rightarrow \pi_{1}^{\pi} _{2}^{N}$$

to a photoproduction amplitude using rho dominance, involves a factor

$$\frac{\operatorname{em}^{2}_{\rho}}{2\gamma_{o}g_{\rho\pi\pi}} = \frac{\operatorname{em}^{2}_{\rho}}{g_{o\pi\pi}^{2}}$$

and replacement of the ρ° polarization vector $(q_{\pi_1}-q_{\pi_2})_{\mu}$ by $\epsilon_{\mu}^{(\gamma)}$; here $\pi_1(\pi_2)$ has charge +e (-e). In the partial wave analysis 1,13 of reaction (4) the ρ° polarization (and helicity) states and the isospin Clebsch-Gordan factors were defined such that π_1 is the π^+ , thus e = +|e|. The phases of the predicted photoproduction amplitudes are therefore also relative to sign g. On the other hand, the measured photoproduction phases are also relative to sign g as contained in the Born term, thus this unknown sign drops out from the comparison. Rho dominance therefore requires absolute agreement of the signs of corresponding amplitudes. Table 4 of ref. 2 in fact shows such an agreement for all the well determined signs.

Thus, the determination of the absolute phase of the inelastic πN partial wave amplitudes confirms the agreement already noted in the relative phases for different resonances, with the predictions from the relativistic quark model, broken $SU(6)_W$, and the Melosh transformation, as well as from vector dominance for the relation between ρ and γ transitions.

I wish to thank Roger Cashmore for useful comments.

References and Footnotes

- D.J. Herndon, R. Longacre, L.R. Miller, A.H. Rosenfeld, E. Smadja,
 P. Söding, R. Cashmore and D.W.G.S. Leith, Phys. Rev. D (to be published);
 A.H. Rosenfeld et al., Phys. Letters <u>55B</u>, 486 (1975)
- R.J. Cashmore, D.W.G.S. Leith, R.S. Longacre, and A.H. Rosenfeld, Nucl. Phys. <u>B92</u>, 37 (1975)
- 3. g and g* are defined by the interactions $i\sqrt{2}$ $g\psi_p\gamma_5\psi_n\Phi$ and $-(g^*/m_\pi)$ $\psi_\Delta^\mu\psi_p\partial^\mu\Phi$, describing $\pi^+n\to p$ and $\pi^+p\to\Delta^+$, respectively. Our metric for four-vectors is $p^2=p^\mu p^\mu=-m^2$. The Δ is here considered a stable particle. The minus sign in front of g* is introduced because Φ (the π^+) is a state -|I|=1, $I_3=1$ > in isospin space.
- 4. R.P. Feynman, M. Kislinger, and F. Ravndal, Phys. Fev. <u>D3</u>, 2706 (1971)
- D. Lüke and P. Söding, Springer Tracts in Modern Physics <u>59</u>, 39 (1971);
 D. Lüke (Ph.D. thesis), DESY internal report F1-72/7 (1972)
- 6. Experimental constraints on the photon couplings of the resonances (ref. 7), as well as the observed angular distributions and helicity density matrix elements of the $\Delta(1236)$ in reaction (3) (see ref. 5), rule out a significant contribution of the $P_{11}(1470)$ or of any other resonance to this pattern. In the $J^P = \frac{3}{2}$ electric Born amplitude the final state S waves dominate strongly over the D waves. The $D_{13}(1520)$ resonance circle appears somewhat rotated, with the phase advanced relative to the Born term; a similarly rotated phase is observed in the reaction $\pi N \to D_{13}(1520) \to \pi \Delta(\ell = 0)$.
- G. Knies, R.G. Moorhouse, and H. Oberlack, Phys. Rev. <u>D9</u>, 2680 (1974);
 W.J. Metcalf and R.L. Walker, Nucl. Phys. <u>B76</u>, 253 (1974);
 R.C.E. Devenish, D.H. Lyth, and W.A. Rankin, Phys. Letters <u>52B</u>, 227 (1974)
- 8. We always use the baryon-first ordering in the isospin Clebsch-Gordan coefficients. Note also that there is a minus sign in the π^+ isospin state (cf. footnote 3).
- 9. It so happens that in the Argand diagrams of ref. 1 the phases were (accidentally) given correctly, if one takes into account the proper signs to convert to the baryon-first isospin convention.
- 10. R.G. Moorhouse and N.H. Parsons, Nucl. Phys. <u>B62</u>, 109 (1973)
- 11. D. Faiman and J. Rosner, Phys. Letters <u>45B</u>, 357 (1973)

- 12. F.J. Gilman, SLAC-PUB-1436; Invited talk at the IV International Meeting on Experimental Meson Spectroscopy, Boston, 1974. See also F.J. Gilman, M. Kugler and S. Meshkov, Phys. Rev. <u>D9</u>, 715 (1974)
- 13. D.J. Herndon, P. Söding, and R.J. Cashmore, Phys. Rev. D (1975) to be published

Table 1. Signs of the residua of the resonance amplitudes in the reactions $\pi N \rightarrow \pi \Delta$ and $\pi N \rightarrow \rho N$ (Refs. 1, 2)

+ **			•		
multiplet	resonance	πΔ	πΔ	ρ Ν *	on *
		lower &	higher l	$S = \frac{1}{2}$	$S = \frac{3}{2}, \text{ lower } \ell$
{70, 1 ⁻ }	D ₁₃ (1520)	+	+		+
	S ₁₁ (1520)			(+?)	
	s ₃₁ (1640)	+		(-?)	-
	D ₃₃ (1670)	- ·	(-?)		
	D ₁₅ (1670)	-			
	D ₁₃ (1700)	+	(-?)		(-?)
	s ₁₁ (1700)	-			
{56, 2 ⁺ }	F ₁₅ (1688)	+	(-?)		+
	P ₁₃ (1700)			-	
	F ₃₇ (1930)	-			(-?)
	F ₃₅ (1880)		-		-
$\{56, 0^{+}\}_{n=2}$	P ₁₁ (1470)	-		(-?)	
	P ₃₃ (1700)	-			
$\frac{1}{\{56, 0^+\}_{n=4}}$	P ₁₁ (1700)	(-?)		(+?)	

^(?) implies sign not determined as reliable as the others

na analysis and a same a same and

S is the total spin of ρ and N, $\vec{S} = \vec{S}_{\rho} + \vec{S}_{N}$. The £S states are defined as in Jacob and Wick, Annals of Physics 7, 404 (1959) (and in ref. 13); in the isospin Clebsch-Gordan coefficients the baryonfirst ordering is used.

Figure Caption

Fig. 1 Total cross section $\sigma(\gamma p \to \pi^- \Delta^{++})$ with the electric Born cross section subtracted (ref. 5).

