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## DYNAMICS OF CHARM MOLECULES

by

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## Dynamics of Charm Molecules

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Abstract: We calculate in a dynamical model based on coupled channels with charm-anticharm mesons  $D\bar{D}$ ,  $D\bar{D}^*$  and  $D^*\bar{D}^*$  and exchanges of light mesons  $\pi$ ,  $\eta$ ,  $\rho$  and  $\omega$  the spectrum of spin-parity states up to  $J = 2$  for  $C = I = 0$  and  $C = 2$ ,  $I = 0, 1$ . They are compared with experimentally known hidden charm states.

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## 1. Introduction

Experimental results at SPEAR and DORIS indicate that some of the structures observed in  $e^+e^-$  annihilation in the energy range 3.7 - 4.4 GeV are resonances that decay mainly into a pair of charmed mesons  $D\bar{D}$ ,  $D\bar{D}^* + D^*\bar{D}$  or  $D^*\bar{D}^*$  <sup>1)</sup>. A number of authors suggested that these peaks are genuine charmed meson-antimeson resonances <sup>2)</sup>. In particular, in Ref. 3 the peak at 4.028 GeV was interpreted as a resonance between  $D^*$  and  $\bar{D}^*$  lying just above the  $D^*\bar{D}^*$  threshold. Such states, which in quark language are four quark composites  $(c\bar{q})(\bar{c}q)$  (with  $q$  being the old  $u$ ,  $d$  and  $s$  quarks) are usually referred to as "charmonium molecules" in distinction to the lower lying  $c\bar{c}$  bound states of  $\psi$ 's and  $\chi$ 's, also called "charmonium atoms". Of course, whether such  $(c\bar{q})(\bar{c}q)$  mesons really exist is a question of dynamics and cannot be answered easily. For example, one could start from a basic theory, like Quantumchromodynamics, in which the low lying  $q\bar{q}$ ,  $c\bar{c}$  and  $c\bar{c}$  states are generated by the basic color confining mechanism. The remaining "Van der Waals" type forces would then produce the molecular bound-states  $(c\bar{q})(\bar{c}q)$  (or any other pairing of the four quarks) at threshold. Without an understanding of the confining forces it is not clear how to apply QCD directly to four quark systems. Therefore one is bound to use more phenomenological means, for example the bag model <sup>4)</sup>. Unfortunately the bag model is suitable only for S-wave molecules. It has been applied to charmonium molecules recently <sup>5)</sup>. In connection with  $e^+e^-$  annihilation we are primarily interested in P-wave charmonium molecules. For them we can expect a more "diatomic" structure than for S-waves, where there is no centrifugal barrier so that all four quarks overlap. For P and higher waves loosely bound systems of colorless atoms  $c\bar{q}$  and  $\bar{c}q$  possibly exist also from the quark dynamics point of view on the basis of qualitative arguments. It has been suggested by several authors to describe the dynamics of such loosely bound  $D\bar{D}$ ,  $D\bar{D}^*$  and  $D^*\bar{D}^*$  (and conceivably  $F\bar{F}$ ,  $F\bar{F}^*$  and  $F^*\bar{F}^*$ ) states by the exchange of a few light mesons <sup>6)</sup>. The strong decay  $D^* \rightarrow D\pi$  has been observed experimentally. So there is no doubt that pion exchange forces exist in  $D\bar{D}^* \rightarrow D^*\bar{D}$  and presumably also for  $D^*\bar{D}^* \rightarrow D^*\bar{D}^*$ . In the  $D\bar{D}$  system we can exchange  $\rho$  and  $\omega$  instead. Then we have a similar situation as in the nucleon-nucleon (or nucleon-antinucleon) system which is successfully described by light meson exchange forces.

So far the molecular states are considered completely distinct from the quark model  $c\bar{c}$  states, which describe  $J/\psi$ ,  $\psi'$ ,  $\psi''$  etc., and it is assumed that the  $c\bar{q}q$  states can be calculated without taking into account the mixing with the  $c\bar{c}$  states. On the other hand some authors found it necessary to introduce mixing of  $D\bar{D}$  components with the  $c\bar{c}$  wave function to account for radiative transitions in the charmonium "atomic" spectrum <sup>7)</sup>. In such a theory the problem of the transition potential between  $c\bar{c}$  and  $D\bar{D}$  states is completely open. Due to our lack of understanding the confinement mechanism to calculate these mixing forces in QCD seems to be as difficult as the calculation of the four quark states. Furthermore in Eichten et al. <sup>7)</sup> the direct forces between the open charm states  $D\bar{D}$  were neglected completely.

At this point one might ask whether it is possible to abandon the QCD framework completely and describe all  $J/\psi$  and  $\chi$  states above and below the charm threshold as bound states or resonances of charm-anticharm mesons. Whether such a framework leads to a reasonable theory of the  $\psi$  and  $\chi$  particles cannot be decided beforehand. It depends very much which channels of charm-anticharm mesons are included and whether the approximation of the binding forces by a small number of meson exchanges is sufficient. For spin 1/2 constituents with weakly spin-dependent forces the level ordering clearly is  $\{0^-, 1^-\}$ ,  $\{0^+, 1^+, 2^+\}$ , ....., which we take as the empirical ordering although the crucial  $0^-$  states are far from being settled. It is a natural guess that the level ordering with boson constituents is completely different. In a boson-antiboson bound state model the observed level ordering would not arise naturally and could come about only through complicated dynamics of many coupled channels. In this sense a boson constituent model, even if it worked, would not look very natural. On the other hand states near charm production threshold, like the 3.77 and 4.03 resonances certainly decay into  $D\bar{D}$ ,  $D\bar{D}^*$  or  $D^*\bar{D}^*$  particles with strong coupling if phase space is available for them. Then the assumption that these states contain very large components of charm-anticharm mesons is natural.

In this paper we shall investigate two separate problems. First we ask the question, whether all known  $J/\psi$  and  $\chi$  states, usually interpreted as  $c\bar{c}$  bound states, can be obtained as bound states of charm-anticharm mesons.

We shall call this our strong coupling model. Then we consider a weak coupling model. Here the states  $J/\psi$  and  $\psi'$  are interpreted as "atomic"  $c\bar{c}$  states. The resonances 3.77 and 4.03 GeV, which decay strongly into  $D\bar{D}$  etc. final states are described as bound states of  $D\bar{D}$  etc. mesons. Actually the forces between the charmed meson are fixed in such a way that the 3.77 and 4.03 levels are the lowest molecular states. Of course, here we make the assumption that there is negligible mixing between "molecular" and "atomic" states. This assumption of no mixing between  $c\bar{c}$  and mesonic bound states is not investigated further in our framework. It might be justified since the 3.77 and 4.03 states are very close to the  $D\bar{D}$ ,  $D^*\bar{D}$  and  $D^*\bar{D}^*$  thresholds. We consider our work as a first step and mixing should be taken into account in an improved version.

The basic assumptions for both models are as follows. We consider only the three channels  $D\bar{D}$ ,  $D\bar{D}^* + D^*\bar{D}$  and  $D^*\bar{D}^*$ , where  $D$  and  $D^*$  are the  $0^-$  and  $1^-$  mesons with  $C = 1$ . As forces we take all one particle exchanges with spins  $0^-$  and  $1^-$  lighter than 1 GeV. Bound states and resonances are calculated with the Blankenbecler-Sugar approximation to the Bethe-Salpeter equation.

After the forces have been determined from the  $C = 0, I = 0$  states we calculate the states with  $C = 0, I = 1$  and  $C = 2, I = 0, 1$ . The forces for such states are directly related to the forces in the  $C = I = 0$  channel using the known isotopic spins and G parities of the exchanged bosons.

The concept of the two models is very similar to the familiar nucleon-antinucleon boson exchange models which are often used to interpret recently found baryonium resonances <sup>8)</sup>. Of course, in this case, one is able to use the information on couplings of exchanged bosons from the nucleon-nucleon analysis. We go more the opposite way and try to use information about the  $C = 0$  system to predict the  $C = 2$  system. Naturally the formal aspects of our model are very similar to the well-known NN and  $N\bar{N}$  treatment <sup>9)</sup>.

The layout of our paper is as follows. In section 2 we give the dynamical equations and describe the structure of the exchanges used as input. The results are presented and discussed in section 3.

## 2. One Boson Exchange Potentials (OBEP) in Momentum Space

The definition of the one boson exchange potential is very similar to equivalent descriptions of the low energy nucleon-nucleon system. The channels  $D\bar{D}$ ,  $D\bar{D}^*$ ,  $D^*\bar{D}$  and  $D^*\bar{D}^*$  are considered on equal footing. We include the exchange of all mesons lighter than 1 GeV with spins  $0^-$  and  $1^-$ . These are the non-strange members of the SU(3) nonets of pseudoscalar ( $\pi$ ,  $\eta$ ,  $\eta'$ ) and vector mesons ( $\rho$ ,  $\omega$ ,  $\phi$ ). We leave out the scalar mesons ( $\delta$ ,  $\epsilon$ ,  $S^*$ ), since their experimental verification as resonances is rather unclear. The exchange of mesons with higher spins ( $J \geq 2$ ) and other parity ( $1^+$ ), such as  $f$ ,  $A_2$ ,  $f'$ ,  $g$ ,  $A_1$  and  $B$  are expected to have little influence because of the short range of the corresponding forces.

The potential of the  $D\bar{D}$  etc. interaction is determined by identifying it with the off-energy-shell Born term of the Feynman amplitude in the center-of-mass system. The corresponding diagram, as a representative the graph for  $D\bar{D} \rightarrow D\bar{D}$ , is shown in Fig. 1. Here  $\vec{p}$  and  $\vec{p}'$  are initial and final state three momenta and  $p_0$  and  $p'_0$  the corresponding energies in the c.m. system. The notation for the other channels  $D\bar{D}^*$  and  $D^*\bar{D}^*$  is analogous. To calculate the complete list of Feynman graphs for  $D\bar{D} \rightarrow D\bar{D}$ ,  $D\bar{D} \rightarrow D^*\bar{D}$ ,  $D\bar{D}^* \rightarrow D\bar{D}^*$ ,  $D^*\bar{D}^* \rightarrow D\bar{D}^*$  and  $D^*\bar{D}^* \rightarrow D^*\bar{D}^*$  we need the couplings of the  $D$  and  $D^*$  with the pseudoscalar and vector meson fields  $\pi$ ,  $\eta$ ,  $\rho$  and  $\omega$ . These couplings are:

$$H_{VPP} = i g_{VPP} \left\{ \partial^\dagger \vec{z} \vec{\partial}^\mu \partial \vec{p}_\mu + \partial^\dagger \vec{\partial}_\mu \partial \omega^\mu + (\vec{\pi} \vec{\partial}^\mu \partial^\dagger \vec{z} \partial_\mu^* + h.c.) + (\eta \vec{\partial}_\mu \partial^\dagger \partial_\mu^* + h.c.) \right\} \quad (2.1)$$

$$H_{VVP} = g_{VVP} \epsilon^{\alpha\lambda\mu\nu} \left\{ \vec{\pi} \partial_\alpha \partial_2^{\dagger\alpha} \vec{z} \partial_\mu \partial_\nu^* + \eta \partial_\alpha \partial_2^{\dagger\alpha} \partial_\mu \partial_\nu^* + (\partial^\dagger \vec{z} \partial_\alpha \partial_2^* \partial_\mu \vec{p}_\nu + h.c.) + (\partial^\dagger \partial_\alpha \partial_2^* \partial_\mu \omega_\nu + h.c.) \right\} \quad (2.2)$$

$$\begin{aligned}
H_{VVV} = & -i \left[ f_1 \left\{ g^{\alpha\beta} \partial_\alpha^{*+} \vec{z} \vec{\partial}^\mu \partial_\beta^* \vec{p}_\mu + g^{\alpha\beta} \partial_\alpha^{*+} \vec{\gamma}_\mu \partial_\beta^* \omega_\mu \right\} \right. \\
& + f_2 \left\{ \partial_\alpha^{*+} \vec{z} \partial_\beta^* (g_\mu^\alpha \partial^\mu - g_\mu^\alpha \partial^\beta) \vec{p}_\mu + \partial_\alpha^{*+} \partial_\beta^* (g_\mu^\alpha \partial^\mu - g_\mu^\alpha \partial^\beta) \omega_\mu \right\} \\
& \left. + \frac{f_3}{m^2} \left\{ \partial_\alpha^{*+} \vec{z} \vec{\gamma}_\mu \partial_\beta^* \partial^\alpha \partial^\beta \vec{p}_\mu + \partial_\alpha^{*+} \vec{\gamma}_\mu \partial_\beta^* \partial^\alpha \partial^\beta \omega_\mu \right\} \right]^{(2.3)}
\end{aligned}$$

Writing down these couplings we assumed SU(4) invariance and ideal mixing in the couplings and for  $\omega$ ,  $\phi$ ,  $\eta$  and  $\eta'$ . Then the  $\phi$  does not couple to the D and D\* mesons and the  $\eta$  in (2.1) to (2.3) stands for the  $1/\sqrt{2} (u\bar{u} + d\bar{d}) \equiv \eta_\sigma$  component of the true  $\eta$  and  $\eta'$ . To use these couplings for the latter particles one has to multiply with the amount of  $\eta_\sigma$  component in the  $\eta$  or  $\eta'$  respectively.

For the coupling  $H_{VVV}$  of three vector mesons we use the decomposition introduced in Ref. 10. It contains three independent coupling constants  $f_1$ ,  $f_2$  and  $f_3$ . In the analogous electromagnetic case the three constants  $f_1$ ,  $f_2$  and  $f_3$  are related to the charge  $f_c$ , the magnetic moment  $f_m$  and the electric quadrupole form factor  $f_q$  respectively<sup>10)</sup>. The connections are:

$$\begin{aligned}
f_1 &= f_c + \frac{2}{3} \eta f_q & \text{where } \eta &= m_s^2 / 4m_{D^*}^2 \\
f_2 &= f_m \\
f_3 &= (2(1-\eta))^{-1} [(1 - \frac{2}{3}\eta)] f_q - f_c + f_m
\end{aligned} \tag{2.4}$$

The evaluation of the OBEP matrix elements is conveniently carried out in momentum space. This way we have the option to take into account relativistic and meson retardation effects on a later stage. The spin properties of the potentials are worked out in the helicity basis. The expressions for the five transition potentials are rather lengthy and will be given in a separate publication<sup>11)</sup>. The next step is the angular momentum decomposition of the OBE potentials. We choose the incident direction  $\vec{p}$  along the z-axis and the outgoing momentum  $\vec{p}'$  in the xz-plane. Then the expansion is:

$$\langle \lambda'_1, \lambda'_2, \vec{p}' | V | \lambda_1, \lambda_2, \vec{p} \rangle = \sum_{\gamma} (2\gamma+1) d_{\lambda_2, \lambda'_2}^{\gamma}(\theta) \langle \lambda'_1, \lambda'_2, p' | V^{\gamma} | \lambda_1, \lambda_2, p \rangle \tag{2.5}$$



with  $\lambda = \lambda_1 - \lambda_2$  and  $\lambda' = \lambda'_1 - \lambda'_2$ . The potentials for fixed J are obtained by inverting (2.5):

$$\langle \lambda'_1, \lambda'_2, p' | V^{\dagger} | \lambda_1, \lambda_2, p \rangle = \frac{1}{2} \int_0^{\pi} d\theta \sin \theta d_{\lambda \lambda'}^{\dagger}(\theta) \langle \lambda'_1, \lambda'_2, \vec{p}' | V | \lambda_1, \lambda_2, \vec{p} \rangle \quad (2.6)$$

The same expansion (2.5) is used for the whole amplitude  $\langle \lambda'_1, \lambda'_2, \vec{p}' | T | \lambda_1, \lambda_2, \vec{p} \rangle$ . The basic integral which occurs in (2.6) is

$$\frac{1}{2} \int_{-1}^{+1} d(\cos \theta) P_J(\cos \theta) / (m_a^2 - t) = \frac{1}{2 p p'} Q_J(z_a) \quad (2.7)$$

with

$$z_a = \frac{1}{2 p p'} (2 p_0 p'_0 - (p_0'^2 - p'^2) - (p_0^2 - p^2) + m_a^2) \quad (2.8)$$

and (see Fig. 1)

$$t = (p_1 - p'_1)^2 \quad (2.9)$$

The completely off-shell partial wave projections of the various potentials have been calculated. The expressions are too lengthy to be reproduced here. They will be given elsewhere <sup>11)</sup>.

As is familiar from low energy nucleon-nucleon dynamics based on OBE potentials most exchange amplitudes are too singular for  $p'$  or  $p \rightarrow \infty$  to guarantee a solution of the dynamical equations. Therefore we modify the OBEP by form factors which represent the combined effect of vertex and propagator corrections. We multiply every potential term by an universal form factor of monopole type

$$F(t) = \frac{\Lambda^2}{m_a^2 + \Lambda^2 - t} \quad (2.10)$$

with a form factor mass  $\Lambda$  to be fixed later. The same form factor is used to modify the two propagators in the Bethe-Salpeter equation. The bound and resonance states are calculated on the basis of the Blankenbecler-

Sugar approximation <sup>12)</sup> to the Bethe-Salpeter equation.

In the case of equal masses  $m$  it has the following form:

$$T_{ij}^J(p, \bar{p}) = V_{ij}^J(p, \bar{p}) + \frac{1}{2\pi} \sum_{j'} \int \frac{dp' p'^2}{(m^2 + p'^2)^{1/2} (p'^2 - k^2)} V_{ij'}^J(p, p') T_{j'j}^J(p', \bar{p}) \quad (2.11)$$

Here  $k^2 = s/4 - m^2$  and  $T_{ij}^J(p, \bar{p})$  is the partial wave projected off-shell amplitude taken as relative energy = 0 limit of the Bjorken-Drell <sup>13)</sup> invariant amplitude (divided by  $4\pi$ ). In the calculation the momentum  $\bar{p}$  is also chosen off-shell in order to avoid left-hand cut singularities in  $V^J(p, \bar{p})$ . The indices  $i, j$  refer to both different particle combinations as well as different helicity states. The equation was solved only for a fixed  $j$  (e.g. the  $D\bar{D}$  state for  $\tau_p = \tau_c = (-1)^j$ ). For the unequal mass state  $D\bar{D}^*$  we replaced  $m$  by twice the reduced mass. In (2.11) the additional form factors coming with the D-propagators are left out for convenience.

Before solving the T-matrix equations we did some further approximations. Since we neglected the retardation in the propagators in the Bethe-Salpeter equation we consequently do the same with the retardation in the meson propagators (including the form factor (2.10)). Furthermore we replace all energies on- and off-shell by their masses.  $p_0 = p'_0 = m_D = 1.87$  GeV, as one would do in a nonrelativistic approximation. Then  $z_\alpha$  in eqn.(2.8) reduces to

$$z_\alpha = \frac{1}{2 p p'} (p'^2 + p^2 + m_\alpha^2) \quad (2.12)$$

In channels with D and  $D^*$  present we use the average of  $m_D$  and  $m_{D^*}$ ,  $\bar{m} = 1.95$  GeV and use this value for  $p_0 = p'_0 = \bar{m}$ . In matrix elements with longitudinal polarization of the vector mesons ( $\lambda_1, \lambda_2, \lambda_1' \text{ or } \lambda_2' = 0$ ) we must renormalize the polarization vectors accordingly. In the matrix elements with only  $D^*$  mesons in the initial and final state we also use the average mass  $\bar{m}$  for simplicity.

Of course the equations used reduce to the familiar Lippman-Schwinger equation in the non-relativistic approximation. Equations of the form (2.11) have also been used in low energy NN scattering theory <sup>9)</sup>.

To obtain the energies of the bound states and the resonance positions we proceed as follows. Bound states and resonances manifest themselves as poles in the T-matrix. The T-matrix equation (2.11) is solved by iteration with subsequent application of Padé approximants. Then bound states or resonances appear as poles in these Padé approximants.

### 3. Results

As advertised in section 1 we first tried to describe all existing hidden charm states as bound states of  $D\bar{D}$ ,  $D\bar{D}^* + D^*\bar{D}$  and  $D^*\bar{D}^*$ . In the following we call this the strong coupling model. We have calculated the levels up to  $J = 2$  and for the three cases  $C = I = 0$ ;  $I = 0, C = 2$  and  $I = 1, C = 2$ . For  $C = 0, I = 1$  no bound states or resonances are possible, as will be seen later. Obviously the results depend on the coupling constants of the charmed mesons on the various particles exchanged in the crossed channel. We have chosen our coupling constants in such a way that they are roughly compatible with relations following from SU(4) symmetry and ideal mixing. Whereas masses are badly broken in SU(4) it is usually assumed that coupling constants are impaired much less by SU(4) breaking<sup>14)</sup>. For the coupling constants  $g_{VPP}$  these symmetry relations are<sup>15)</sup>:

$$\begin{aligned} g(\omega D^+ D^-) &= -g(\rho^0 D^+ D^-) = -g(D^{*+} \eta_\sigma D^-) = +g(D^{*+} \pi^0 D^-) \\ &= -\frac{1}{2} g(\rho^0 \pi^+ \pi^-) \end{aligned} \quad (3.1)$$

and for  $g_{VVP}$ :

$$\begin{aligned} g(D^{*+} D^{*-} \eta_\sigma) &= -g(D^{*+} D^{*-} \pi^0) = g(D^{*-} \omega D^+) = -g(D^{*-} \rho^0 D^+) \\ &= \frac{1}{2} g(\rho^- \omega \pi^+) \end{aligned} \quad (3.2)$$

The coupling constants for VVV fulfill the same symmetry relations as the VPP coupling constants in (3.1) with appropriate change of notation. For  $f_1(\rho^0 \rho^+ \rho^-)$  we expect that it is roughly equal to  $g(\rho^0 \pi^+ \pi^-)$  if the electromagnetic form factor of the  $\rho^+$  is dominated by  $\rho^0$  exchange as the  $\pi^+$  form factor is. The particle  $\eta_\sigma = \frac{1}{\sqrt{2}}(u\bar{u} + d\bar{d})$  is the ideal mixed  $\eta$ . The relation of the physical  $\eta$  and  $\eta'$  to  $\eta_\sigma$  are well known.  $f_2(VVV)$  is fixed

in such a way, so that approximately  $f_2(VVV) = 2 f_1(VVV)$ . This relation is obtained in the quark model or in current algebra for the  $\rho$  meson <sup>16)</sup>.  $f_3(VVV)$  will be neglected throughout. For simplicity we take  $m_{\eta'} = m_{\eta} = m_{\pi}$  and of course  $m_{\rho} = m_{\omega}$ . In the following we shall not assume the symmetry relations (3.1) and (3.2) to be correct in all details, but consider them as a basis for orientation. However we have always assumed that  $\rho$  and  $\omega$  exchange are still related to each other by (3.1) and (3.2). The same is assumed for  $\pi$  and  $\eta$  exchange. Actually symmetry breaking of coupling constants can be connected with the symmetry breaking of masses in the framework of dual resonance amplitudes. This has been investigated by several authors. For example, Kuroda and Young find that  $g(D^{*+}D^{-}\pi^0)$  is larger than the SU(4) symmetry value by the factor  $(\alpha'_{\rho}/\alpha'_{\omega})^{1/2} = 1.15$  <sup>17)</sup>, whereas Thews finds for this increase, using finite energy sum rules the factor 1.2 - 1.5 <sup>18)</sup>.

In the strong coupling model we varied the coupling constants in the vicinity of the symmetry values (3.1) and (3.2) with  $g(\rho\pi\pi) = 6$  and  $g(\omega\rho\pi) = 17.5 \text{ GeV}^{-1}$  until we obtained  $1^-$  states at 3.1 and 3.6 GeV and a  $0^-$  state at 2.82 GeV. The energies of all the other levels for all three cases  $C = I = 0$ ;  $C = 2, I = 0, 1$  are shown in Table 1. The corresponding coupling constants are presented in Table 2.

The symmetry values for the VPP coupling, first line in Table 2, is 3.0, for the VVP coupling, the second line in Table 2 is  $8.75 \text{ GeV}^{-1}$  and for the VVV coupling  $f_1 = f_2/2 = 3.0$ . We see that the values in Table 2 do not differ very much from these values and that the 50% increase of the  $D^{*}\pi D$  coupling can be justified with the work of Thews <sup>18)</sup>.

A further input is the form factor mass  $\Lambda$  in (2.10). We have chosen  $\Lambda^2 = 2 \text{ GeV}^2$  as is suggested by other studies of hadron properties with the Bethe-Salpeter equation <sup>19)</sup>. The same value for  $\Lambda^2$  was used in the form factor for the propagators in the Bethe-Salpeter equation. All three factors are necessary to correct the singular high energy behaviour of the potentials due to the vector meson exchange. The value for the form factor mass and the magnitude of the coupling constants are not independent. We have checked that the spectrum is changed very little when  $\Lambda^2$  is varied in the

vicinity of  $2 \text{ GeV}^2$  by  $\pm 1 \text{ GeV}^2$ . The overall strength of the potential had to be lowered if  $\Lambda^2$  was increased. We now shall look into the isospin and charm content of the potentials.

For  $C = 0, I = 1$  the potential vanishes because we have  $m_\pi = m_\eta = m_{\eta'}$ . Even if we relax this constraint the potential is so weak so that no bound states or resonances are formed. One would need a very strong breaking of the relations of  $\pi$  and  $\eta$  and of  $\rho$  and  $\omega$  couplings respectively as given in (3.1) and (3.2) to produce bound states for  $C = 0, I = 1$ . From this we conclude that charm molecules with  $C = 0$  and  $I = 1$  are very unlikely. In the four channels  $C = 0, 2, I = 0, 1$  the contributions of  $\omega, \rho, \pi$  and  $\eta, \eta'$  (which is the  $\eta_\sigma$ ) appear in  $V(C, I)$  with the following factors:

$$\begin{aligned}
 V(0, 0) &= (\eta_\sigma + 3\pi) + (\omega + 3\rho) \\
 V(0, 1) &= (\eta_\sigma - \pi) + (\omega - \rho) \\
 V(2, 0) &= (\eta_\sigma - 3\pi) + (-\omega + 3\rho) \\
 V(2, 1) &= (\eta_\sigma + \pi) + (-\omega - \rho)
 \end{aligned} \tag{3.3}$$

Clearly the  $C = I = 0$  potential is the most attractive. For  $C = 2$  the relative magnitude of pseudoscalar versus vector exchange determines whether the potentials are attractive or not. Of course these remarks, based on (3.3) do not hold without exceptions since the sign of the potential depends also on the spin-parity state and the influence of nondiagonal versus diagonal terms in the potential. From (3.4) we expect the strongest binding for  $C = I = 0$  and less binding for  $C = 2, I = 0, 1$ .

From Table 1 we observe that for  $I = C = 0$  almost all states up to  $J = 2$  have bound states or resonances. Since  $m_D = 1.87 \text{ GeV}$  all states above  $3.74 \text{ GeV}$  are resonances. It was not difficult to find coupling constants reproducing almost perfectly the spectrum of  $1^{--}$  states (of course  $J/\psi = 3.1 \text{ GeV}$  served as input). Also the  $0^{--}$  states are reasonable. But the states  $0^{++}, 1^{++}$  and  $2^{++}$  lie lower than the measured states (see first column of Table 1) on the basis of the usual assignments<sup>20</sup>). In particular the lowest  $0^{++}$  state has a very small mass. This feature, too strong binding in the

states  $0^{++}$ ,  $1^{+-}$  and  $2^{++}$ , presumably is characteristic for this model based on boson constituents. For  $0^{++}$  states in  $D\bar{D}$  and  $D^*\bar{D}^*$  channels contribute in s-waves and similarly for  $1^{+-}$  do the  $D\bar{D}^* + D^*\bar{D}$  and  $D^*\bar{D}^*$  and also  $2^{++}$  has s-wave contributions in  $D^*\bar{D}^*$ . The fact that the  $2^{++}$  state has a much larger mass than the  $0^{++}$  state is caused by the tensor forces. We conclude from the results in Table 1 that for an understanding of the low mass part of the charmonium spectrum spin 1/2 constituents are essential. Nevertheless we have computed also the exotic  $C = 2$  states which are produced by the couplings in Table 2. We see that the  $I = 0$  states are in average more strongly bound than the  $I = 1$  states. In  $I = 0$  we have stable molecules with charm equal two in  $1^{+-}$  at 3.7 GeV,  $1^{--}$  at 3.61 GeV, in  $1^{++}$  at 3.67 GeV. The prediction for  $0^{++}$  is unreliable, since here in  $C = 0$  the forces are already much too strong. We also mention that states with "wrong" C parity, which cannot be generated by  $c\bar{c}$  states are possible in this model. In  $2^{+-}$  we have a bound state at 3.55 GeV. The first  $1^{+-}$  and  $2^{+-}$  occur in the channels  $D\bar{D}^*$  and  $D^*\bar{D}^*$  as p- and d-waves respectively.

In the second model the forces are reduced in such a way that the lowest  $1^{--}$  state is generated at 3.77 GeV. A second  $1^{--}$  state is obtained at 4.04 GeV which we identify with the experimentally found state at 4.03 GeV. For the couplings we assumed the symmetry relations (3.1) and (3.2) and took the values given in Table 4.

In this model the width of the  $1^{--}$  state at 3.77 GeV is  $\Gamma = 23$  MeV which has to be compared with  $\Gamma = (24 \pm 5)$  MeV, measured by DELCO <sup>21)</sup> and  $\Gamma = (28 \pm 5)$  MeV, measured by SLAC-LBL <sup>22)</sup>. For the width of the 4.04 resonance we obtain  $\Gamma \approx 60$  MeV. This number could not be determined better because of computational problems which appear above the  $D^*\bar{D}^*$  threshold. Its value agrees well with the  $\Gamma_{\text{exp}}(4.04) = (52 \pm 10)$  MeV as measured by the DASP Group at DORIS <sup>23)</sup>. It is clear that the 3.77 resonance can decay only into  $D\bar{D}$  states as experimentally observed <sup>20)</sup>. The 4.03 resonance can decay in all three channels  $D\bar{D}$ ,  $D\bar{D}^* + D^*\bar{D}$  and  $D^*\bar{D}^*$ . The measured fractions are  $0.09 \pm 0.05 : 0.58 \pm 0.06 : 0.33 \pm 0.08$  <sup>24)</sup>. We obtain:

0.15 : 0.48 : 0.37, which agrees quite well with the experimentally determined ratios.

The other spin-parity states are located where one has states also in the charmonium model, in particular for  $0^{-+}$  the  $\eta_c'$  in charmonium,  $1^{+-}$ ,  $0^{++}$  and  $1^{++}$ . This means that for these states the  $c\bar{c}$  component and the  $D\bar{D}$  component will mix strongly. For the  $2^{++}$  the mixing seems to be less important. Certainly a complete treatment of these states requires a model incorporating these two components with realistic forces in all channels.

We notice that we still predict a "wrong" C-parity state  $2^{+-}$  resonance but now high above threshold. The resonance energies of the  $C = 2$  exotic states are also rather high except a  $0^{++}$  state with  $I = 0$  at 3.44 GeV.

From our analysis we can draw two conclusions. The use of spin 1/2-constituents to explain the lower part of the charmonium spectrum is essential. On the other hand we showed that OBE-potentials in the  $D\bar{D}$ ,  $D\bar{D}^* + D\bar{D}^*$  and  $D\bar{D}^{**}$  channels are capable of forming bound states and narrow resonances. Our approach provides a quite natural way to understand the widths and branching ratios of  $\psi(3.77)$  and  $\psi(4.03)$ . Higher  $1^{--}$  resonances are possible and might be due to the coupling of D- to F-meson channels via K-exchanges.

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TABLE 1

$J^{PC}$	$C = I = 0$ Experiment	$C = I = 0$	$C = 2$ $I = 0$	$C = 2$ $I = 1$
$2^{+-}$		3.55 4.15	none	none
$1^{-+}$		$\gg 4.$	none	3.60
$2^{--}$		4.01	none	none
$2^{++}$	3.550	3.05 3.80	3.92 4.05	none
$1^{++}$	3.505	3.28	3.67	3.89 4.11
$0^{++}$	3.413	very low 2.75 3.60	2.10 3.10 3.85	2.90 4.30
$1^{--}$	3.096 3.685 3.772	3.10 3.64 3.88	3.61 4.00	4.20
$2^{-+}$		none	none	none
$1^{+-}$		2.84 3.71	3.70	4.01 4.30
$0^{-+}$	2.83 3.455	2.82 3.71	none	3.25 3.95

TABLE 2:

VPP	$g(\rho^0 D^+ D^-) = 4.0$	$g(D^{*+} \pi^0 D^-) = 6.0$
VPP	$g(D^{*+} D^- \rho^0) = 8.7 \text{ GeV}^{-1}$	$g(D^{*+} D^{*+} \pi^0) = 12.4 \text{ GeV}^{-1}$
VVV	$f_1(\rho^0 D^{*+} D^{*-}) = 6.0$	$f_2(\rho^0 D^{*+} D^{*-}) = 10.7$

TABLE 3:

$J^{PC}$	$C = I = 0$ Experiment	$C = I = 0$	$C = 2$ $I = 0$	$C = 2$ $I = 1$
$2^{+-}$		4.15	4.37	none
$1^{-+}$		none	none	3.87
$2^{--}$		> 4.30	none	none
$2^{++}$	3.55	3.81 4.10	4.18	none
$1^{++}$	3.505	3.69	none	4.15
$0^{++}$	3.413	3.40 3.80	3.44 3.95	4.05
$1^{--}$	3.77 4.03	3.77 4.04	4.00	none
$2^{-+}$		none	none	none
$1^{+-}$		3.52 4.30	none	4.10
$0^{-+}$	3.455	3.71	none	3.99 4.10

TABLE 4:

VPP	$g(\rho^0 D^+ D^-) = 3.5$	$g(D^{*+} \pi^0 D^-) = 3.5$
VVP	$g(D^{*+} D^- \rho^0) = 7.3 \text{ GeV}^{-1}$	$g(D^{*+} D^{*+} \pi^0) = 7.3 \text{ GeV}^{-1}$
VVV	$f_1(\rho^0 D^{*+} D^{*-}) = 3.5$	$f_2(\rho^0 D^{*+} D^{*-}) = 11.5$

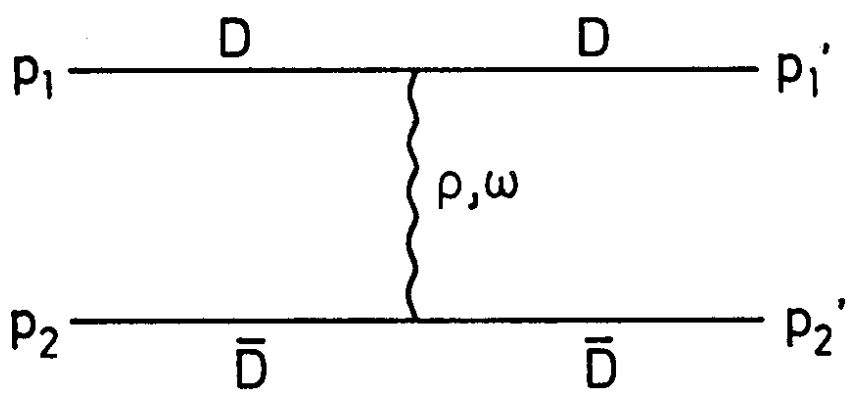


Fig. 1

Figure Captions:

Fig. 1 . Diagram for  $D\bar{D}$  scattering with  $\rho$  and  $\omega$  exchange

Table Captions:

Table 1 Calculated mass values for various spin-parity states for the strong coupling model. In the second row are the experimental masses <sup>20)</sup>.

Table 2 Coupling constants for the results in Table 1.

Table 3 Calculated mass values for various spin-parity states for the weak coupling model. In the second row we have given the experimental mass values of the charmonium spectrum <sup>20)</sup> and the measured excited states in the  $1^{--}$  state.

Table 4 Coupling constants for the results in Table 3.