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J/ψ Radiative decays into ππγ and KKγ

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Abstract: The radiative decays of J/ψ into f<sub>γ</sub>, f'γ, ππγ and KKγ have been measured using the double arm spectrometer DASP at DORIS. We find

$$B(J/\psi \rightarrow f\gamma) = \frac{J/\psi \rightarrow f\gamma}{J/\psi \rightarrow a11} = (0.9 \pm 0.3) \cdot 10^{-3} \text{ to } (1.5 \pm 0.4) \cdot 10^{-3} \text{ depending}$$

on the multipole mode of the J/ψ decay,  $B(J/\psi \rightarrow f'\gamma)/B(J/\psi \rightarrow f\gamma) \leq 1/3$  and that the relative strength of  $\frac{J/\psi \rightarrow \pi\pi\gamma}{J/\psi \rightarrow \pi\pi\omega}$  at high ππ masses is smaller by an order of magnitude than its value at the f mass.

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The large rate of some J/ψ radiative decays<sup>1,2)</sup> (e.g. J/ψ → nγ, n'γ) and the small rate of others (e.g. J/ψ → π<sup>0</sup>γ) suggests<sup>3)</sup> the possibility of a c $\bar{c}$  quark component in the n, n' mesons. The study of further J/ψ radiative decays will test these ideas and, if correct, can be used to determine the c $\bar{c}$  content of other "old" mesons. In this note we report on a measurement of J/ψ decays into ππγ and KKγ final states using the DASP detector at DORIS.

A detailed description of DASP has been given elsewhere<sup>1,4)</sup>. It consists of two identical magnetic spectrometers positioned symmetrically with respect to the interaction point (outer detector, ΔΩ ~ 0.9 sr) and a nonmagnetic detector located between the magnets (inner detector, ΔΩ ~ 9 sr). The spectrometer arms provide high momentum resolution and good particle identification by time of flight, shower energy, and range measurement<sup>4)</sup>. The inner detector can separate charged particles and photons and determine their direction with an accuracy of about one degree<sup>1)</sup>.

The total c.m. energy E was required to be in the interval 3.086 < E < 3.098 GeV centered at the J/ψ mass. A total of 1.71 · 10<sup>6</sup> J/ψ events were produced in this energy region. Candidates for e<sup>+</sup>e<sup>-</sup> → J/ψ → f<sub>γ</sub> (f → π<sup>+</sup>π<sup>-</sup>) were sought among events with a photon plus two charged particles of which at least one had its momentum measured by the outer detector and was identified as a pion.

A computer algorithm was used to preselect as ππγ candidates events with at least one outer detector track and two or three additional inner detector tracks (charged or neutral). For these events all possible track permutations were fitted to the hypothesis J/ψ → ππγ (2C fit). Thus, for an event with one outer and 3 inner tracks all three possible inner track combinations were tried with both photon or pion mass assignments making six fits altogether. Only events for which at least one combination yielded a χ<sup>2</sup> < 20.0 were retained. These were then scanned by physicists for the appropriate event topology to verify the track reconstruction and identification as provided by the computer programs. Out of 1116 scanned events, 350 were found to be consistent with the hypothesis J/ψ → ππγ (χ<sup>2</sup> < 20.0). Most of the rejected events had more than three particles in the final state.

The Dalitz plot for the ππγ events is shown in Fig. 1a. A strong concentration of events is seen near the boundaries which corresponds to low ππ or πγ masses. The invariant ππ and πγ mass distributions are plotted in Figs. 1b and 1c where enhancements are seen at the rho mass. A significant enhancement around 1250 MeV (f region) is also seen in the ππ mass distribution (Figs. 1a and 1b). Since J/ψ → ρ<sup>0</sup>γ is forbidden by charge conjugation, we assume that the

enhancements in the rho region are due to

$$J/\psi \rightarrow \pi^0 \rho^0 (\pi^0 \rightarrow \gamma\gamma) \quad (1a)$$

or  $J/\psi \rightarrow \pi^+ \rho^- (\rho^- \rightarrow \pi^0 \pi^0, \pi^0 \rightarrow \gamma\gamma) \quad (1b)$

where one  $\gamma$  from  $\pi^0$  decay escaped detection. This interpretation is supported by the charged pion angular distribution for effective  $\pi\pi$  and  $\pi\gamma$  masses in the rho region. These distributions (not shown here) are roughly proportional to  $\sin^2\theta$  as expected for reactions (1a) and (1b). The  $\chi^2$  distributions for  $J/\psi \rightarrow \pi\pi\gamma$  events in the  $\rho^0$  ( $m_{\pi\pi}^2 \leq 1.0 \text{ GeV}^2$ ) plus  $\rho^\pm$  ( $m_{\pi\gamma}^2 \leq 1.0 \text{ GeV}^2$ ) bands and in the  $f$  ( $1.0 \leq m_{\pi\pi}^2 \leq 2.0 \text{ GeV}^2$ ) band are plotted in Fig.'s 2a,b. The distribution for events in the  $\rho$ -band is much wider than expected for a 2C fit, whereas events in the  $f$ -band are in agreement with the expected distribution for  $J/\psi \rightarrow \pi\pi\gamma$ . This shows that the 1250-MeV peak corresponds to genuine  $\pi\pi\gamma$  events. The width and mass of the 1250-MeV peak are consistent with being the  $f$ . We therefore attribute the peak to

$$J/\psi \rightarrow f\gamma \rightarrow \pi^+ \pi^- \gamma \quad (2)$$

Monte-Carlo calculations which simulated reactions (1a), (1b) and (2) were used to calculate the detection efficiency for the decay  $J/\psi \rightarrow f\gamma$  and for the background below the  $f$  peak. Gaussian distributed errors, derived from the experimental data, were imposed on the Monte-Carlo events which were fitted to  $J/\psi \rightarrow \pi\pi\gamma$  using the same routines as for the data. Masses and widths from the Particle Data Group ( $M_f = 1.271 \text{ GeV}$ ,  $\Gamma_f = 0.180 \text{ GeV}$ ,  $M_\rho = 0.773 \text{ GeV}$  and  $\Gamma_\rho = 0.152 \text{ GeV}$ ) were used. For  $f$  production the form of the angular distribution  $I(\theta, \phi, \chi, \psi)$ , where  $\theta, \phi$  and  $\chi, \psi$  refer to the  $f$  production and decay angles in the helicity frame respectively<sup>+</sup>, is not unique. We therefore tried  $I(\theta, \phi, \chi, \psi) = \text{const.}$  and distributions expected for pure

<sup>+</sup> To be more specific,  $\theta$  is the angle between the  $f$  and the  $e^+$  in the  $e^+e^-$  frame.  $\chi$  and  $\psi$  are the polar and azimuthal angles of the  $\pi^+$  in the  $f$  helicity frame, i.e. in the Cartesian system with unit vectors  $\hat{X}, \hat{Y}, \hat{Z}$ , where  $\hat{Z}$  is opposite to the  $\gamma$  direction,  $\hat{Y}$  parallel to  $(e^+ \times \gamma)$  and  $\hat{X} = (\hat{Y} \times \hat{Z})$  all in the  $f$  rest frame.

E1, M2 and E3 transition in  $J/\psi \rightarrow f\gamma^+$ . For  $\rho$  production (vector  $\rightarrow$  vector + pseudoscalar) the angular distribution  $I \propto \sin^2\chi(1 + \cos^2\theta + \sin^2\theta \cos 2\psi)$  was used. The numbers  $\eta_i$  of  $f\gamma$ ,  $\rho^0\pi^0$  and  $\rho^\pm\pi^\mp$  events, detected as  $\pi\pi\gamma$ 's, ( $i = 1, 2, 3$  respectively) were then calculated in the following way. First the Dalitz plot was divided into four regions: The  $f$  band ( $1.0 \text{ GeV}^2 < m_{\pi\pi}^2 < 2.0 \text{ GeV}^2$ ), the  $\rho^0$  band ( $m_{\pi\pi}^2 < 1.0 \text{ GeV}^2$ ), the  $\rho^\pm$  band ( $m_{\pi\gamma}^2 < 1.0 \text{ GeV}^2$ ), and the rest of the Dalitz plot. Then the fractions  $\alpha_{ik}$  of  $f, \rho^0$  and  $\rho^\pm$  events to be observed as  $\pi\pi\gamma$ 's in each region ( $k = 1, 2, 3$ ) were calculated. Finally, the  $\eta_i$ 's were obtained by solving the equations  $\sum \alpha_{ik} \eta_i = m_k$  ( $k = 1, 2, 3$ ) where  $m_k$  is the number of observed  $\pi\pi\gamma$  events in the  $k$ -th region. We find that more than 90% of the observed events are due to reactions (1a), (1b) and (2).

The same fit yields  $(30.4 \pm 6.6) f\gamma$  events, detected as  $\pi\pi\gamma$ 's, in our experiment. Computing the Monte-Carlo efficiency for an isotropic  $f$  production and decay, and normalizing to the  $J/\psi \rightarrow \mu^+\mu^-$  events observed in the same experiment, we find  $B(J/\psi \rightarrow f\gamma) = (1.1 \pm 0.3) 10^{-3}$ . For pure E1, M2 and E3  $J/\psi \rightarrow f\gamma$  transitions we obtain  $B(J/\psi \rightarrow f\gamma) = (0.9 \pm 0.3) 10^{-3}$ ,  $(1.5 \pm 0.4) 10^{-3}$  and  $(1.0 \pm 0.3) 10^{-3}$  respectively. The errors in the branching ratio contain statistical and systematic uncertainties. This procedure was repeated with different  $\chi^2$  cuts and fiducial regions, on both the data and Monte-Carlo events, yielding the same results within errors.

As a consistency check, we determined from our data the  $\rho^0\pi^0$  and  $\rho^\pm\pi^\mp$  branching ratios which have been measured previously<sup>5-7</sup>. Repeating the above procedure yields  $B(J/\psi \rightarrow \rho^0\pi^0) = (0.43 \pm 0.10) 10^{-2}$  and  $B(J/\psi \rightarrow \rho^\pm\pi^\mp) = (0.93 \pm 0.18) 10^{-2}$ . These values are in good agreement with  $B(J/\psi \rightarrow \rho^0\pi^0) = (0.78 \pm 0.19) 10^{-2}$  as measured by DASP5<sup>5</sup> using the outer detector only and with  $B(J/\psi \rightarrow \rho\pi) = (1.3 \pm 0.3) 10^{-2}$  as given in ref. (6).

<sup>+</sup> Explicit expressions for  $I(\theta, \phi, \chi, \psi)$  are:

$$E1: \frac{1}{160\pi} [3T_1 + 18T_2 + 18T_3 + 3T_4 + 6T_5 - 18T_6]$$

$$M2: \frac{1}{160\pi} [15T_1 + 10T_2 + 10T_3 + 5T_4 - 10T_5 + 10T_6]$$

$$E3: \frac{1}{160\pi} [12T_1 + 32T_2 + 2T_3 - 8T_4 + 4T_5 + 8T_6]$$

where:  $T_1 = (1 + \cos^2\theta) |Y_2^0|^2$ ,  $T_2 = \sin^2\theta |Y_2^1|^2$ ,  $T_3 = (1 + \cos^2\theta) |Y_2^2|^2$

$$T_4 = \sqrt{6} \sin 2\theta \text{Re}(Y_2^1 Y_2^0^*), T_5 = \sqrt{6} \sin^2\theta \text{Re}(Y_2^2 Y_2^0^*), T_6 = \sin 2\theta \text{Re}(Y_2^2 Y_2^1)^*$$

and  $Y_\ell^m = Y_\ell^m(\chi, \psi)$

<sup>\*</sup> We have used  $B(J/\psi \rightarrow \mu^+\mu^-) = 0.069 \pm 0.009$  as given by Boyarski et al., Phys. Rev. Lett. 34 (1975) 1357 and  $B(f \rightarrow \pi^+\pi^-) = 0.54$ .

Our values for  $B(J/\psi \rightarrow f\gamma)$  are smaller but still consistent within errors with an earlier measurement of  $(2.0 \pm 0.7) \cdot 10^{-3}$  by the PLUTO-Collaboration<sup>8)</sup>.

Comparing the radiative decay to the related strong decay  $J/\psi \rightarrow f\omega$ , we find

$$R_f = \frac{B(J/\psi \rightarrow f\gamma)}{B(J/\psi \rightarrow f\omega)} \cdot \frac{PS(f\omega)}{PS(f\gamma)} \approx 0.5 \quad \text{where } (PS(f\omega)/PS(f\gamma)) = 0.89 \text{ is a small}$$

correction due to the different phase space. The ratio  $R_f$  was evaluated for  $B(J/\psi \rightarrow f\gamma) = 1.1 \cdot 10^{-3}$  and using the value for  $B(J/\psi \rightarrow f\omega)$  given in ref. (9).

The same  $R_f$  value is obtained using  $B(J/\psi \rightarrow f\gamma)$  and  $B(J/\psi \rightarrow f\omega)$  from references (8) and (10). This value for  $R_f$  is of order 1, whereas vector dominance with  $\omega$  predicts a value of the order of  $10^{-3}$ . Also note that the branching ratio  $B(J/\psi \rightarrow f\gamma)$  is similar to the values measured for  $J/\psi \rightarrow n\gamma$  and  $J/\psi \rightarrow n'\gamma$ . This may indicate that the wave function of the  $f$  also contains a small  $c\bar{c}$  component and that the radiative decay proceeds via this component as has been conjectured for the  $n$  and  $n'$  decays.

We have also determined the branching ratio for  $J/\psi \rightarrow \pi^+\pi^-\gamma$  for  $\pi^+\pi^-$  masses outside the  $f$ -region.

For  $\pi\pi\gamma$  events with  $m_{\pi\pi} < 1.0$  GeV ( $\epsilon$  region) we find that all events are consistent with  $\rho^0\pi^0$  decays as can be deduced from the amount of  $\pi^+\pi^-$  events with the same  $\chi^2$  and  $m_{\pi\pi}$  cuts. However, with the extreme pessimistic assumption that all events with  $\chi^2 < 6.0$  in this mass region are genuine radiative decays an upper limit of  $B(J/\psi \rightarrow \pi^+\pi^-\gamma) = (0.7 \pm 0.2) \cdot 10^{-3}$  is obtained for  $m_{\pi\pi} < 1.0$  GeV.

The radiative decay into a  $\pi\pi$ -system with a mass above 1.6 GeV was determined by selecting events with  $\chi^2 < 6.0$  and  $m_{\pi\pi}^2 > 1.2$  GeV<sup>2</sup>. The resulting  $\pi\pi$ -mass distribution is plotted in Fig. 3a. A total of 12 events with  $m_{\pi\pi} > 1.6$  GeV satisfied the cuts. By comparing the experimental  $\chi^2$  distribution for these events with the distributions predicted for  $\pi^+\pi^-\gamma$  and  $\pi^+\pi^0$ , we estimated a radiative signal of  $(6.1 \pm 3.9)$  events. To evaluate the detection efficiencies including corrections resulting from the cuts on  $\chi^2$  and the  $\pi\gamma$ -mass, we assumed that the  $\pi\pi$ -system is produced and decays isotropically. This yields a branching ratio of  $B(J/\psi \rightarrow \pi^+\pi^-\gamma) = (1.7 \pm 1.1) \cdot 10^{-4}$  for  $m_{\pi\pi} > 1.6$  GeV. This can be compared to the decay  $J/\psi \rightarrow \pi^+\pi^-\omega$ . We find

$$R(m_{\pi\pi} > 1.6 \text{ GeV}) = \frac{B(J/\psi \rightarrow \pi^+\pi^-\gamma)}{B(J/\psi \rightarrow \pi^+\pi^-\omega)} \cdot \frac{PS(\pi\omega)}{PS(\pi\pi\gamma)} = (0.04 \pm 0.03) \quad \text{taking the value}$$

for  $B(J/\psi \rightarrow \pi^+\pi^-\omega)$  from ref. (9). This value for  $R$  is smaller than the value for  $R_f$  by an order of magnitude. This might indicate that the high mass  $\pi^+\pi^-$  state has a smaller  $c\bar{c}$  component than the  $f$ .

A procedure similar to the one described above was used to select  $K^+K^-\gamma$  events. Events with a photon plus two charged tracks of which at least one was identified as a kaon were fitted to the hypothesis  $J/\psi \rightarrow K^+K^-\gamma$  (2C fit). The  $K^+K^-$  invariant mass distribution is shown in Fig. 3b for all events with  $\chi^2 < 20.0$ , and for events with  $\chi^2 < 6.0$  and  $m_{K\bar{K}}^2 > 1.2$  GeV<sup>2</sup> (shaded area). The  $m_{K\bar{K}}^2$  cut was introduced to eliminate  $K^+K^{*0}$  (890) reflections. We find 4 events ( $\chi^2 < 6$ ) with a  $KK$  mass between 1.553 and 1.572 GeV which differ by 40 to 60 MeV from the  $f'$  (1516) mass compared to an experimental mass resolution at this mass value of  $\sim 25$  MeV. The branching ratio  $J/\psi \rightarrow f'\gamma$  was therefore evaluated for two extreme possibilities: 1) We have no candidates for  $J/\psi \rightarrow f'\gamma$  ( $f' \rightarrow K^+K^-$ ) which yields<sup>†)</sup> a 90 % confidence upper limit  $B(J/\psi \rightarrow f'\gamma) = 1.9 \cdot 10^{-4}$ , 2) Assuming all 4 events are genuine  $f'\gamma$  events we obtain<sup>†)</sup>  $B(J/\psi \rightarrow f'\gamma) = (3.4 \pm 1.8) \cdot 10^{-4}$ . This yields  $B(J/\psi \rightarrow f'\gamma)/B(J/\psi \rightarrow f\gamma) \leq 0.3$ . Pure singlet mixing with  $c\bar{c}$  would give  $\frac{B(J/\psi \rightarrow f'\gamma)}{B(J/\psi \rightarrow f\gamma)} = 0.5$  (11). However, note that the similar branching ratios found for  $n\gamma$  and  $n'\gamma$  indicate that the mixing does not respect the SU(3) assignment. For  $m_{KK} > 1.6$  GeV we find 7 events with  $\chi^2 < 6$  yielding  $B(J/\psi \rightarrow K^+K^-\gamma) = (2.5 \pm 1.0) \cdot 10^{-4}$ . This should be taken as an upper limit since the data have not been corrected for possible background.

Our results for the branching ratios are summarized in Table I.

We wish to thank Dr. T. Walsh for his helpful discussions. We are indebted to the engineers and technicians from DESY and the collaborating institutions which have made this experiment possible by building, operating and maintaining DESY, DORIS, DASP and the Computer Center. The non-DESY members of the collaboration wish to thank the DESY directorate for their hospitality.

†) Isotropic production and decay of the  $f'$  and  $B(f' \rightarrow K^+K^-) = 0.5$  were assumed.

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By measuring the final state  $\pi\pi\gamma\gamma$  (both photons detected) the author finds  $B(J/\psi \rightarrow \rho^{\pm}\pi^{\mp}) = (0.99 \pm 0.24) 10^{-2}$  and  $B(J/\psi \rightarrow \rho^0\pi^0) = (0.39 \pm 0.15) 10^{-2}$  in good agreement with the present results.
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Submitted to Physics Letters.
9. F. Vannucci et al., Phys. Rev. D15 (1977) 1817. The value of  $B(J/\psi \rightarrow \pi\pi\omega)$  for  $m_{\pi\pi} > 1.6$  GeV was derived by multiplying  $B(J/\psi \rightarrow \pi\pi\omega) = (6.8 \pm 1.9) 10^{-3}$  by the ratio of  $\pi\pi\omega$  events with  $m_{\pi\pi} > 1.6$  GeV to all  $\pi\pi\omega$  events and correcting for the change in efficiency in the high  $m_{\pi\pi}$  region (F. Vannucci, private communication).
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Table I: Radiative decay modes of the  $J/\psi(3095)$  into  $\pi\pi\gamma$  and  $K\bar{K}\gamma$ .

Reaction	$\pi\pi(K\bar{K})$ mass region	Angular distribution <sup>a)</sup>	Branching Ratio
$J/\psi \rightarrow f\gamma$		Isotropy	$1.1 \pm 0.3 \cdot 10^{-3}$
		E1	$0.9 \pm 0.3 \cdot 10^{-3}$
		M2	$1.5 \pm 0.4 \cdot 10^{-3}$
		E3	$1.0 \pm 0.3 \cdot 10^{-3}$
$J/\psi \rightarrow f'\gamma$		Isotropy	$\leq 0.34 \cdot 10^{-3}$
$J/\psi \rightarrow \pi^+\pi^-\gamma$	<1.0 GeV	Isotropy	$\leq 0.7 \cdot 10^{-3}$
	>1.6 GeV	Isotropy	$0.17 \pm 0.11 \cdot 10^{-3}$
$J/\psi \rightarrow K^+K^-\gamma$	>1.6 GeV	Isotropy	$\leq 0.25 \cdot 10^{-3}$

a) Isotropy denotes an isotropic distribution for both production and decay except for  $J/\psi \rightarrow \pi\pi\gamma$  with  $m_{\pi\pi} < 1.0$  GeV where a production distribution of  $1 + \cos^2\theta$  was used.

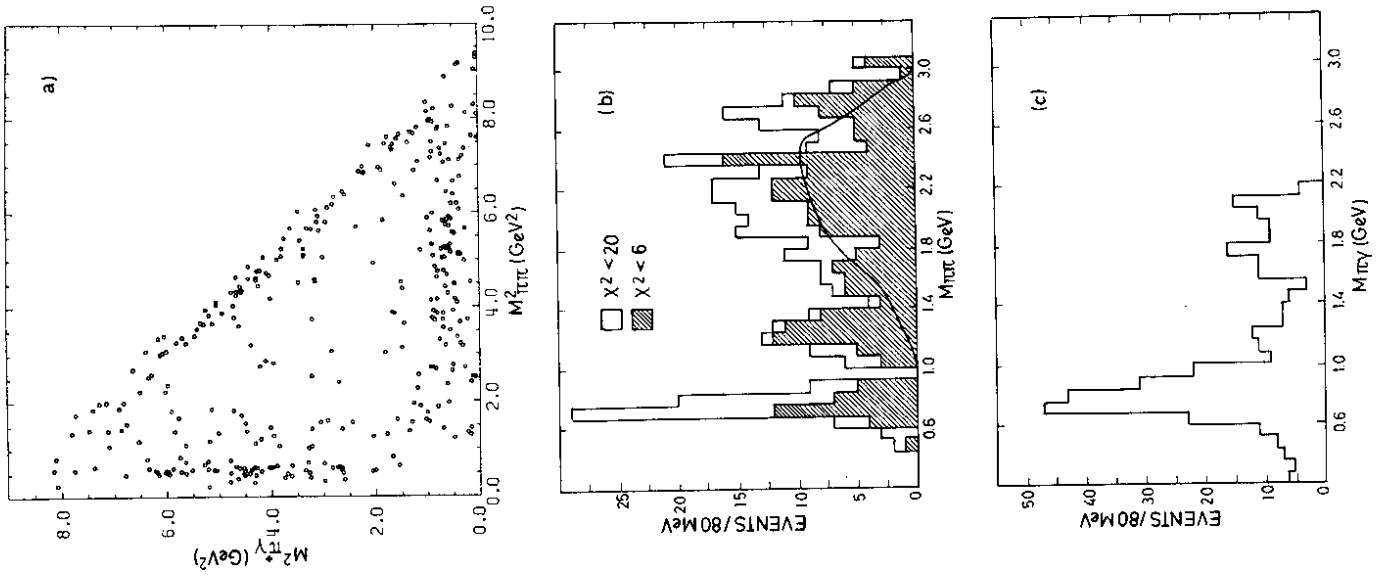


Fig. 1

**Figure Captions**

1. (a) Dalitz plot for  $e^+ e^- \rightarrow J/\psi \rightarrow \pi^+ \pi^- \gamma$  events with  $\chi^2 < 20$ .  
 (b)  $\pi^+ \pi^-$  invariant mass distribution for  $\pi^+ \pi^- \gamma$  with  $\chi^2 < 20$ .  
 The shaded area represents events with  $\chi^2 < 6$ . The line represents reflection from  $\rho^+ \pi^-$  events as calculated by Monte-Carlo ( $\chi^2 < 6$ ).  
 (c)  $\pi^\pm \gamma$  invariant mass distribution for  $\pi^+ \pi^- \gamma$  events with  $\chi^2 < 20$ . Only the low mass  $\pi\gamma$  combination is shown.
  
2.  $\chi^2$  distributions for  $\pi^+ \pi^- \gamma$  events (a) in the  $\rho^0$  band ( $m_{\pi\pi}^2 < 1.0 \text{ GeV}^2$ ) or in the  $f$  band ( $m_{\pi\gamma}^2 < 1.0 \text{ GeV}^2$ ) (b) in the  $f$  band ( $1.0 \text{ GeV}^2 < m_{\pi\pi}^2 < 2.0 \text{ GeV}^2$ ). The lines represent the expected distributions in these bands as calculated by Monte-Carlo.
  
3. (a)  $\pi^+ \pi^-$  invariant mass distribution for  $\pi^+ \pi^- \gamma$  events with  $\chi^2 < 6$  and  $m_{\pi\gamma}^2 > 1.2 \text{ GeV}^2$  for both  $\pi\gamma$  combinations.  
 (b)  $K^+ K^-$  invariant mass distribution for  $K^+ K^- \gamma$  events with  $\chi^2 < 20$ .  
 The shaded area represents  $K^+ K^- \gamma$  events with  $\chi^2 < 6$  and  $m_{K\gamma}^2 > 1.2 \text{ GeV}^2$  for both  $K\gamma$  combinations.

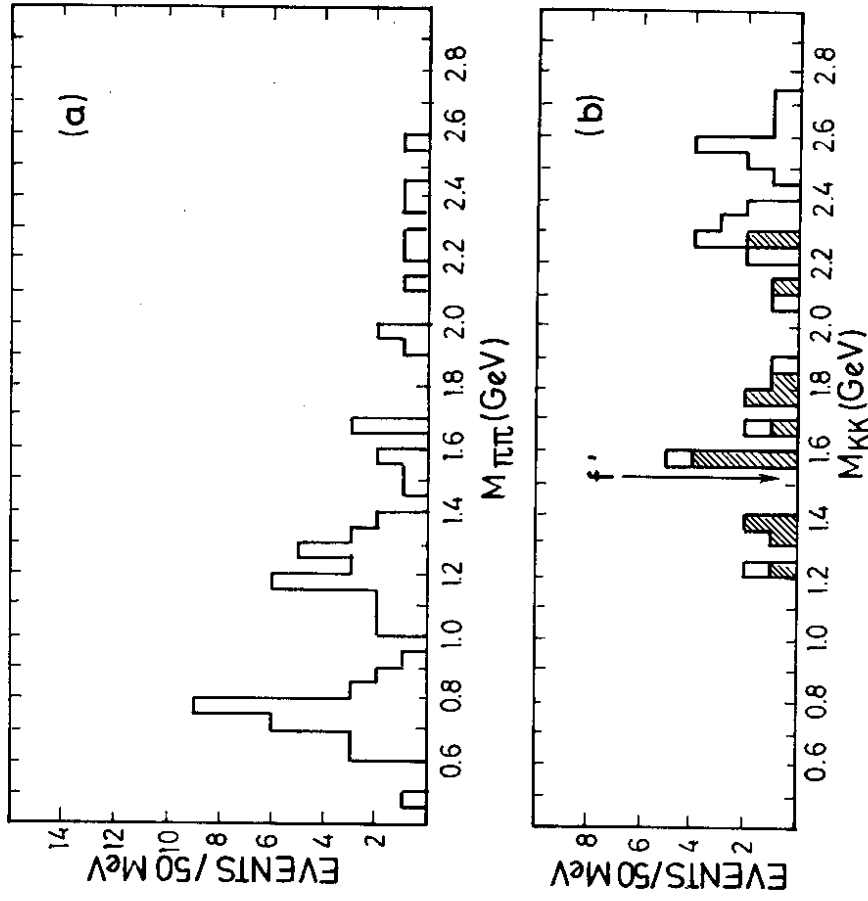


Fig.3

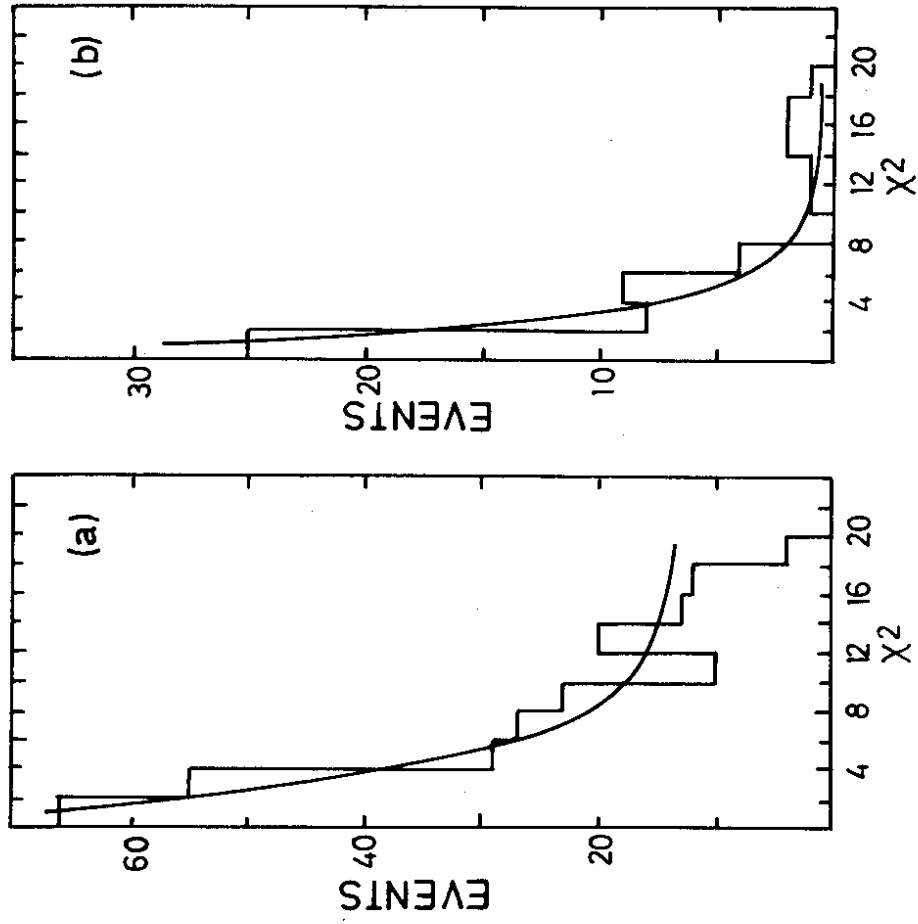


Fig.2